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USERS' GUIDE  
TO  
FOUR-BODY AND THREE-BODY TRAJECTORY  
OPTIMIZATION PROGRAMS  
by  
C. L. Pu and T. N. Edelbaum

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**USERS' GUIDE**

**to**

**Four-Body and Three-Body Trajectory  
Optimization Programs**

**by**

**C. L. Pu and T. N. Edelbaum**

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## ABSTRACT

This users' guide documents a collection of computer programs and subroutines written in FORTRAN to calculate 4-body (sun-earth-moon space) and 3-body (earth-moon space) optimal trajectories. The programs incorporate a new variable step integration technique and a new quadrature formula to correct single step errors. These new features have resulted in significant improvement in efficiency and accuracy.

The programs provide capability to solve initial value problem, two point boundary value problem of a transfer from a given initial position to a given final position in fixed time, optimal 2-impulse transfer from an earth parking orbit of given inclination to a given final position and velocity in fixed time and optimal 3-impulse transfer from a given position to a given final position and velocity in fixed time.

## INTRODUCTION

This users' guide documents a collection of computer programs and subroutines written in FORTRAN to calculate 4-body optimal trajectories under the combined influence of the sun, earth, and moon. Additional programs and subroutines have been provided so that 3-body optimal trajectories can be computed without the influence of the sun.

The method used in the extrapolation of the state vector and the solution of boundary value problems is essentially the same as presented in Ref. (1) and (2). However, the present programs incorporate a new variable step integration technique and a new quadrature formula to correct single step errors. These changes have resulted in significant improvement in efficiency and accuracy. The 4-body as well as the 3-body state extrapolation subroutine automatically determines the step size that will yield a fixed estimate of the single step position and velocity errors. The quadrature formula developed by T. N. Fdelaum is based on the 4th derivatives of the position error estimates at the beginning of a step and the second derivatives of the Stumpff-Weiss position errors at the end of the step.

In addition, two subroutines have been provided to compute target position and velocity in a Halo orbit about the  $L_1$  libration point on the sun-earth line or one of the libration points on the earth-moon line. State vectors are now available also in rotating frames similar to the familiar barycentric frame commonly used in the restricted 3-body problem. These new features will be described in some detail.

## PROGRAM ORGANIZATION

The 4-body and 3-body programs consist of 4 options. The name of a 3-body program is given in parenthesis following the name of a corresponding 4-body program.

**Option 1:** Program TRAJ (TRAJ3)

This option is a trajectory integration program to solve initial value problems.

**Option 2:** Program EXLAM (EXLAM3)

This option is a program to solve two point boundary value problem of a transfer from a given initial position to a given final position in fixed time using Newton-Raphson method.

**Option 3:** Program ETP2I (ETP2I3)

This option determines the optimal 2-impulse transfer from an earth parking orbit of given inclination to a given final position and velocity in fixed time. It employs an accelerated gradient projection method using Davidon's Variance algorithm.

**Option 4:** Program PTP3I (PTP3I3)

This option computes the optimal 3-impulse transfer from a given initial position to a given final position and velocity in fixed time. It uses an accelerated gradient method (Davidon's Variance algorithm) in the outer-loop and Newton-Raphson method in the second leg of the inner loop.

These 4 main programs call one or more of the following subroutines.

<u>Subroutine</u>	<u>Function</u>
FOURBY (THREBDY)	State extrapolation.
TWOBODY	2-body state extrapolation.
CSTEP (CSTEP3)	Computes single step size and error estimate at beginning of step.
DELRV (DELRV3)	Computes corrections by quadrature formula.
LAMB (LAMB3)	Solves Lambert problem.
CTAR (CTAR3)	Computes target position and velocity on a Halo orbit about a libration point. Called by ETP2I (ETP2I3).
COMIC (COMIC3)	Transforms input parameters with respect to earth into states with respect to sun (4-body) or earth (3-body).
COMFG (COMFG3)	Computes function and gradient in ETP2I (ETP2I3).

COMAUG	Forms augmented function and gradient in ETP2I (ETP2I3)
COMDX	Computes changes in independent variables in ETP2I (ETP2I3).
COMF (COMF3)	Computes function in PTP3I (PTP3I3).
COMG	Computes gradient in PTP3I (PTP3I3).
PVEC	Advances primer vectors and monitor its magnitude in FOURBY (THRBDY).
RVEMV	Computes state vectors in FOURBY. Not used in 3-body.
UPX	Updates variables and functions in ETP2I (ETP2I3).
DISP (DISP3)	Computes states in rotating coordinates for display.
PTRAJ (PTRAJ3)	Prints trajectory.
FDATA (FDATA3)	Files data for further processing outside of the program.

The main programs and the above mentioned subroutines will be described in some detail in the sections to follow. In addition, there are a number of service subroutines, which performs standard mathematical operations.

<u>Service Subroutines</u>	<u>Function</u>
MXV	Multiplication of a vector by a matrix, $\bar{a} = M \bar{b}$ .
VVT	Outer product of a vector, $M = \bar{a} \bar{a}^T$ .
DOT	Dot product of 2 vectors, $\bar{c} = \bar{a}^T \bar{b}$ .
VMAG	Magnitude of a vector.
INVERT	Inversion of a matrix
UNITV	Unit vector of a vector
VXV	Cross product of 2 vectors, $\bar{a} = \bar{b} \times \bar{c}$ .
MTRANS	Transpose a matrix, $N = M^T$ .
MXM	Multiplication of 2 matrices, $C = MN$

These service subroutines will be listed but not discussed further.

A tabulation of the subroutines called by the main programs is given in Table 1.

Table 1 PROGRAMS AND SUBROUTINES

Program Sub- routine	TRAJ (TRAJ3)	EXLAM (EXLAM3)	ETP2I (ETP2I3)	PTP3I (PTP3I3)
FOURBY(THRBDY)	X	X	X	X
TWOBDY	X	X	X	X
CSTEP (CSTEP3)	X	X	X	X
DELRV (DELRV3)	X	X	X	X
COMIC (COMIC3)	X	X	X	
COMFG (COMFG3)			X	
COMF (COMF3)				X
COMG				X
LAMB (LAMB3)		X		X
COMAUG			X	
COMDX			X	
CTAR (CTAR3)			X	
UPX			X	
(1) RVEMV	X	X	X	X
PVEC	X	X	X	X
DISP (DISP3)	X	X	X	X
PTRAJ (PTRAJ3)	X	X	X	X
FDATA (FDATA3)	X	X	X	X
MXV	X	X	X	X
VVT	X	X	X	X
DOT	X	X	X	X
VMAG	X	X	X	X
INVERT		X	X	X
UNITV	X	X	X	X
VXV	X	X	X	X
MTRANS			X	X
MXM	X	X	X	X

Note: 1 Not used in 3-body programs.

## COORDINATES SYSTEMS

The position or velocity vector of a body with respect to another body may be expressed in different coordinates systems at different stages of computation. These coordinates systems are described below.

<u>Coordinate Systems</u>	<u>Definition</u>
S-frame (Basic computation frame in 4-body programs)	An inertial frame centered at the sun in which state extrapolation is performed. Since it is likely that input ephemerides will be obtained from JPL tapes, the $X_S$ - $Y_S$ plane will be the Ecliptic-Equinox plane of 1950.0, with the $X_S$ -axis pointing in the Equinox direction.
E-frame (4-body)	An inertial frame centered at the earth parallel to S-frame.
M-frame (4-body)	An inertial frame centered at the moon parallel to S-frame.
e-frame (Basic computation frame in 3-body programs)	An inertial frame centered at the earth. The $X_e$ - $Y_e$ plane is the Equator-Equinox plane of 1950.0 with $X_e$ pointing in the Equinox direction.
m-frame (3-body)	An inertial frame centered at the moon parallel to e-frame.
L-frame (4-body)	A rotating frame centered at the $L_1$ libration point used to define a target on a Halo orbit about $L_1$ . The $X_L$ -axis is along the line from the sun to the earth-moon barycenter. The $Z_L$ -axis is along the total angular momentum vector of the earth and moon about the sun.
$L_1$ -frame (3-body)	A rotating frame centered at either $L_1$ or $L_2$ libration point to define a target on a Halo orbit. The $X_{L_1}$ -axis is along the line from the earth to the moon. The $Z_{L_1}$ -axis is along the angular momentum vector of the moon about the earth.

O-frame

An inertial frame centered at the earth. The  $X_O$ - $Y_O$  plane is the parking orbit plane of an inclination  $i$ . The  $X_O$ -axis is along the line of ascending node.

D-frame  
(4-body)

A rotating frame centered at the earth used for display purpose. This frame is the equivalent of the rotating barycentric frame in a restricted 3-body problem. The  $X_D$ -axis is along the line from the sun to the earth. The  $Z_D$ -axis is along the angular momentum vector of the earth about the sun.

d-frame  
(3-body)

A rotating frame centered at the moon used for display purpose. The  $X_d$ -axis is along the line from the earth to the moon. The  $Z_d$ -axis is along the angular momentum vector of the moon about the earth.

These frames are shown in Figure 1.

In general, when there is no ambiguity, a vector of a body A with respect to another body B will be written with subscripts BA. For example,  $\bar{R}_{SV}$  will be a position vector of the vehicle with respect to the sun in the S-frame. Sometimes, it is necessary to add a superscript to indicate the frame in which the components are resolved. Thus,  $\bar{\omega}_{SL}^S$  is the angular velocity of the L-frame with respect to the S-frame with components in the S-frame.

A transformation matrix will be denoted by a subscript and a superscript. It will transform a vector from the frame indicated by the subscript to the frame indicated by the superscript. For example  $\bar{R}^L = C_S^L \bar{R}^S$  transforms  $\bar{R}$  in S-frame to  $\bar{R}$  in L-frame.

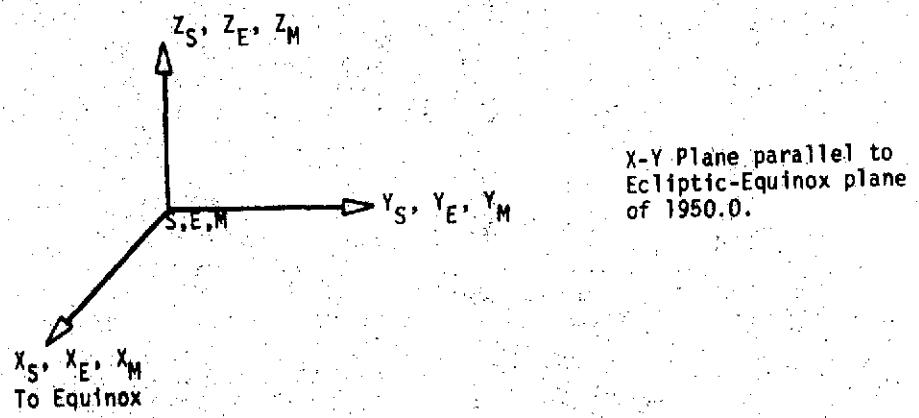


Figure 1a Inertial S, E, and M Frames

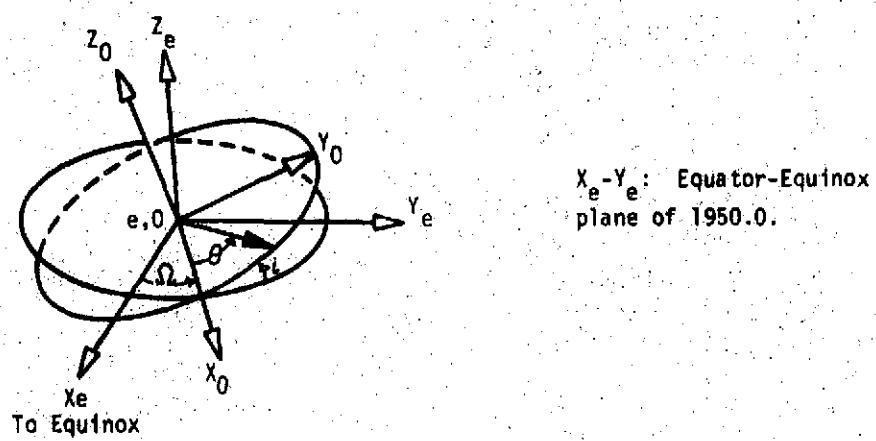


Figure 1b Inertial e and O Frames

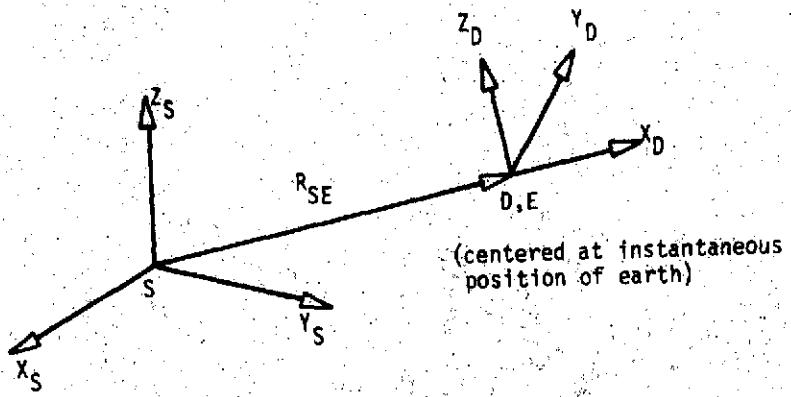


Figure 1c D-Frame

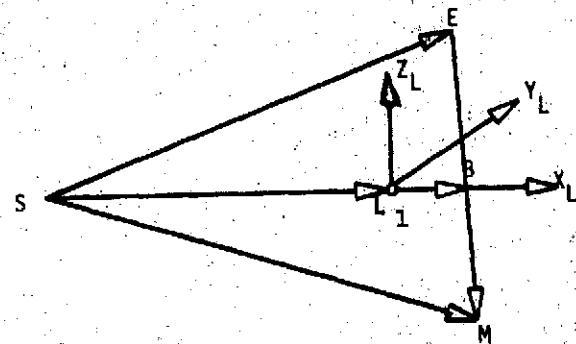


Figure 1d L-Frame

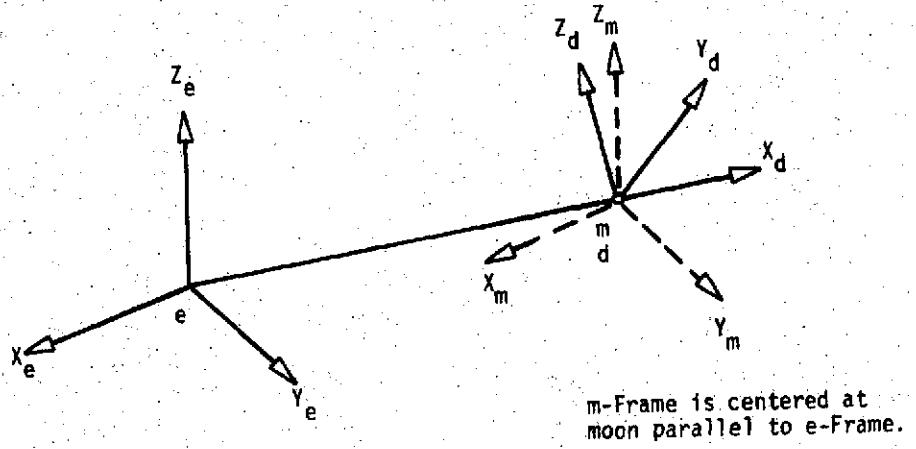


Figure 1e m and d Frames

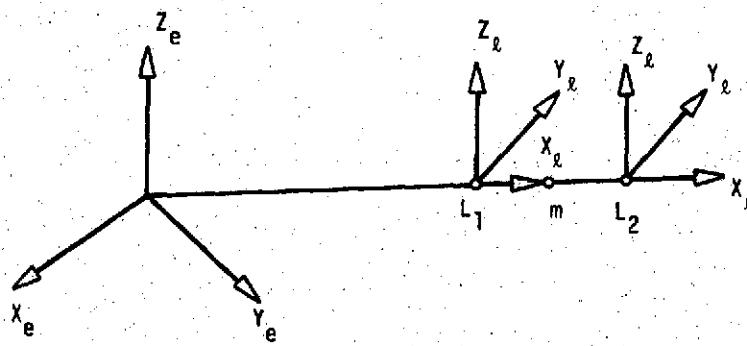


Figure 1f l Frame

## VARIABLE STEP INTEGRATION

The variable step integration technique used in subroutine FOURBY (THRBDY) is summarized here. The computation of step size and estimates of position errors, which is performed in subroutine CSTEP (CSTEPS), is an extension of D'Amario's derivation for the 3-body problem (Ref. 4). Let

$\bar{R}'(t+h)$  = approximate vehicle position determined by Stumpff-Weiss method

$\bar{R}(t+h)$  = true vehicle position

The position error at the end of a single step is

$$\bar{\epsilon}(t+h) = \bar{R}(t+h) - \bar{R}'(t+h) \quad (1)$$

Expanding Eq. (1) in Taylor series at  $t$  we obtain

$$\bar{\epsilon}(t+h) = \bar{\epsilon}(t) + \dot{\bar{\epsilon}}(t)h + \frac{1}{2}\ddot{\bar{\epsilon}}(t)h^2 + \frac{1}{6}\dddot{\bar{\epsilon}}(t)h^3 + \frac{1}{24}\bar{\epsilon}^{(4)}(t)h^4 + O(h^5) \quad (2)$$

By definition,

$$\bar{\epsilon}(t) = 0. \quad (3)$$

It can be shown that

$$\dot{\bar{\epsilon}}(t) = \ddot{\bar{\epsilon}}(t) = \dddot{\bar{\epsilon}}(t) = 0 \quad (4)$$

The first non-zero term is the 4th derivative term. Neglecting all higher derivative terms the position error is given by

$$\bar{\epsilon}(t+h) \approx \frac{1}{24}\bar{\epsilon}^{(4)}(t)h^4 \quad (5)$$

Let

$$|\bar{\epsilon}(t+h)| = \epsilon_{\max} \quad (6)$$

= allowable single step position error.

Then, an estimate of step size is given by

$$h = \left( 24 \frac{\epsilon_{\max}}{\bar{\epsilon}(t)} \right)^{1/4} \quad (7)$$

In CSTEP we compute  $\epsilon_{RSV}$  to estimate step size  $h$  and also  $\epsilon_{RSE}$  and  $\epsilon_{RSM}$  for use in DELRV to compute error corrections. If we make the following definitions in a 4-body space,

$$G_{SV} = \frac{\partial}{\partial \bar{R}_{SV}} \left[ -\mu_S \frac{\bar{R}_{SV}}{R_{SV}^3} \right] = \frac{\partial}{\partial \bar{R}_{SV}} \left[ \frac{\mu}{\bar{R}_{SV}} \right]$$

$$G_{EV} = \frac{\partial}{\partial \bar{R}_{EV}} \left[ -\mu_E \frac{\bar{R}_{EV}}{R_{EV}^3} \right] = \frac{\partial}{\partial \bar{R}_{EV}} \left[ \frac{\mu}{\bar{R}_{EV}} \right]$$

$$G_{SE} = \frac{\partial}{\partial \bar{R}_{SE}} \left[ -(\mu_S + \mu_E) \frac{\bar{R}_{SE}}{R_{SE}^3} \right] = \frac{\partial}{\partial \bar{R}_{SE}} \left[ \frac{\mu}{\bar{R}_{SE}} \right] \quad (8)$$

$$G_{MV} = \frac{\partial}{\partial \bar{R}_{MV}} \left[ -\mu_M \frac{\bar{R}_{MV}}{R_{MV}^3} \right] = \frac{\partial}{\partial \bar{R}_{MV}} \left[ \frac{\mu}{\bar{R}_{MV}} \right]$$

$$G_{SM} = \frac{\partial}{\partial \bar{R}_{SM}} \left[ -(\mu_S + \mu_M) \frac{\bar{R}_{SM}}{R_{SM}^3} \right] = \frac{\partial}{\partial \bar{R}_{SM}} \left[ \frac{\mu}{\bar{R}_{SM}} \right]$$

$$\delta \bar{g}_{SV} = \bar{R}_{SV} - \left[ \bar{R}_{SV} \right]$$

$$\delta \bar{g}_{EV} = \bar{R}_{EV} - \left[ \bar{R}_{EV} \right]$$

$$\delta \bar{g}_{SE} = \bar{R}_{SE} - \left[ \bar{R}_{SE} \right] \quad (9)$$

$$\delta \bar{g}_{MV} = \bar{R}_{MV} - \left[ \bar{R}_{MV} \right]$$

$$\delta \bar{g}_{SM} = \bar{R}_{SM} - \left[ \bar{R}_{SM} \right]$$

we can express the estimated errors by

$$\begin{aligned}
\bar{\epsilon}_{RSV}^{(t+h)} &= \left\{ G_{SV} \delta \bar{g}_{SV} + G_{EV} \delta \bar{g}_{EV} + \frac{\mu_E}{\mu_S + \mu_E} G_{SE} \delta \bar{g}_{SE} \right. \\
&\quad \left. + G_{MV} \delta \bar{g}_{MV} + \frac{\mu_M}{\mu_S + \mu_M} G_{SM} \delta \bar{g}_{SM} \right\} \frac{h^4}{24} + O(h^5) \\
\bar{\epsilon}_{RSE}^{(t+h)} &= \left\{ G_{SE} \delta \bar{g}_{SE} - \frac{\mu_M}{\mu_E + \mu_M} G_{EM} \delta \bar{g}_{EM} \right. \\
&\quad \left. + \frac{\mu_M}{\mu_S + \mu_M} G_{SM} \delta \bar{g}_{SM} \right\} \frac{h^4}{24} + O(h^5) \\
\bar{\epsilon}_{RSM}^{(t+h)} &= \left\{ G_{SM} \delta \bar{g}_{SM} + \frac{\mu_E}{\mu_E + \mu_M} G_{EM} \delta \bar{g}_{EM} \right. \\
&\quad \left. + \frac{\mu_E}{\mu_S + \mu_E} G_{SE} \delta \bar{g}_{SE} \right\} \frac{h^4}{24} + O(h^5)
\end{aligned} \tag{10}$$

In CSTEP3 we compute  $\bar{\epsilon}_{REV}^{***}$  to determine  $h$  and the error may be expressed by

$$\bar{\epsilon}_{REV}^{(t+h)} = \left\{ G_{EV} \delta \bar{g}_{EV} + G_{MV} \delta \bar{g}_{MV} \right\} \frac{h^4}{24} + O(h^5) \tag{11}$$

Note that  $\bar{\epsilon}_{REM}^{***} = 0$  in a 3-body space.

## CORRECTION OF ERRORS BY QUADRATURE FORMULAS

The quadrature formulas proposed by T. N. Edelbaum and used in subroutine DELRV (DELRV3) to compute a single step position and velocity corrections are presented here.

Assume the second derivative of the position error in a single step is given by

$$\ddot{\epsilon} = \frac{t^2}{2} (\bar{a} + \bar{b} t) \quad (12)$$

where

$$\bar{a} = \ddot{\epsilon}(0) = \ddot{\epsilon}_0 \quad (13)$$

Then the second derivative of the position error at the end of a singl step is given by

$$\ddot{\epsilon}_1 = \frac{h^2}{2} (\bar{a} + \bar{b} h) \quad (14)$$

Solving Eq. (14) and using Eq. (13),

$$\bar{b} = \frac{2\ddot{\epsilon}_1 - \ddot{\epsilon}_0}{h^3} \quad (15)$$

Integrating Eq. (12)

$$\dot{\epsilon} = \frac{\bar{a}t^3}{6} + \frac{\bar{b}t^4}{8} \quad (16)$$

$$\dot{\epsilon} = \frac{\bar{a}t^4}{24} + \frac{\bar{b}t^5}{40} \quad (17)$$

Using Eqs.(13) and (15) in (16) and (17), we obtain the following corrections at the end of a single step,

$$\dot{\epsilon}_1 = \frac{h}{4} \left( \ddot{\epsilon}_0 \frac{h^2}{6} + \ddot{\epsilon}_1 \right) \quad (18)$$

$$\dot{\epsilon}_1 = \frac{h^2}{20} \left( \ddot{\epsilon}_0 \frac{h^2}{3} + \ddot{\epsilon}_1 \right) \quad (19)$$

$\ddot{\epsilon}_0$  is the 4th derivative of position error estimate at the beginning of a step and  
 $\ddot{\epsilon}_1$  is the second derivative of Stumpff-Weiss error estimate at the end of the step.

## INPUT PARAMETERS

The following input parameters are required for all 4 options.

<u>Parameters</u>	<u>Symbol or Definition</u>	<u>Suggested Value</u>
<u>4-Body Programs:</u>		
GL1	$\gamma_{L1}$	$1.001098 \times 10^{-2}$
AUM	1 unit of distance in meters	$1.49597893 \times 10^{11} \text{ m}$
UTIME	1 unit of time in days	58.1323577631 days
UVELM	1 m/s in dimensionless velocity	$3.35742409867 \times 10^{-5}$
MS	$\mu_S$ (sun)	$9.99996959568 \times 10^{-1}$
ME	$\mu_E$ (earth)	$3.00348453188 \times 10^{-6}$
MM	$\mu_M$ (moon)	$3.69431224671 \times 10^{-8}$
RSE0	$\overline{R}_{SE}(t_0)$	
VSE0	$\overline{V}_{SE}(t_0)$	
RSM0	$\overline{R}_{SM}(t_0)$	
VSM0	$\overline{V}_{SM}(t_0)$	
<u>3-Body Programs (Ref. 4 and 5)</u>		
GAMMA	$\gamma$	$\gamma_{L1} = 0.150935$ $\gamma_{L2} = -0.187833$
UDM	1 unit of distance in meters	$3.8441 \times 10^8 \text{ m}$
UTIME	1 unit of time	104.362/24 days
UVELM	1 m/s in dimensionless velocity	1/1023.17 m/s

ME	$\mu_E$ (earth)	.9878493
MM	$\mu_M$ (moon)	.0121507
REMO	$R_{EM}(t_0)$	
VEM0	$V_{EM}(t_0)$	

Common to both 4- and 3-Body Programs:

IPV	Flag to compute primer vector	IPV = 0, no 1, yes
IPTRAJ (IPTJX)	Flag to print trajectory each time step	IPTRAJ (IPTJX) = 0, no 1, yes
IFILEX (IFILE)	Flag to file data each time step	IFILEX (IFILE) = 0, no 1, yes
ERRMXM	Allowable single step position error in meters	150 m or higher
ERRMAX	Dimensionless ERRMXM	$10^{-9}$ or higher
TDAY0	Starting time in days from reference date	
TRIPD	Trip time in days	

The following input parameters are required for Davidon's variance algorithm used in ETP2I (ETP2I3) and PTP3I (PTP3I3). See Ref. 2, Appendix A.

EPS                   $10^{-11}$  for ETP2I (ETP2I3)  
 $10^{-3}$  for PTP3I (PTP3I3)

V

V

ICOMV

EPSV

Davidon's Variance matrix.

If ICOMV = 1, this input is not needed and the program will compute an estimate. Once a working V matrix has been developed through iterations, it should be used in a new run to continue iteration.

Flag to compute V.

ICOMV = 0, no (input V)

1, yes

Small number to scale down  
V matrix if ICOMV = 1. It specifies  
the magnitude of the first step in the  
gradient direction. A typical value  
is about  $10^{-5}$ .

## PROGRAM TRAJ (TRAJ3)

### A. Input Parameters

<u>Parameters</u>	<u>Symbol</u>	<u>Definition/ Value</u>
IMODE		Mode to select input IMODE = 1, 2, or 3
	<u>IMODE = 1</u>	
REVMAG	$ \bar{R}_{EV}(t_o) $	$4.38739157152 \times 10^{-5}$ for 100 n.m. parking orbit.
VEVMAG	$ \bar{V}_{EV}^+(t_o) $	Estimate of departure velocity magnitude with respect to earth.
OINCD	$i$ (deg)	Inclination of earth parking orbit.
OBLD	OBL (deg)	Obliquity angle = $23.44578743018259$ deg between E-frame and e-frame.
(not used in 3-body)		
THED	$\theta$ (deg)	Position of vehicle from ascending node in orbital plane.
LOND	$\Omega$ (deg)	Longitude of ascending node.
	<u>IMODE = 2</u>	
REVO	$\bar{R}_{EV}(t_o)$	
VEVOP	$\bar{V}_{EV}^+(t_o)$	
	<u>IMODE = 3</u>	
RSV0	$\bar{R}_{SV}(0)$	
VSVI	$\bar{V}_{SV}^+(0)$	

### B. Computation

Inputs of IMODE = 1 or 2 are converted into position and velocity of vehicle in S-frame or e-frame. The initial states are propagated to the final time using subroutine FOURBY (THRBDY).

### C. Output Parameters

Terminal states are printed out. States at each time step will be printed out if IPTRAJ = 1 and they will be filed if IFILE = 1.

## PROGRAM EXLAM (EXLAM3)

### A. Input Parameters

<u>Parameters</u>	<u>Symbol/Unit</u>	<u>Definition/ Value</u>
IMODE		Mode to select input IMODE = 1 or 2
Same inputs for IMODE = 1, 2 as shown under PROGRAM TRAJ (TRAJ3)		
ERRMIN	$\epsilon_{\text{MIN}}$	Allowable error for stopping Newton-Raphson method ( $10^{-10}$ )
KNR		Initial estimate of change in initial velocity magnitude (1)
ITLMAX		Maximum number of iterations (50)
RSVTAR	$R_{SV}(t_f)$	Target position
IPTJX		Flag to compute and print trajectory after convergence IPTJX = 0, no 1, yes
IFILEX		Flag to compute and file trajectory after convergence IFILEX = 0, no 1, yes

### B. Computation

Program calls subroutine LAMB (LAMB3) to solve the boundary value problem.

### C. Output Parameters

Outputs are given under subroutine LAMB (LAMB3). If either IPTJX = 1 or IFILEX = 1, the trajectory after convergence will be printed or filed or both.

## PROGRAM ETP2I (ETP2I3)

### A. Input Parameters

<u>Parameter</u>	<u>Symbol</u>	<u>Definition</u>
ITAR		Flag to input or compute target ITAR = 0, compute 1, input
REVMAG	$ R_{EV}(t_o) $	
OINCD	i (deg)	
OBLD	OBL (deg)	
TDAY0	$t_o$ (deg)	
TTRIPD		$t_f - t_o$ (day)
VEVMAG	$ \nabla_{EV}(t_o) $	
LOND	$\Omega$ (deg)	
THED	$\theta$ (deg)	
KDX		Initial value of constraint restoration parameter (start with KDX = 1)
EPSV		V-matrix scaling
EPSTSI		Allowable constraint violation ( $10^{-10}$ )
ITERMX		Max. No. of iterations
ITAR = 0:		Parameter to define target on Halo orbit. $A_y = 2 \times 10^5$ km $A_z = 1 \times 10^5$ km $A_{TAR}$ = Target position measured from $X_L$ or $X_R$ axis.
AYM	$A_y$ (m)	
AZM	$A_z$ (m)	
ATARD	$A_{TAR}$ (deg)	
4-Body:		
RSE0	$R_{SE}(t_o)$	
VSE0	$\bar{V}_{SE}(t_o)$	
RSM0	$\bar{R}_{SM}(t_o)$	
VSM0	$\bar{V}_{SM}(t_o)$	

ITAR = 1:

RSVTAR

$$\bar{R}_{SVTAR}(t_f)$$

VSVTAR

$$\bar{V}_{SVTAR}(t_f)$$

3-Body:

REMO

$$\bar{R}_{EM}(t_o)$$

VEMO

$$\bar{V}_{EM}(t_o)$$

ITAR = 1:

REVSTAR

$$\bar{R}_{EVTAR}(t_f)$$

VEVTAR

$$\bar{V}_{EVTAR}(t_f)$$

### B. Computation

See Ref. 2 appendix, program listing and flow chart.

### C. Internal Parameters

ALPHA, BETA

Davidon algorithm parameters

ALPHAM, BETAM

Davidon algorithm parameters

Current Variables	Trial Variables	Dummy Variables	
X	XS	XD	Independent variables
F	FS	FD	Cost
G	GS	GD	Cost gradient
FG	FGS	FGD	Augmented cost
TSI	TSIS	TSID	Constraint violation
LT	LTS	LTD	Constraint gradient
GG	GGS	GGD	Augmented cost gradient
TESTR	TESTRS	TESTRD	Magnitude of constraint violation
KDX			Constraint restoration scaling (internally adjusted)

**KV**

V matrix internal scaling  
(internally determined)

**R**

Parameters to compute quantities  
to update V matrix

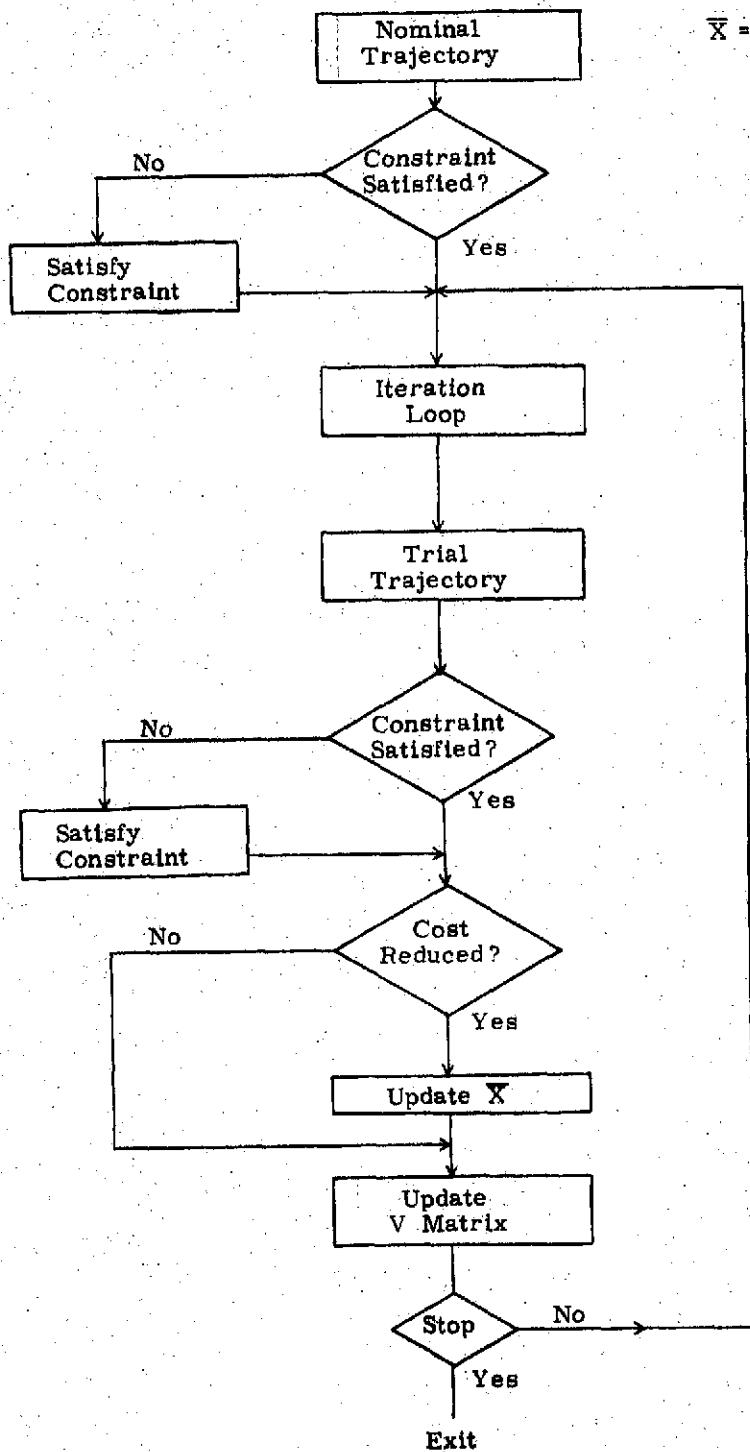
**P**

Estimate of twice the excess of cost  
above its minimum value. If  
 $P < EPS$ , the problem is considered  
to be converged.

**Program ETP2I and ETP2IS**

$\bar{X}$  = Independent Variables

$$\bar{X} = \left( |\bar{V}_{EV}(t_0)|, \Omega, \theta \right)$$



**PROGRAM PTP3I(PTPSI3)**

**A. Input Parameters**

<u>Parameters</u>	<u>Symbol</u>	<u>Definition</u>
<b>4-Body:</b>		
RSV0	$\bar{R}_{SV}(t_0)$	
VSV0	$\bar{V}_{SV}^-(t_0)$	Velocity before initial impulse
VSVI	$\bar{V}_{SV}^+(t_0)$	Velocity after initial impulse
RSE0	$\bar{R}_{SE}(t_0)$	
VSE0	$\bar{V}_{SE}(t_0)$	
RSM0	$\bar{R}_{SM}(t_0)$	
VSM0	$\bar{V}_{SM}(t_0)$	
VSVMP	$\bar{V}_{SM}^+(t_m)$	Velocity after interior impulse
TM	$t_m$	Time of interior impulse
RSVTAR	$\bar{R}_{SVTAR}(t_f)$	Target position
VSVTAR	$\bar{V}_{SVTAR}(t_f)$	Target velocity
<b>3-Body:</b>		
REVO	$\bar{R}_{EV}(t_0)$	
VEVO	$\bar{V}_{EV}^-(t_0)$	Velocity before impulse
VEVOP	$\bar{V}_{EV}^+(t_0)$	Velocity after impulse
REMO	$\bar{R}_{EM}(t_0)$	
VEM0	$\bar{V}_{EM}(t_0)$	
VEVMP	$\bar{V}_{EV}^+(t_m)$	Velocity after interior impulse
TM	$t_m$	Time of interior impulse

**Common to 4-Body and 3-Body:**

ITLMAX

Maximum number of Lambert iterations

ILINC

Number of increments to solve Lambert problem

ITDMAX

Maximum number of Davidon iterations

FMINM

Estimated minimum value of  $\Delta V$  (m/s)

KNR

Lambert iteration parameter  
(use KNR = 1 to start)

ERRMIN

Allowable constraint violation ( $10^{-10}$ )

**B. Computation**

See Ref. 2, program listing and flow chart.

**C. Internal Parameters**

SG

Projection of cost gradient on search direction.

ALPHA

Step size in search direction

SGS

Projection of trial point cost gradient on search direction. Its sign is used to determine whether an interpolation or a reduction of interval is to be made.

R, RC

Parameters to update V matrix.  
R used in trial step. RC used in interpolation.

ALPHAC

Step size in search direction determined by cubic interpolation.

P, PC

Parameters to update V matrix.  
P used in trial step. PC used in interpolation

**EPS**

If magnitude of cost gradient is less than EPS, the problem is considered to be converged.

**F**

Cost

**GMAG**

Magnitude of cost gradient.

**GSMAG**

Magnitude of cost gradient of a trial point.

**GCMAG**

Magnitude of cost gradient of an interpolated point.

**RMAG**

Magnitude of R.

**RCMAG**

Magnitude of RC.

**FS**

Cost of a trial point.

**FC**

Cost of an interpolated point.

**DG**

Difference in cost gradient.

**DX**

Change in independent variable to compute a trial point.

**DXC**

Change in independent variable to compute an interpolated point.

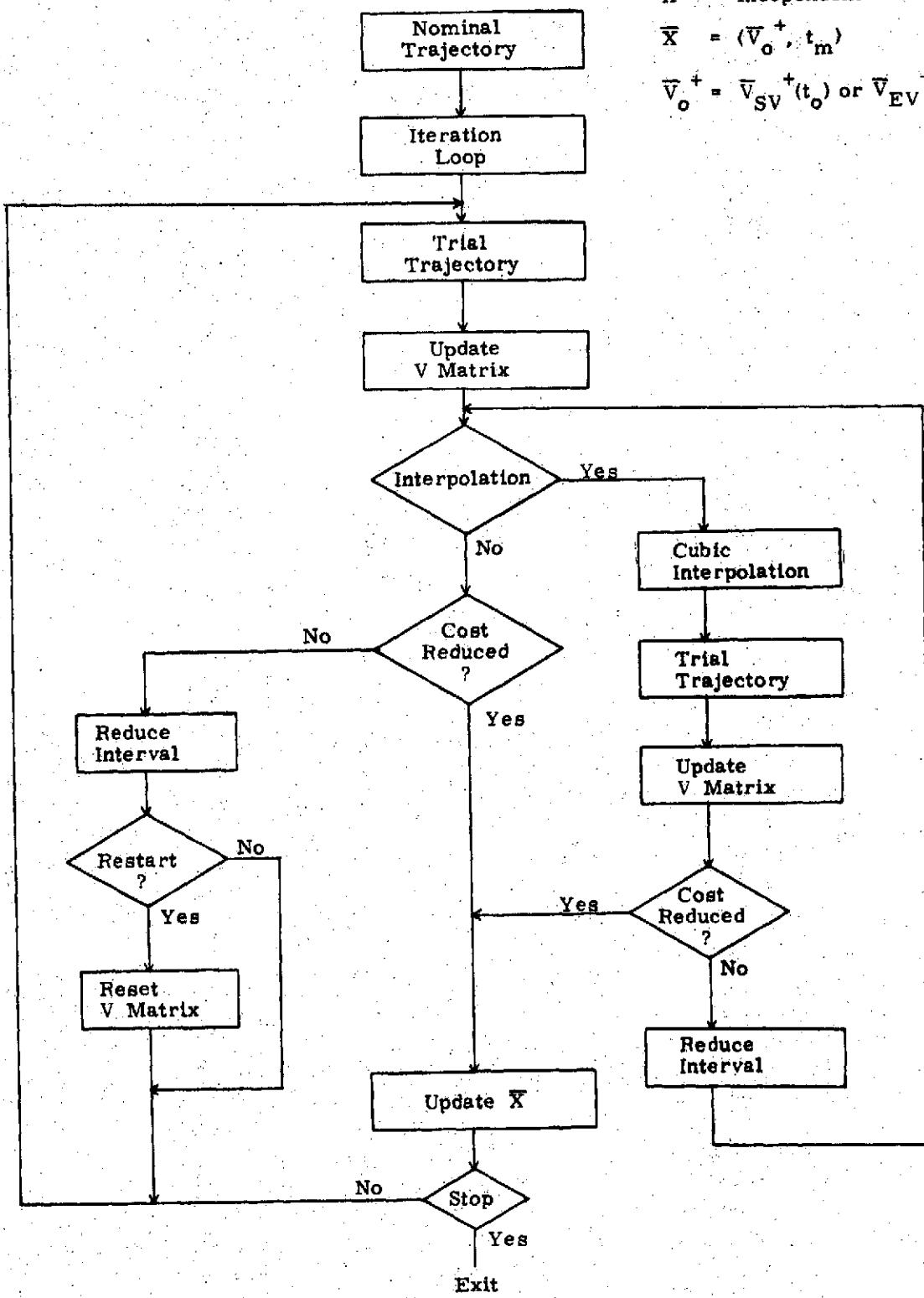
**PVMMAG, PVP MAG**

See subroutine COMG

**D. Stopping Options**

The programmed stopping condition is when GMAG is reduced to less than EPS. However, one should stop the iteration if F is not decreasing significantly from one iteration to the next. On the other hand, it may be necessary to continue iteration to satisfy the condition that PVMMAG is nearly equal to PVP MAG. (See comment in Ex. 4.)

Program PTP3I and PTP3IS



$\mathbf{X}$  = Independent Variables

$$\bar{\mathbf{X}} = (\bar{V}_o^+, t_m)$$

$$\bar{V}_o^+ = \bar{V}_{SV}^+(t_o) \text{ or } \bar{V}_{EV}^+(t_o)$$

## INPUT DATA DECKS

### Program TRAJ

<u>Card No.</u>	<u>Format</u>	<u>Parameters</u>
1	4D20.11	GLI, AUM, UTIME, UVELM
2	3D20.11	MS, ME, MM
3	415	IMODE, IPV, IPTRAJ, IFILE
4	4D20.11	RSE0(1), RSE0(2), RSE0(3), VSE0(1)
5	4D20.11	VSE0(2), VSE0(3), RSM0(1), RSM0(2)
6	4D20.11	RSM0(3), VSM0(1), VSM0(2), VSM0(3)
7	3D20.11	TDAY0, TRIPD, ERRMXM

The above 7 input cards are needed for all modes. The following 2 cards depend on the mode selected

		IMODE = 1
8	4D20.11	REVMAG, VEVPMAG, OINCD, OBLD
9	2D20.11	LOND, THED
		IMODE = 2
8	4D20.11	REVO(1), REVO(2), REVO(3), VEVOP(1)
9	2D20.11	VEVOP(2), VEVOP(3)
		IMODE = 3
8	4D20.11	RSV0(1), RSV0(2), RSV0(3), VSVI(1)
9	2D20.11	VSVI(2), VSVI(3)
		The following 2 input cards are needed if IPV = 1
10	4D20.11	PV0(1), PV0(2), PV0(3), PV0(4)
11	2D20.11	PV0(5), PV0(6)

**Program TRAJ3**

<u>Card No.</u>	<u>Format</u>	<u>Parameters</u>
1	4D20.11	GAMMA, UDM, UTIME, UVELM
2	2D20.11	ME, MM
3	4D20.11	IMODE, IPV, IPTRAJ, IFILE
4	4D20.11	REMO(1), REMO(2), REMO(3), VEMO(1)
5	2D20.11	VEMO(2), VEMO(3)
6	3D20.11	TDAY0, TRIPD, ERRMXM

The above 6 input cards are needed for all modes. The following 2 cards depend on the mode selected.

IMODE = 1

7	4D20.11	REVMAG, VEVMAG, OINCD, LOND
8	1D20.11	THED

IMODE = 2

7	4D20.11	REV0(1), REV0(2), REV0(3), VEV0P(1)
8	2D20.11	VEV0P(2), VEV0P(3)

The following 2 cards are needed if IPV = 1

9	4D20.11	PV0(1), PV0(2), PV0(3), PV0(4)
10	2D20.11	PV0(5), PV0(6)

**Program EXLAM**

<u>Card No.</u>	<u>Format</u>	<u>Parameters</u>
1	4D20.11	GLI, AUM, UTIME, UVELM
2	3D20.11	MS, ME, MM
3	4I5	IMODE, ITLMAX, IPTJX, IFILEX
4	4D20.11	RSE0(1), RSE0(2), RSE0(3), VSE0(1)
5	4D20.11	VSE0(2), VSE0(3), RSM0(1), RSM0(2)
6	4D20.11	RSM0(3), VSM0(1), VSM0(2), VSM0(3)
7	3D20.11	TDAY0, TRIPD, ERRMXM
8	4D20.11	RSVTAR(1), RSVTAR(2), RSVTAR(3), ERRMIN
9	1D20.11	KNR

The above 9 cards are needed for all modes. The following cards depend on the mode selected.

		IMODE = 1
10	4D20.11	REVMAG, VEVmag, OINCD, OBLD
11	2D20.11	LOND, THED
		IMODE = 2
10	4D20.11	REV0(1), REV0(2), REV0(3), VEV0P(1)
11	2D20.11	VEV0P(2), VEV0P(3)
		IMODE = 3
10	4D20.11	RSV0(1), RSV0(2), RSV0(3), VSVI(1)
11	2D20.11	VSVI(2), VSVI(3)

**Program EXLAM3**

<u>Card No.</u>	<u>Format</u>	<u>Parameters</u>
1	4D20.11	GAMMA, UDM, UTIME, UVELM
2	2D20.11	ME, MM
3	415	IMODE, ITLMAX, IPTJX, IFILEX
4	4D20.11	REMO(1), REMO(2), REMO(3), VEMO(1)
5	2D20.11	VEMO(2), VEMO(3)
6	3D20.11	TDAY0, TRIPD, ERRMXM
7	4D20.11	REVTAR(1), REVTAR(2), REVTAR(3), ERRMIN
8	1D20.11	KNR

The above 8 cards are needed for all modes. The following cards depend on the mode selected.

IMODE = 1

9	4D20.11	REVMAG, VEVPMAG, OINCD, LOND
10	1D20.11	THED

IMODE = 2

9	4D20.11	REVO(1), REVO(2), REVO(3), VEVOP(1)
10	2D20.11	VEVOP(2), VEVOP(3)

**Program ETP2I**

<u>Card No.</u>	<u>Format</u>	<u>Parameters</u>
1	4D20.11	GLI, AUM, UTIME, UVELM
2	3D20.11	MS, ME, MM
3	4D20.11	REVMAG, OINCD, OBLD, ERRMXM
4	2D20.11	TDAY0, TTRIPD
5	3D20.11	VEVMAG, LOND, THED
6	4D20.11	RSE0(1), RSE0(2), RSE0(3), VSE0(1)
7	4D20.11	VSE0(2), VSE0(3), RSM0(1), RSM0(2)
8	4D20.11	RSM0(3), VSM0(1), VSM0(2), VSM0(3)
9	4D20.11	EPS, EPSTSI, KDX, EPSV
10	415	ICOMV, ITERMX, IFILEX, ITAR

The next 1 or 2 cards depend on ITAR.

ITAR = 0

11	3D20.11	AYM, AYZ, ATARD
----	---------	-----------------

ITAR = 1

11	4D20.11	RSVTAR(1), RSVTAR(2), RSVTAR(3), VSVTAR(1)
12	2D20.11	VSVTAR(2), VSVTAR(3)

The following 3 cards are needed only if ICOMV = 0.

13	4D20.11	V(1, 1), V(1, 2), V(1, 3), V(2, 1)
14	4D20.11	V(2, 2), V(2, 3), V(3, 1), V(3, 2)
15	4D20.11	V(3, 3)

**Program ETP213**

<u>Card No.</u>	<u>Format</u>	<u>Parameters</u>
1	4D20.11	GAMMA, UDM, UTIME, UVELM
2	2D20.11	ME, MM
3	3D20.11	REVMAG, OINCD, ERRMXM
4	2D20.11	TDAY0, TTRIPD
5	3D20.11	VEVMAG, LOND, THED
6	4D20.11	REM0(1), REM0(2), REM0(3), VEM0(1)
7	2D20.11	VEM0(2), VEM0(3)
8	4D20.11	EPS, EPSTSI, KDX, EPSV
9	4I5	ICOMV, ITERMX, IFILEX, ITAR

The next 1 or 2 cards depend on ITAR.

ITAR = 0

10	3D20.11	AYM, AZM, ATARD
----	---------	-----------------

ITAR = 1

11	4D20.11	REVTAR(1), REVTAR(2), REVTAR(3), VEVATAR(1)
12	2D20.11	VEVTAR(2), VEVATAR(3)

The following 3 cards are needed only if ICOMV = 0.

13	4D20.11	V(1, 1), V(1, 2), V(1, 3), V(2, 1)
14	4D20.11	V(2, 2), V(2, 3), V(3, 1) V(3, 2)
15	4D20.11	V(3, 3)

**Program PTP3I**

<u>Card No.</u>	<u>Format</u>	<u>Parameters</u>
1	4D20.11	GLI, AUM, UTIME, UVELM
2	3D20.11	MS, ME, MM
3	3D20.11	TSTART, TM, TEND
4	4D20.11	RSE0(1), RSE0(2), RSE0(3), VSE0(1)
5	4D20.11	VSE0(2), VSE0(3), RSM0(1), RSM0(2)
6	4D20.11	RSM0(3), VSM0(1), VSM0(2), VSM0(3)
7	4D20.11	RSV0(1), RSV0(2), RSV0(3), VSV0(1)
8	2D20.11	VSV0(2), VSV0(3)
9	4D20.11	VSVI(1), VSVI(2), VSVI(3), VSVMP(1)
10	2D20.11	VSVMP(2), VSVMP(3)
11	4D20.11	RSVTAR(1), RSVTAR(2), RSVTAR(3), VSVTAR(1)
12	2D20.11	VSVTAR(2), VSVTAR(3)
13	3D20.11	KNR, ERRMIN, ERRMXM
14	3D20.11	FMINM, EPS, EPSV
15	515	ICOMV, ITLMAX, ILINC, ITDMAX, IFILEX

The following 4 cards are needed only if ICOMV = 0.

16	4D20.11	V(1, 1), V(1, 2), V(1, 3), V(1, 4)
17	4D20.11	V(2, 1), V(2, 2), V(2, 3), V(2, 4)
18	4D20.11	V(3, 1), V(3, 2), V(3, 3), V(3, 4)
19	4D20.11	V(4, 1), V(4, 2), V(4, 3), V(4, 4)

**Program PTP8|3**

<u>Card No.</u>	<u>Format</u>	<u>Parameters</u>
1	4D20.11	GAMMA, UDM, UTIME, UVELM
2	2D20.11	ME, MM
3	3D20.11	TSTART, TM, TEND
4	4D20.11	REM0(1), REM0(2), REM0(3), VEM0(1)
5	2D20.11	VEM0(2), VEM0(3)
6	4D20.11	REVO(1), REVO(2), REVO(3), VEV0(1)
7	2D20.11	VEV0(2), VEV0(3)
8	4D20.11	VEV0P(1), VEV0P(2), VEV0P(3), VEVMP(1)
9	2D20.11	VEVMP(2), VEVMP(3)
10	4D20.11	REVTAR(1), REVTAR(2), REVTAR(3), VEVTAR(1)
11	2D20.11	VEVTAR(2), VEVTAR(3)
12	3D20.11	KNR, ERRMIN, ERRMXM
13	3D20.11	FMINM, EPS, EPSV
14	515	ICOMV, ITLMAX, ILINC, ITDMAX, IFILEX

The following 4 cards are needed only if ICOMV = 0.

15	4D20.11	V(1, 1), V(1, 2), V(1, 3), V(1, 4)
16	4D20.11	V(2, 1), V(2, 2), V(2, 3), V(2, 4)
17	4D20.11	V(3, 1), V(3, 2), V(3, 3), V(3, 4)
18	4D20.11	V(4, 1), V(4, 2), V(4, 3), V(4, 4)

### PROGRAM PRINTOUT DESCRIPTION

<b>ALPHA</b>	Step size in search direction or Davidon algorithm parameter
<b>ALPHAC</b>	Step size in cubic interpolation
<b>ANGE</b>	Subtended angle at earth (deg)
<b>ANGM</b>	Subtended angle at moon (deg)
<b>ANGS</b>	Subtended angle at sun (deg)
<b>ANGV</b>	Subtended angle at spacecraft (deg)
<b>ATARD</b>	Parameter to define Halo orbit (deg)
<b>AUM</b>	1. Unit of distance in meters (4-body)
<b>AYM</b>	Parameter to define Halo orbit (meter)
<b>AZM</b>	Parameter to define Halo orbit (meter)
<b>BETA</b>	Davidon algorithm parameter
<b>DG</b>	Cost gradient difference
<b>DELX</b>	Change in independent variables
<b>DGC</b>	Cost gradient difference
<b>DRM</b>	Change in interior impulse position
<b>DUVI</b>	Primer vector derivative at initial time
<b>DUVMM</b>	Primer vector derivative before interior impulse
<b>DUVMP</b>	Primer vector derivative after interior impulse
<b>DV</b>	Cost
<b>DVI</b>	Impulse at initial time
<b>DVIMAG</b>	Magnitude of initial impulse
<b>DVM</b>	Interior impulse
<b>DVMMAG</b>	Magnitude of interior impulse

DVMPX	Change in interior impulse
DVF	Impulse at terminal time
DVF MAG	Magnitude of terminal impulse
DVF MPS	Cost of terminal impulse (MPS)
DVIMPS	Cost of initial impulse (MPS)
DVMPS	Total cost (MPS)
DVMMPS	Cost of interior impulse (MPS)
DX	Change in independent variables
DXC	Change in independent variables
EPS	Parameter to terminate Davidon iterations
EPSTSI	Allowable terminal constraint violation
EPSV	Factor to scale down variance matrix
ERR	Constraint violation in Lambert iteration
ERRMAX	Allowable single step position error
ERRMIN	Allowable Lambert constraint violation
ERRMXM	Allowable single step position error (meter)
F	Cost
FC	Cost in cubic interpolation.
FD	Cost
FG	Augmented cost
FGS	Augmented cost
FMINM	Estimated cost (MPS)
FS	Cost
G	Cost gradient

GAMMA	Parameter to define libration point (3-body)
GC	Cost gradient in cubic interpolation
GCMAG	Magnitude of cost gradient
GD	Cost radient
GG	Augmetned cost gradient
GGS	Augmented cost gradient
GL1	Parameter to define L1 libration point (4-body)
GMAG	Magnitude of cost gradient
GS	Cost gradient
GSMAG	Magnitude of cost gradient
H	Computed step size in state extrapolation
HDAY	Step size in days
ICOMV	Flag to compute variance matrix
IFILE	Flag to file trajectory data
IFILEX	Flag to file trajectory data
ILINC	Number of Lambert increments
IMODE	Flag to select mode of initial condition
IMTX	Flag to compute state transition matrix
IPTRJX	Flag to print trajectory
IPTRAJ	Flag to print trajectory
IPV	Flag to compute primer vector
IPVTM	Flag to monitor primer vector magnitude history
ISTEP	Number of integration steps
ITAR	Flag to compute target position and velocity on Halo orbit

<b>ITDMAX</b>	Maximum number of Davidon iterations
<b>ITER</b>	Number of iteration in Lambert routine
<b>ITERD</b>	Number of Davidon iterations
<b>ITERL</b>	Number of Lambert increment
<b>ITERMX</b>	Maximum of Davidon iterations
<b>ITLMAX</b>	Maximum number of Lambert iterations
<b>KDX</b>	Parameter to scale independent variables in constraint restoration
<b>KNR</b>	Parameter to scale independent variables in Lambert iteration.
<b>KV</b>	Parameter to scale variance matrix
<b>LDM</b>	Derivative of primer vector magnitude
<b>LDTM</b>	Derivative of maximum primer vector magnitude
<b>LOND</b>	Longitude of ascending node (deg)
<b>LM</b>	Magnitude of primer vector
<b>LT</b>	Constraint gradient matrix
<b>LTM</b>	Maximum primer vector magnitude
<b>ME</b>	Gravitational constant of earth
<b>MM</b>	Gravitational constant of moon
<b>MS</b>	Gravitational constant of sun
<b>OBLI</b>	Obliquity angle (deg)
<b>OINCD</b>	Orbital inclination (deg)
<b>P</b>	Davidon algorithm parameter (iteration stops if P is less than EPS in ETP2I or ETP2I3)
<b>PC</b>	Davidon algorithm parameter
<b>PV</b>	Primer vector and derivative
<b>PVO</b>	Primer vector and derivative at initial time

PVMMAG	Projection of primer vector derivative on primer vector before interior impulse
PVPMMAG	Projection of primer vector derivative on primer vector after interior impulse
R	Davidon algorithm parameters
RC	Davidon algorithm parameters in cubic interpolation
RCMAG	Magnitude of RC
RDED	Position of earth in rotating coordinates
RDLID	Position of L1 libration point in rotating coordinates
RDMID	Position of moon in rotating coordinates
RDSID	Position of sun in rotating coordinates
RDVD	Position of spacecraft in rotating coordinates
REL	Position of libration point wrt earth
REM	Position of moon wrt earth
REMO	Position of moon wrt earth at initial time
REMFI	Position of moon wrt earth at terminal time
REV	Position of spacecraft wrt earth
REVFI	Position of spacecraft wrt earth at terminal time
REVM	Position of spacecraft wrt earth at interior impulse time
REVMAG	Distance of spacecraft to earth
REVMX	Change of position of spacecraft wrt earth at interior impulse time
REVO	Position of spacecraft wrt earth at initial time
REVMD	Position of spacecraft wrt earth at interior impulse time
REVTAR	Target position wrt earth

RLTARL	Target position wrt libration point
RMAG	Magnitude of R
RMV	Position of spacecraft wrt moon
RMVF	Position of spacecraft wrt moon at terminal time
RMVMAG	Distance of spacecraft to moon
RSE	Position of earth wrt sun
RSEO	Position of earth wrt sun at initial time
RSEF	Position of earth wrt sun at terminal time
RSL1	Position of L1 libration point wrt sun
RSM	Position of moon wrt sun
RSMO	Position of moon wrt sun at initial time
RSMF	Position of moon wrt sun at terminal time
RSV	Position of spacecraft wrt sun
RSVO	Position of spacecraft wrt sun at initial time
RSVF	Position of spacecraft wrt sun at terminal time
RSVM	Position of spacecraft wrt sun at interior impulse time
RSVMAG	Distance of spacecraft to sun
RSVMID	Position of moon wrt sun at interior impulse time
RSVMX	Spacecraft position wrt sun at interior impulse
RSVTAR	Target position wrt sun
RTM	Position of spacecraft at maximum primer vector magnitude
S	Davidon algorithm search direction
SG	Projection of cost gradient on search direction
SGS	Projection of cost gradient on search direction

T	Time
TO	Initial time
TDAY	Time in day
TDAYO	Initial time in day
TDAYF	Terminal time in day
TEND	Terminal time
TESTR	Magnitude of constraint violation
TESTRD	Magnitude of constraint violation
TESTRS	Magnitude of constraint violation
TF	Terminal time
THED	Position of spacecraft from line of node (deg)
TM	Interior impulse time
TRIPD	Trip time in day
TSI	Constraint violation
TSID	Constraint violation
TSIS	Constraint violation
TSTART	Initial time
TTM	Time of maximum primer vector magnitude
TTRIP	Trip time
TTRIPD	Trip time in day
UDM	1 Unit of distance in meters (3-body)
UTIME	1 Unit of time in days
UVELM	1 MPS in dimensionless velocity
UVF	Unit vector of terminal impulse

UVI	Unit vector of initial impulse
UVM	Unit vector of interior impulse
V	Variance matrix
VDED	Velocity of earth in rotating coordinates
VDLID	Velocity of L1 libration point in rotating coordinates
VDMD	Velocity of moon in rotating coordinates
VDSD	Velocity of sun in rotating coordinates
VDVD	Velocity of spacecraft in rotating coordinates
VEL	Velocity of libration point wrt earth
VEM	Velocity of moon wrt earth
VEMO	Velocity of moon wrt earth at initial time
VEMF	Velocity of moon wrt earth at terminal time
VEV	Velocity of spacecraft wrt earth
VEVO	Velocity of spacecraft wrt earth at initial time before impulse
VEVOP	Velocity of spacecraft wrt earth after initial impulse
VEVMP	Velocity of spacecraft wrt earth after interior impulse
VEVMPX	Spacecraft velocity wrt earth after interior impulse
VEVF	Velocity of spacecraft wrt earth at terminal time
VEVMAG	Magnitude of spacecraft velocity wrt earth
VEVMPD	Velocity of spacecraft wrt earth after interior impulse
VEVMPS	Magnitude of spacecraft velocity wrt earth in MPS
VEVTAR	Target velocity wrt earth
VIT	Initial velocity in Lambert iteration
VLTARL	Velocity of target wrt libration point

VMV	Velocity of spacecraft wrt moon
VMVF	Velocity of spacecraft wrt moon at terminal time
VSE	Velocity of earth wrt sun
VSEO	Velocity of earth wrt sun at initial time
VSEF	Velocity of earth wrt sun at terminal time
VSL1	Velocity of L1 libration point wrt sun
VSM	Velocity of moon wrt sun
VSMO	Velocity of moon wrt sun at initial time
VSMF	Velocity of moon wrt sun at terminal time
VSV	Velocity of spacecraft wrt sun
VSVI	Velocity of spacecraft wrt sun after initial impulse
VSVMPX	Spacecraft velocity wrt sun after interior impulse
VSVF	Velocity of spacecraft wrt sun at terminal time
VSVMP	Velocity of spacecraft wrt sun after interior impulse
VSVMPD	Velocity of spacecraft wrt sun after interior impulse
VSVO	Velocity of spacecraft wrt sun at initial time before impulse
VSVTAR	Target velocity wrt sun
V'IM	Velocity of spacecraft at maximum primer vector magnitude
X	Independent variables in Davidon iterations
XC	Independent variables in cubic interpolation.
XD	Independent variables
XS	Independent variables

### Subroutine FOURBY

#### A. Input Parameters

<u>Parameter</u>	<u>Symbol</u>	<u>Definition</u>
XTO	$t_o$	
XTF	$t_f$	
RSVO	$\bar{R}_{SV}(t_o)$	
VSV0	$\bar{V}_{SV}(t_o)$	
RSE0	$\bar{R}_{SE}(t_o)$	
VSE0	$\bar{V}_{SE}(t_o)$	
RSM0	$\bar{R}_{SM}(t_o)$	
VSM0	$\bar{V}_{SM}(t_o)$	
PVO	$\lambda(t_o), \dot{\lambda}(t_o)$	Primer vector and derivative

#### B. Output Parameters

RSVD	$\bar{R}_{SV}(t_f)$	
VSVD	$\bar{V}_{SV}(t_f)$	
RSED	$\bar{R}_{SE}(t_f)$	
VSED	$\bar{V}_{SE}(t_f)$	
RSMD	$\bar{R}_{SM}(t_f)$	
VSMD	$\bar{V}_{SM}(t_f)$	
S11, S12, S21, S22	$\varphi(t_f, t_o)$	State transition matrix

#### C. Computation

- Step 1. Initialize running variables equal to input states.
- Step 2. Call RVEMV to compute  $\bar{R}_{EV}, \bar{V}_{EV}, \bar{R}_{MV}, \bar{V}_{MV}, \bar{R}_{EM}, \bar{V}_{EM}$ .
- Step 3. Call CSTEP to compute step size  $h$ ,  $\epsilon_{RSV}^{***}, \epsilon_{RSE}^{***}, \epsilon_{RSM}^{***}$  and  $J$ .

Step 4. Call DISP

Step 5. If IPV = 1, call PVEC.  
If IFILE = 1, call FDATA.  
If IPTRAJ = 1, call PTRAJ.

Step 6. Call TWOBDY to compute 6 conics:

$$[\bar{R}_{SV}, \bar{V}_{SV}]$$

$$[\bar{R}_{SE}, \bar{V}_{SE}]$$

$$[\bar{R}_{SM}, \bar{V}_{SM}]$$

$$[\bar{R}_{EV}, \bar{V}_{EV}]$$

$$[\bar{R}_{MV}, \bar{V}_{MV}]$$

$$[\bar{R}_{EM}, \bar{V}_{EM}]$$

Step 7. Compute 3 perturbation vectors. Let  
 $[\bar{R}_{i,j}]$  = CONIC of j with respect to i

$\bar{R}_{i,j}$  = reference trajectory of j with respect to i.

$$d\bar{R}_{SV} = [\bar{R}_{SV}] - \bar{R}_{SV}(0) - h \bar{V}_{SV}(0)$$

$$d\bar{V}_{SV} = [\bar{V}_{SV}] - \bar{V}_{SV}(0)$$

$$d\bar{R}_{SE} = [\bar{R}_{SE}] - \bar{R}_{SE}(0) - h \bar{V}_{SE}(0)$$

$$d\bar{V}_{SE} = [\bar{V}_{SE}] - \bar{V}_{SE}(0)$$

$$d\bar{R}_{SM} = [\bar{R}_{SM}] - \bar{R}_{SM}(0) - h \bar{V}_{SM}(0)$$

$$d\bar{V}_{SM} = [\bar{V}_{SM}] - \bar{V}_{SM}(0)$$

$$d\bar{R}_{EV} = [\bar{R}_{EV}] - \bar{R}_{EV}(0) - h \bar{V}_{EV}(0)$$

$$d\bar{V}_{EV} = [\bar{V}_{EV}] - \bar{V}_{EV}(0)$$

$$d\bar{R}_{MV} = [\bar{R}_{MV}] - \bar{R}_{MV}(0) - h \bar{V}_{MV}(0)$$

$$d\bar{V}_{MV} = [\bar{V}_{MV}] - \bar{V}_{MV}(0)$$

$$d\bar{R}_{EM} = [\bar{R}_{EM}] - \bar{R}_{EM}(0) - h \bar{V}_{EM}(0)$$

$$d\bar{V}_{EM} = [\bar{V}_{EM}] - \bar{V}_{EM}(0)$$

Approximate perturbations

$$\bar{P}_{RSV} = \frac{\mu_E}{\mu_S + \mu_E} d\bar{R}_{SE} + d\bar{R}_{EV} + \frac{\mu_M}{\mu_S + \mu_M} d\bar{R}_{SM} + d\bar{R}_{MV}$$

$$\bar{P}_{VSV} = \frac{\mu_E}{\mu_S + \mu_E} d\bar{V}_{SE} + d\bar{V}_{EV} + \frac{\mu_M}{\mu_S + \mu_M} d\bar{V}_{SM} + d\bar{V}_{MV}$$

$$\bar{P}_{RSE} = \frac{\mu_M}{\mu_S + \mu_M} d\bar{R}_{SM} - \frac{\mu_M}{\mu_E + \mu_M} d\bar{R}_{EM}$$

$$\bar{P}_{VSE} = \frac{\mu_M}{\mu_S + \mu_M} d\bar{V}_{SM} - \frac{\mu_M}{\mu_E + \mu_M} d\bar{V}_{EM}$$

$$\bar{P}_{RSM} = \frac{\mu_E}{\mu_S + \mu_E} d\bar{R}_{SE} + \frac{\mu_E}{\mu_E + \mu_M} d\bar{R}_{EM}$$

$$\bar{P}_{VSM} = \frac{\mu_E}{\mu_S + \mu_E} d\bar{V}_{SE} + \frac{\mu_E}{\mu_E + \mu_M} d\bar{V}_{EM}$$

Step 8. Compute reference trajectories

$$\bar{R}_{SV} = [\bar{R}_{SV}] + \bar{P}_{RSV}$$

$$\bar{V}_{SV} = [\bar{V}_{SV}] + \bar{P}_{VSV}$$

$$\bar{R}_{SE} = [\bar{R}_{SE}] + \bar{P}_{RSE}$$

$$\bar{V}_{SE} = [\bar{V}_{SE}] + \bar{P}_{VSE}$$

$$\bar{R}_{SM} = [\bar{R}_{SM}] + \bar{P}_{RSM}$$

$$\bar{V}_{SM} = [\bar{V}_{SM}] + \bar{P}_{VSM}$$

$$\bar{R}_{EV} = -\bar{R}_{SE} + \bar{R}_{SV}$$

$$\bar{V}_{EV} = -\bar{V}_{SE} + \bar{V}_{SV}$$

$$\bar{R}_{MV} = -\bar{R}_{SM} + \bar{R}_{SV}$$

$$\bar{V}_{MV} = -\bar{V}_{SM} + \bar{V}_{SV}$$

$$\bar{R}_{EM} = -\bar{R}_{SE} + \bar{R}_{SM}$$

$$\bar{V}_{EM} = -\bar{V}_{SE} + \bar{V}_{SM}$$

$$t = t + h$$

Step 9. Call DELRV to compute corrections.

Step 10. Correct state vectors.

Step 11. If IMTX = 1, update state transition matrix.

Step 12. Call DISP

Step 13. If IPV = 1, call PVEC.  
If IFILE = 1, call FDATA.  
If IPTRAJ = 1, call PTRAJ

Step 14. If  $t \geq t_f$ , exit.

Step 15. Call CSTEP.  
Go to Step 6.

### Subroutine THRBDY

#### A. Input Parameters

<u>Parameters</u>	<u>Symbol</u>	<u>Definition</u>
XTO	$t_o$	
XTF	$t_f$	
REVO	$\bar{R}_{EV}(t_o)$	
VEVO	$\bar{V}_{EV}(t_o)$	
REMO	$\bar{R}_{EM}(t_o)$	
VEMO	$\bar{V}_{EM}(t_o)$	
PVO	$\lambda, \dot{\lambda}$	

#### B. Output Parameters

REVD	$\bar{R}_{EV}(t_f)$	
VEVD	$\bar{V}_{EV}(t_f)$	
REMD	$\bar{R}_{EM}(t_f)$	
VEMD	$\bar{V}_{EM}(t_f)$	
S11, S12, S21, S22	$\phi(t_f, t_o)$	State transition matrix

#### C. Computation

- Step 1. Initialize running variables equal to input states.
- Step 2. Call CSTEP3 to compute step size  $h$ ,  $\epsilon_{REV}$  and  $J$ .
- Step 3. Call DISP3
- Step 4. If IPV = 1, call PVEC  
If IFILE = 1, call FDATA3  
If IPTRAJ = 1, call PTRAJ3.
- Step 5. Call TWOBDY to compute 3 conics:

$$[\bar{R}_{EV}, \bar{V}_{EV}]$$

$$[\bar{R}_{EM}, \bar{V}_{EM}]$$

$$[\bar{R}_{MV}, \bar{V}_{MV}]$$

**Step 6.** Compute perturbation vector

$$\bar{P}_{REV} = [\bar{R}_{MV}] - \bar{R}_{MV}(0) - h \bar{V}_{MV}(0)$$

$$\bar{P}_{VEV} = [\bar{V}_{MV}] - \bar{V}_{MV}(0)$$

**Step 7.** Compute reference trajectories

$$\bar{R}_{EV} = [\bar{R}_{EV}] + \bar{P}_{REV}$$

$$\bar{V}_{EV} = [\bar{V}_{EV}] + \bar{P}_{VEV}$$

$$\bar{R}_{EM} = [\bar{R}_{EM}]$$

$$\bar{V}_{EM} = [\bar{V}_{EM}]$$

$$\bar{R}_{MV} = -\bar{R}_{EM} + \bar{R}_{EV}$$

$$\bar{V}_{MV} = -\bar{V}_{EM} + \bar{V}_{EV}$$

$$t = t + h$$

**Step 8.** Call DELRV3 to compute corrections.

**Step 9.** Correct state vectors.

**Step 10.** If IMTX = 1, update state transition matrix.

**Step 11.** Call DISP3

- Step 12. If IPV = 1, call PVEC.  
If IFILE = 1, call FDATA3.  
If IPTRAJ = 1, call PTRAJ3.
- Step 13. If  $t \geq t_f$ , exit.
- Step 14. Call CSTEP3.  
Go to Step 5.

### Subroutine TWOBODY

#### A. Input Parameters

<u>Parameters</u>	<u>Symbol</u>	<u>Definition</u>
XRO	$\bar{R}(t)$	
XVO	$\bar{V}(t)$	
TAU	$h$	Step size
MU	$\mu$	Gravitational constant
PSI	$\psi$	Generalized eccentric anomaly
IMTX	$I_{MTX}$	Flag to compute state transition matrix: $I_{MTX} = 0$ , no 1, yes

#### B. Output Parameters

XRF	$\bar{R}(t+h)$	
VRF	$\bar{V}(t+h)$	
PSI	$\psi$	
P	$\phi(t+h; t)$	State transition matrix

#### C. Computation

See Ref. (3).

### Subroutine CSTEP

#### A. Input Parameters

<u>Parameters</u>	<u>Symbol</u>	<u>Definition</u>
ERRMAX	$\epsilon_{\max}$	Allowable single step position error
REV	$\bar{R}_{EV}(t)$	
RSE	$\bar{R}_{SE}(t)$	
RSV	$\bar{R}_{SV}(t)$	
RMV	$\bar{R}_{MV}(t)$	
RSM	$\bar{R}_{SM}(t)$	
REM	$\bar{R}_{EM}(t)$	
TGO	tgo	$t_f - t$

#### B. Output Parameters

H	h	Step size
DR4RSV	$\overline{\epsilon}_{RSV}^{(4)}(t)$	
DR4RSE	$\overline{\epsilon}_{RSE}^{(4)}(t)$	
DR4RSM	$\overline{\epsilon}_{RSM}^{(4)}(t)$	
BIGJ	J	$J = \begin{pmatrix} I_3 & hI_3 \\ O_3 & I_3 \end{pmatrix}$

#### C. Computation

$$\begin{aligned}
\overline{\epsilon}_{RSV}(t) = & \mu_S \mu_E \left[ \frac{1}{R_{SV}} \left( I - 3 \bar{u}_{SV} \bar{u}_{SV}^T \right) \left( \frac{\bar{R}_{EV}}{R_{EV}} + \frac{\bar{R}_{SE}}{R_{SE}} \right) \right. \\
& + \frac{1}{R_{EV}} \left( I - 3 \bar{u}_{EV} \bar{u}_{EV}^T \right) \left( \frac{\bar{R}_{SV}}{R_{SV}} - \frac{\bar{R}_{SE}}{R_{SE}} \right) \left. \right] \\
& + \mu_S \mu_M \left[ \frac{1}{R_{SV}} \left( I - 3 \bar{u}_{SV} \bar{u}_{SV}^T \right) \left( \frac{\bar{R}_{MV}}{R_{MV}} + \frac{\bar{R}_{SM}}{R_{SM}} \right) \right. \\
& + \frac{1}{R_{MV}} \left( I - 3 \bar{u}_{MV} \bar{u}_{MV}^T \right) \left( \frac{\bar{R}_{SV}}{R_{SV}} - \frac{\bar{R}_{SM}}{R_{SM}} \right) \left. \right] \\
& + \mu_E \mu_M \left[ \frac{1}{R_{EV}} \left( I - 3 \bar{u}_{EV} \bar{u}_{EV}^T \right) \left( \frac{\bar{R}_{MV}}{R_{MV}} + \frac{\bar{R}_{EM}}{R_{EM}} \right) \right. \\
& - \frac{1}{R_{SE}} \left( I - 3 \bar{u}_{SE} \bar{u}_{SE}^T \right) \left( \frac{\bar{R}_{EM}}{R_{EM}} - \frac{\bar{R}_{SM}}{R_{SM}} \right) \left. \right] \\
& + \frac{1}{R_{MV}} \left( I - 3 \bar{u}_{MV} \bar{u}_{MV}^T \right) \left( \frac{\bar{R}_{EV}}{R_{EV}} - \frac{\bar{R}_{EM}}{R_{EM}} \right) \\
& \left. + \frac{1}{R_{SM}} \left( I - 3 \bar{u}_{SM} \bar{u}_{SM}^T \right) \left( \frac{\bar{R}_{EM}}{R_{EM}} + \frac{\bar{R}_{SE}}{R_{SE}} \right) \right]
\end{aligned}$$

$$h = \left( 24 \frac{\epsilon_{\max}}{\overline{\epsilon}_{RSV}} \right)^{1/4}$$

$$\bar{u}_{SV} = \text{UNIT}(\bar{R}_{SV})$$

$$\bar{u}_{EV} = \text{UNIT}(\bar{R}_{EV})$$

$$\bar{u}_{MV} = \text{UNIT}(\bar{R}_{MV})$$

$$\bar{u}_{SE} = \text{UNIT}(\bar{R}_{SE})$$

$$\bar{u}_{SM} = \text{UNIT}(\bar{R}_{SM})$$

$$\begin{aligned}
\frac{\epsilon_{RSE}^{...}(t)}{RSE} &= - \frac{(\mu_S + \mu_E)}{R_{SE}} \mu_M (I - 3 \bar{u}_{SE} \bar{u}_{SE}^T) \left( \frac{\bar{R}_{EM}}{R_{EM}} - \frac{\bar{R}_{SM}}{R_{SM}} \right) \\
&\quad - \frac{\mu_M \mu_S}{R_{EM}} (I - 3 \bar{u}_{EM} \bar{u}_{EM}^T) \left( \frac{\bar{R}_{SM}}{R_{SM}} - \frac{\bar{R}_{SE}}{R_{SE}} \right) \\
&\quad + \frac{\mu_M \mu_E}{R_{SM}} (I - 3 \bar{u}_{SM} \bar{u}_{SM}^T) \left( \frac{\bar{R}_{EM}}{R_{EM}} + \frac{\bar{R}_{SE}}{R_{SE}} \right) \\
\frac{\epsilon_{RSM}^{...}(t)}{RSM} &= \frac{(\mu_S + \mu_M)}{R_{SM}} \mu_E (I - 3 \bar{u}_{SM} \bar{u}_{SM}^T) \left( \frac{\bar{R}_{EM}}{R_{EM}} + \frac{\bar{R}_{SE}}{R_{SE}} \right) \\
&\quad + \frac{\mu_E \mu_S}{R_{EM}} (I - 3 \bar{u}_{EM} \bar{u}_{EM}^T) \left( \frac{\bar{R}_{SM}}{R_{SM}} - \frac{\bar{R}_{SE}}{R_{SE}} \right) \\
&\quad - \frac{\mu_E \mu_M}{R_{SE}} (I - 3 \bar{u}_{SE} \bar{u}_{SE}^T) \left( \frac{\bar{R}_{EM}}{R_{EM}} - \frac{\bar{R}_{SM}}{R_{SM}} \right)
\end{aligned}$$

All quantities are evaluated at the beginning of an integration step. If  $h$  is greater than  $tgo$ , it is set to  $tgo$  for the last step.

Subroutine CSTEP3

**A. Input Parameters**

<u>Parameters</u>	<u>Symbols</u>	<u>Definition</u>
ERRMAX	$\epsilon_{\max}$	Allowable single step position error
REV	$\bar{R}_{EV}(t)$	
RMV	$\bar{R}_{MV}(t)$	
TGO	tgo	Terminal time - present time

**B. Output Parameters**

H	h	Step size
DR4REV	$\ddot{\epsilon}_{REV}(t)$	4th Derivative of position error estimate
BIGJ	J	$J = \begin{pmatrix} I_3 & hI_3 \\ O_3 & I_3 \end{pmatrix}$

**C. Computation**

$$\begin{aligned} \ddot{\epsilon}_{REV}(t) &= \mu_E \mu_M \left\{ \frac{1}{R_{EV}^3} (I - 3 \bar{u}_{EV} \bar{u}_{EV}^T) \left( \frac{\bar{R}_{MV}}{R_{MV}^3} + \frac{\bar{R}_{EM}}{R_{EM}^3} \right) \right. \\ &\quad \left. + \frac{1}{R_{MV}^3} (I - 3 \bar{u}_{MV} \bar{u}_{MV}^T) \left( \frac{\bar{R}_{EV}}{R_{EV}^3} - \frac{\bar{R}_{EM}}{R_{EM}^3} \right) \right\} \end{aligned}$$

$$\ddot{\epsilon}_{REM}(t) = 0$$

$$h = \left( 24 \frac{\epsilon_{\max}}{\ddot{\epsilon}_{REV}} \right)^{1/4}$$

$$\bar{u}_{EV} = \text{UNIT}(\bar{R}_{EV})$$

$$\bar{u}_{MV} = \text{UNIT}(\bar{R}_{MV})$$

All quantities are evaluated at the beginning of an integration step. If h is greater than tgo, it is set to tgo for the last step.

Subroutine DELRV

**A. Input Parameters**

<u>Parameters</u>	<u>Symbol</u>	<u>Definition</u>
H	h	Step size
RSV	$\bar{R}_{SV}(t+h)$	
REV	$\bar{R}_{EV}(t+h)$	
RMV	$\bar{R}_{MV}(t+h)$	
RSE	$\bar{R}_{SE}(t+h)$	Conics plus perturbations at end of step.
RSM	$\bar{R}_{SM}(t+h)$	
REM	$\bar{R}_{EM}(t+h)$	
CRSV	$[\bar{R}_{SV}(t+h)]$	
CREV	$[\bar{R}_{EV}(t+h)]$	
CRMV	$[\bar{R}_{MV}(t+h)]$	
CRSE	$[\bar{R}_{SE}(t+h)]$	Conics at end of step
CRSM	$[\bar{R}_{SM}(t+h)]$	
CREM	$[\bar{R}_{EM}(t+h)]$	
DR4RSV	$\overline{\epsilon}_{RSV}(t)$	
DR4RSE	$\overline{\epsilon}_{RSE}(t)$	
DR4RSM	$\overline{\epsilon}_{RSM}(t)$	4th derivative of position error estimates at beginning of step.

**B. Output Parameters**

RRSV	$d\bar{R}_{SV}(t+h)$	
RVSV	$d\bar{V}_{SV}(t+h)$	
RRSE	$d\bar{R}_{SE}(t+h)$	
RVSE	$d\bar{V}_{SE}(t+h)$	Position and velocity corrections computed by quadrature formula.
RRSM	$d\bar{R}_{SM}(t+h)$	
RVSM	$d\bar{V}_{SM}(t+h)$	

C. Computation

Define

$$\bar{s}_{i,j} = \frac{[\bar{R}_{i,j}(t+h)] - [\bar{R}_{i,j}]}{|[\bar{R}_{i,j}(t+h)]| - |\bar{R}_{i,j}|}$$

$$(i, j) = (SV, EV, MV, SE, SM, EM)$$

The second derivatives of Stumpff-Weiss position errors are given by

$$\ddot{\epsilon}_{1, RSV} = \mu_S \mu_M \bar{s}_{SV} + \mu_E (\bar{s}_{SE} + \bar{s}_{EV}) + \mu_M (\bar{s}_{SM} + \bar{s}_{MV})$$

$$\ddot{\epsilon}_{1, RSE} = (\mu_S + \mu_E) \bar{s}_{SE} + \mu_M (\bar{s}_{SM} - \bar{s}_{EM})$$

$$\ddot{\epsilon}_{1, RSM} = (\mu_S + \mu_M) \bar{s}_{SM} + \mu_E (\bar{s}_{SE} + \bar{s}_{EM})$$

The position and velocity corrections are computed by quadrature formulas below.

$$d\bar{R}_{SV} = \frac{h^2}{20} (\dot{\epsilon}_{RSV} \frac{h^2}{3} + \ddot{\epsilon}_{1, RSV})$$

$$dV_{SV} = \frac{h}{4} (\dot{\epsilon}_{RSV} \frac{h^2}{6} + \ddot{\epsilon}_{1, RSV})$$

$$d\bar{R}_{SE} = \frac{h^2}{20} (\dot{\epsilon}_{RSE} \frac{h^2}{3} + \ddot{\epsilon}_{1, RSE})$$

$$dV_{SE} = \frac{h}{4} (\dot{\epsilon}_{RSE} \frac{h^2}{6} + \ddot{\epsilon}_{1, RSE})$$

$$d\bar{R}_{SM} = \frac{h^2}{20} (\dot{\epsilon}_{RSM} \frac{h^2}{3} + \ddot{\epsilon}_{1, RSM})$$

$$dV_{SM} = \frac{h}{4} (\dot{\epsilon}_{RSM} \frac{h^2}{6} + \ddot{\epsilon}_{1, RSM})$$

### Subroutine DELRV3

#### A. Input Parameters

<u>Parameters</u>	<u>Symbol</u>	<u>Definition</u>
H	h	Step size
REV	$\bar{R}_{EV}(t+h)$	Conics plus perturbations at end of step.
RMV	$\bar{R}_{MV}(t+h)$	
CREV	$\left[ \begin{array}{c} \bar{R}_{EV}(t+h) \\ \bar{R}_{MV}(t+h) \end{array} \right]$	Conics at end of step.
CRMV	$\left[ \begin{array}{c} \bar{R}_{EV}(t+h) \\ \bar{R}_{MV}(t+h) \end{array} \right]$	
DR4REV	$\ddot{\epsilon}_{REV}(t)$	4th derivative of position error estimate at beginning of step

#### B. Output Parameters

RREV	$d\bar{R}_{EV}(t+h)$	Position and velocity corrections computed by quadrature formula
RVEV	$d\bar{V}_{EV}(t+h)$	

#### C. Computation

Define

$$\bar{s}_{i, j} = \frac{\left[ \bar{R}_{i, j}(t+h) \right]}{\left| \bar{R}_{i, j}(t+h) \right|}$$

$$(i, j) = (EV, MV)$$

The second derivative of Stumpff-Weiss position errors is given by

$$\ddot{\epsilon}_{1, REV} = \mu_E \bar{s}_{EV} + \mu_M \bar{s}_{MV}$$

The position and velocity corrections by quadrature formula are

$$d\bar{R}_{EV} = \frac{h^2}{20} \left( \ddot{\epsilon}_{REV} \frac{h^2}{3} + \dot{\epsilon}_{1, REV} \right)$$

$$d\bar{V}_{EV} = \frac{h}{4} \left( \ddot{\epsilon}_{REV} \frac{h^2}{8} + \dot{\epsilon}_{1, REV} \right)$$

Note that there is no error in moon's position and velocity in a 3-body space.

Subroutine COMIC

**A. Input Parameters**

Parameters	Symbol	Definition
REVMAG	$r_o$	$ \bar{r}_{EV}(t_o) $
VEMAG	$v_o$	$ \bar{v}_{EV}^+(t_o) $
LON	$\Omega$ (rad)	Longitude of ascending node
THE	$\theta$ (rad)	Position of vehicle from ascending line of node in orbital plane.
OINC	$i$ (rad)	Orbital inclination
OBL	OBL (rad)	Obliquity angles
RSE0	$\bar{r}_{SE}(t_o)$	
VSE0	$\bar{v}_{SE}(t_o)$	

**B. Output Parameters**

REVO	$\bar{r}_{EV}(t_o)$
VEVO	$\bar{v}_{EV}^-(t_o)$
RSV0	$\bar{r}_{SV}(t_o)$
VSV0	$\bar{v}_{SV}^-(t_o)$
VSVI	$\bar{v}_{SV}^+(t_o)$
	Velocity before impulse
	Velocity after impulse

**C. Computation**

Matrix to transform a vector from O-frame to e-frame:

$$C_O^e = \begin{pmatrix} \cos \Omega & -\sin \Omega & 0 \\ \sin \Omega & \cos \Omega & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos i & -\sin i \\ 0 & \sin i & \cos i \end{pmatrix} \begin{pmatrix} \cos \theta & -\sin \theta & 0 \\ \sin \theta & \cos \theta & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

Matrix to transform a vector from e-frame to E-frame:

$$C_e^E = \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos(\text{OBL}) & \sin(\text{OBL}) \\ 0 & -\sin(\text{OBL}) & \cos(\text{OBL}) \end{pmatrix}$$

$$\bar{r}_{EV}(t_o) = C_e^E C_O^e \begin{pmatrix} r_o \\ 0 \\ 0 \end{pmatrix}$$

$$\bar{v}_{EV}^+(t_o) = C_e^E C_O^e \begin{pmatrix} 0 \\ v_o \\ 0 \end{pmatrix}$$

$$\bar{r}_{SV}(t_o) = \bar{r}_{SE}(t_o) + \bar{r}_{EV}(t_o)$$

$$\bar{v}_{SV}^+(t_o) = \bar{v}_{SE}(t_o) + \bar{v}_{EV}^+(t_o)$$

$$\bar{v}_{EV}^-(t_o) = \text{UNIT}(\bar{v}_{EV}^+(t_o)) \sqrt{\frac{\mu_E}{r_o}}$$

$$\bar{v}_{SV}^-(t_o) = \bar{v}_{SE}(t_o) + \bar{v}_{EV}^-(t_o)$$

### Subroutine COMIC3

#### A. Input Parameters

<u>Parameter</u>	<u>Symbol</u>	<u>Definition</u>
REVMAG	$r_o$	$ \bar{R}_{EV}(t_o) $
VEVMAG	$v_o$	$ \bar{v}_{EV}^+(t_o) $
LON	$\Omega$ (rad)	Longitude of ascending node
THE	$\theta$ (rad)	Position of vehicle from ascending node in orbital plane
OINC	$i$ (rad)	Orbital inclination

#### B. Output Parameters

REVO	$\bar{R}_{EV}(t_o)$
VEVO	$\bar{v}_{EV}^-(t_o)$
VEVOP	$\bar{v}_{EV}^+(t_o)$

#### C. Computation

$C_O^e$  = matrix to transform a vector from O-frame to e-frame  
 (given in COMIC)

$$\bar{R}_{EV}(t_o) = C_O^e \begin{pmatrix} r_o \\ 0 \\ 0 \end{pmatrix}$$

$$\bar{v}_{EV}^-(t_o) = C_O^e \begin{pmatrix} 0 \\ v_o \\ 0 \end{pmatrix}$$

$$\bar{v}_{EV}^+(t_o) = \text{UNIT}(\bar{v}_{EV}^-(t_o)) \sqrt{\frac{\mu_E}{r_o}}$$

Subroutine COMFG

A. Input Parameters

<u>Parameters</u>	<u>Symbol</u>	<u>Definition</u>
TSTART	$t_o$	
TEND	$t_f$	
REVMAG	$r_o$	$ \bar{R}_{EV}(t_o) $
VEVMAG	$v_o$	$ \bar{V}_{EV}^+(t_o) $
LON	$\Omega$ (rad)	Longitude of ascending node
THE	$\theta$ (rad)	Position of vehicle from ascending node in orbital plane
OINC	$i$ (rad)	Orbital inclination
OBL	OBL (rad)	Obliquity angle
RSE0	$\bar{R}_{SE}(t_o)$	
VSE0	$\bar{V}_{SE}(t_o)$	
RSM0	$\bar{R}_{SM}(t_o)$	
VSM0	$\bar{V}_{SM}(t_o)$	

B. Output Parameters

FD	$\Delta V$	$\Delta V =  \bar{V}_{SVTAR} - v_{SV}(t_f) $
TESTRD	$\epsilon$	$\epsilon =  \bar{\psi} $
GD	$\bar{g}$	$\bar{g} = \frac{\partial \Delta V}{\partial (v_o, \Omega, \theta)}$
TSID	$\bar{\psi}$	$\bar{\psi} = \bar{R}_{SV}(t_f) - \bar{R}_{SVTAR}$
LTD	$L^T$	$L^T = \frac{\partial \bar{\psi}}{\partial (v_o, \Omega, \theta)}$
S11, S12, S21, S22	$\varphi(t_f, t_o)$	$\varphi = \frac{\partial (\bar{R}_{SV}(t_f), \bar{V}_{SV}(t_f))}{\partial (\bar{R}_{SV}(t_o), \bar{V}_{SV}(t_o))}$
UVI	$\bar{u}_{VI}$	$\bar{u}_{VI} = \text{UNIT}(\bar{V}_{SV}^+(t_o) - \bar{V}_{SV}^-(t_o))$

UVF

UVF

$$\bar{u}_{VF} = \text{UNIT} (\bar{v}_{SVTAR} - \bar{v}_{SV}(t_f))$$

### C. Computation

$$\bar{x} = (v_o, \Omega, \theta)$$

Call COMIC to compute  $\bar{R}_{SV}(t_o)$ ,  $\bar{v}_{SV}^-(t_o)$ ,  $\bar{v}_{SV}^+(t_o)$ .

Call FOURBY to advance states to  $t_f$  and compute  $\varphi$ .

For the first iteration, call CTAR to compute  $\bar{R}_{SVTAR}$ ,  $\bar{v}_{SVTAR}$ .

$$\Delta \bar{v}_o = \bar{v}_{SV}^+(t_o) - \bar{v}_{SV}^-(t_o)$$

$$u_{VI} = \text{UNIT} (\Delta \bar{v}_o)$$

$$\Delta \bar{v}_f = \bar{v}_{SVTAR} - \bar{v}_{SV}(t_f)$$

$$u_{VF} = \text{UNIT} (\Delta \bar{v}_f)$$

$$\Delta v = |\Delta \bar{v}_f|$$

$$\bar{g} = \frac{\partial \Delta v}{\partial \bar{x}} = - \frac{\Delta \bar{v}_f^T}{\Delta v} \left( \varphi_{21} \frac{\partial \bar{R}_{SV}(t_o)}{\partial \bar{x}} + \varphi_{22} \frac{\partial \bar{v}_{SV}(t_o)}{\partial \bar{x}} \right)$$

$$\bar{\psi} = \bar{R}_{SV}(t_f) - \bar{R}_{SVTAR}$$

$$L^T = \frac{\partial \bar{\psi}}{\partial \bar{x}} = \varphi_{11} \frac{\partial \bar{R}_{SV}(t_o)}{\partial \bar{x}} + \varphi_{12} \frac{\partial \bar{v}_{SV}(t_o)}{\partial \bar{x}}$$

$$\bar{R}_{SV}(t_o) = \bar{R}_{SE}(t_o) + \bar{R}_{EV}(t_o)$$

$$\bar{v}_{SV}(t_o) = \bar{v}_{SE}(t_o) + \bar{v}_{EV}^+(t_o)$$

$$\frac{\partial \bar{R}_{SV}(t_o)}{\partial \bar{x}} = \frac{\partial \bar{R}_{EV}(t_o)}{\partial \bar{x}} = A$$

$$A(1, 1) = 0$$

$$A(1, 2) = r_o (-\sin \Omega \cos \theta - \cos \Omega \cos i \sin \theta)$$

$$A(1, 3) = r_o (-\cos \Omega \sin \theta - \sin \Omega \cos i \cos \theta)$$

$$A(2, 1) = 0$$

$$A(2, 2) = r_o \cos (\text{OBL}) (\cos \Omega \cos \theta - \sin \Omega \cos i \sin \theta)$$

$$A(2, 3) = r_o [\cos (\text{OBL}) (-\sin \Omega \sin \theta + \cos \Omega \cos i \cos \theta) \\ + \sin (\text{OBL}) \sin i \cos \theta]$$

$$A(3, 1) = 0$$

$$A(3, 2) = -r_o \sin (\text{OBL}) (\cos \Omega \cos \theta - \sin \Omega \cos i \sin \theta)$$

$$A(3, 3) = r_o [-\sin (\text{OBL}) (-\sin \Omega \sin \theta + \cos \Omega \cos i \cos \theta) \\ + \sin (\text{OBL}) \sin i \cos \theta]$$

$$\frac{\partial \bar{V}_{SV}(t_o)}{\partial \bar{x}} = \frac{\partial \bar{V}_{EV}^+(t_o)}{\partial \bar{x}} = B$$

$$B(1, 1) = -\cos \Omega \sin \theta - \sin \Omega \cos i \cos \theta$$

$$B(1, 2) = v_o (\sin \Omega \sin \theta - \cos \Omega \cos i \cos \theta)$$

$$B(1, 3) = v_o (-\cos \Omega \cos \theta + \sin \Omega \cos i \sin \theta)$$

$$B(2, 1) = \cos (\text{OBL}) (-\sin \Omega \sin \theta + \cos \Omega \cos i \cos \theta) \\ + \sin (\text{OBL}) \sin i \cos \theta$$

$$B(2, 2) = v_o \cos (\text{OBL}) (-\cos \Omega \sin \theta - \sin \Omega \cos i \cos \theta)$$

$$B(2, 3) = v_o [\cos (\text{OBL}) (-\sin \Omega \cos \theta - \cos \Omega \cos i \sin \theta) \\ - \sin (\text{OBL}) \sin i \sin \theta]$$

$$B(3, 1) = -v_0 \sin(\Omega L) (-\sin \Omega \sin \theta + \cos \Omega \cos i \cos \theta) \\ + \cos(\Omega L) \sin i \cos \theta$$

$$B(3, 2) = -v_0 \sin(\Omega L) (-\cos \Omega \sin \theta - \sin \Omega \cos i \cos \theta)$$

$$B(3, 3) = v_0 [-\sin(\Omega L) (-\sin \Omega \cos \theta - \cos \Omega \cos i \sin \theta) \\ - \cos(\Omega L) \sin i \sin \theta]$$

Subroutine COMFG3

**A. Input Parameters**

<u>Parameters</u>	<u>Symbol</u>	<u>Definition</u>
TSTART	$t_o$	
TEND	$t_f$	
REVMAG	$r_o$	$ \bar{R}_{EV}(t_o) $
VEVMAG	$v_o$	$ \bar{v}_{EV}^+(t_o) $
LON	$\Omega$ (rad)	Longitude of ascending node
THE	$\theta$	Position of vehicle from ascending node in orbital plane
OINC	$i$ (rad)	Orbital inclination
REMO	$\bar{R}_{EM}(t_o)$	
VEM0	$\bar{v}_{EM}(t_o)$	

**B. Output Parameters**

FD	$\Delta V$	$\Delta V =  \bar{v}_{EVTAR} - \bar{v}_{EV}(t_f) $
TESTRD	$\epsilon$	$\epsilon =  \bar{\psi} $
GD	$\bar{g}$	$\bar{g} = \frac{\partial \Delta V}{\partial (v_o, \Omega, \theta)}$
TSID	$\bar{\psi}$	$\bar{\psi} = \bar{R}_{EV}(t_f) - \bar{R}_{EVTAR}$
LTD	$L^T$	$L^T = \frac{\partial \bar{\psi}}{\partial (v_o, \Omega, \theta)}$
S11, S12, S21, S22	$\phi(t_f, t_o)$	$\phi = \frac{\partial (\bar{R}_{EV}(t_f), \bar{v}_{EV}(t_f))}{\partial (\bar{R}_{EV}(t_o), \bar{v}_{EV}(t_o))}$
UVI	$\bar{u}_{VI}$	$\bar{u}_{VI} = \text{UNIT}(\bar{v}_{EV}^+(t_o) - \bar{v}_{EV}^-(t_o))$
UVF	$\bar{u}_{VF}$	$\bar{u}_{VF} = \text{UNIT}(\bar{v}_{EVTAR} - \bar{v}_{EV}(t_f))$

C. Computation

Call COMIC3 to compute  $\bar{R}_{EV}(t_0)$ ,  $\bar{V}_{EV}^-(t_0)$ ,  $\bar{V}_{EV}^+(t_0)$ .

Call THRBDY to advance states to  $t_f$  and compute  $\phi$ .

For the first iteration, call CTAR3 to compute  $\bar{R}_{EVTAR}$  and  $\bar{V}_{EVTAR}$ .

Equations are same as in COMFG with  $\cos(OBL) = 1$  and  $\sin(OBL) = 0$ .

### Subroutine COMAUG

#### A. Input Parameters

<u>Parameters</u>	<u>Symbol</u>	<u>Definition</u>
F	f	$\Delta V$
G	$\bar{g}$	$\bar{g} = \frac{\partial \Delta V}{\partial (v_o, \Omega, \theta)}$ Constraint gradient transposed
$L^T$	$L^T$	$L^T = \frac{\partial \bar{\psi}}{\partial (v_o, \Omega, \theta)}$
V	V	Davidon's Variance matrix
TSI	$\bar{\psi}$	Constraint violation $\bar{\psi} = \bar{R}(t_f) - \bar{R}_{fd}$ $\bar{R}_{fd} = \bar{R}_{SVTAR}$ or $\bar{R}_{EVTAR}$

#### B. Output Parameters

L	$L$	$L = (L^T)^T$
FG		$f + \bar{v}^T \bar{\psi}$
GG		$\bar{g} + L \bar{v}$

#### C. Computation

$$\begin{aligned} L &= (L^T)^T \\ \bar{v} &= -[L^T V L]^{-1} L^T V \bar{g} \\ FG &= f + \bar{v}^T \bar{\psi} \\ GG &= \bar{g} + L \bar{v} \end{aligned}$$

### Subroutine CTAR

#### A. Input Parameters

<u>Parameters</u>	<u>Symbol</u>	<u>Definition</u>
RSEF	$\bar{R}_{SE}(t_f)$	
VSEF	$\bar{V}_{SE}(t_f)$	
RSMF	$\bar{R}_{SM}(t_f)$	
VSMF	$\bar{V}_{SM}(t_f)$	
REMf	$\bar{R}_{EM}(t_f)$	
VEMf	$\bar{V}_{EM}(t_f)$	
AY	Ay	Parameters to define a point on
AZ	Az	a Halo orbit.
ATAR	A <sub>TAR</sub>	

#### B. Output Parameters

RSVTAR	$\bar{R}_{SVTAR}^S$
VSVTAR	$\bar{V}_{SVTAR}^S$

#### C. Computation

Position and velocity of L<sub>1</sub> in S-frame:

$$\bar{R}_{SL1}^S = (1 - \gamma_{L1}) (\bar{R}_{SE}^S + \frac{\mu_M}{\mu_E + \mu_M} \bar{R}_{EM}^S)$$

$$\bar{V}_{SL1}^S = (1 - \gamma_{L1}) (\bar{V}_{SE}^S + \frac{\mu_M}{\mu_E + \mu_M} \bar{V}_{EM}^S)$$

If both A<sub>y</sub> and A<sub>z</sub> are zero, the following computation is omitted and target position and velocity are set equal to that of L<sub>1</sub>. Define L-frame unit vectors.

$$\bar{u}_{XL}^S = \text{UNIT}(\bar{R}_{SL1}^S)$$

$$\bar{u}_{ZL}^S = \text{UNIT}(\mu_E \bar{R}_{SE}^S \times \bar{V}_{SE}^S + \mu_M \bar{R}_{SM}^S \times \bar{V}_{SM}^S)$$

$$\bar{u}_{YL}^S = \bar{u}_{ZL}^S \times \bar{u}_{XL}^S$$

The matrix to transform a vector from S-frame to L-frame is given by

$$C_S^L = ((\bar{u}_{XL}^S)^T, (\bar{u}_{YL}^S)^T, (\bar{u}_{ZL}^S)^T)$$

The angular velocity of L-frame with respect to S-frame in S-frame is defined by

$$\bar{\omega}_{SL}^S = \bar{u}_{ZL}^S (\bar{u}_{YL}^S \cdot \frac{\bar{v}_{SL1}^S}{|\bar{r}_{SL1}|})$$

The target position and velocity in L-frame are defined by

$$\bar{r}_{LTAR}^L = \begin{pmatrix} k & Ay & \sin A_{TAR} \\ - & Ay & \cos A_{TAR} \\ Az & \sin A_{TAR} \end{pmatrix}$$

$$\bar{v}_{LTAR}^L = \begin{pmatrix} k & \omega_n & Ay & \cos A_{TAR} \\ - & \omega_n & Ay & \sin A_{TAR} \\ \omega_n & Az & \cos A_{TAR} \end{pmatrix}$$

where

$$\omega_n = \sqrt{1 - \frac{B_L}{2} + \sqrt{\left(\frac{3B_L}{2}\right)^2 - 2B_L}}$$

$$B_L = \frac{1 - \mu}{(1 - \gamma_{L1})^3} + \frac{\mu}{\gamma_{L1}^3}$$

$$\mu = \frac{\mu_E + \mu_M}{\mu_S + \mu_E + \mu_M}$$

$$k = \frac{2\omega_n}{\omega_n^2 + (2B_L + 1)}$$

The target position and velocity in S-frame are then given by

$$\bar{r}_{SVTAR}^S = \bar{r}_{SL1}^S + (C_S^L)^T \bar{r}_{LTAR}^L$$

$$\bar{v}_{SVTAR}^S = \bar{v}_{SL1}^S + (C_S^L)^T \bar{v}_{LTAR}^L + \bar{\omega}_{SL}^S \times (C_S^L)^T \bar{r}_{LTAR}^L$$

### Subroutine CTAR3

#### A. Input Parameters

<u>Parameters</u>	<u>Symbol</u>	<u>Definition</u>
REMFI	$\bar{R}_{EM}(t_f)$	In e-frame
VEMFI	$\bar{V}_{EM}(t_f)$	
AY	Ay	
AZ	Az	Parameters to define a point on a Halo orbit
ATAR	A <sub>TAR</sub>	

#### B. Output Parameters

REV TAR	$\bar{R}_{EVTAR}^e$
VEV TAR	$\bar{V}_{EVTAR}^e$

#### C. Computation

Position and velocity of libration point in e-frame

$$\bar{R}_{EL}^e = (1 - \gamma) \bar{R}_{EM}^e \quad \gamma > 0 \text{ for } L_1$$

$$\bar{V}_{EL}^e = (1 - \gamma) \bar{V}_{EM}^e \quad \gamma < 0 \text{ for } L_2$$

If both Ay and Az are zero, the following computation is omitted and target position and velocity are set equal to that of the libration point. Define *l*-frame by unit vectors:

$$\bar{u}_{XL}^e = \text{UNIT}(\bar{R}_{EL}^e)$$

$$\bar{u}_{ZL}^e = \text{UNIT}(\bar{R}_{EM}^e \times \bar{V}_{EM}^e)$$

$$\bar{u}_{YL}^e = \bar{u}_{ZL}^e \times \bar{u}_{XL}^e$$

The matrix to transform a vector from e-frame to *l*-frame is given by

$$C_e^l = ((\bar{u}_{XL}^e)^T, (\bar{u}_{YL}^e)^T, (\bar{u}_{ZL}^e)^T)$$

The angular velocity of  $\ell$ -frame with respect to  $e$ -frame in  $e$ -frame is defined by

$$\bar{\omega}_{EL}^e = \bar{u}_{ZL}^e \left( \bar{u}_{YL}^e \cdot \frac{\bar{v}_{EL}^e}{|\bar{R}_{EL}^e|} \right)$$

The target position and velocity in  $\ell$ -frame are defined by

$$\begin{aligned}\bar{R}_{LTAR}^\ell &= \begin{pmatrix} k & Ay & \sin A_{TAR} \\ Ay & \cos A_{TAR} \\ Az & \sin A_{TAR} \end{pmatrix} \\ \bar{v}_{LTAR}^\ell &= \begin{pmatrix} k & \omega_n & Ay & \cos A_{TAR} \\ -\omega_n & Ay & Ay & \sin A_{TAR} \\ \omega_n & Az & Az & \cos A_{TAR} \end{pmatrix}\end{aligned}$$

where

$$\omega_n = \sqrt{1 + \frac{B_L}{2} + \sqrt{\left(\frac{3B_L}{2}\right)^2 - 2B_L}}$$

$$B_L = \frac{1 - \mu}{(1 - \gamma)^3} + \frac{\mu}{\gamma^3}$$

$$\mu = \frac{\mu_M}{\mu_E + \mu_M}$$

$$k = \frac{2\omega_n}{\omega_n^2 + (2B_L + 1)}$$

The target position and velocity in  $e$ -frame are then given by

$$\bar{R}_{EV TAR}^e = \bar{R}_{EL}^e + (C_e^\ell)^T \bar{R}_{LTAR}^\ell$$

$$\bar{v}_{EV TAR}^e = \bar{v}_{EL}^e + (C_e^\ell)^T \bar{v}_{LTAR}^\ell + \bar{\omega}_{EL}^e \times (C_e^\ell)^T \bar{R}_{LTAR}^\ell$$

**Subroutine COMDX**

**A. Input Parameters**

<u>Parameters</u>	<u>Symbol</u>	<u>Definition</u>
LTS	$L^T$	$\frac{\partial \bar{\psi}}{\partial (v_0, \Omega, \theta)}$
LS	$L$	$\bar{\psi} = \bar{R}(t_f) - \bar{R}_{fd}$
TSIS	$\psi$	$\bar{R}_{fd} = \bar{R}_{SVTAR} \text{ or } \bar{R}_{EVTAR}$

**B. Output Parameters**

DX	$d\bar{x}$	$d\bar{x} = (dv_0, d\Omega, d\theta)$
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**C. Computation**

$$d\bar{x} = -L(L^T L)^{-1} \bar{\psi}$$

### Subroutine RVEMV

#### A. Input Parameters

<u>Parameters</u>	<u>Symbol</u>	<u>Definition</u>
RSV	$\bar{R}_{SV}(t)$	
VSV	$\bar{V}_{SV}(t)$	
RSE	$\bar{R}_{SE}(t)$	
VSE	$\bar{V}_{SE}(t)$	
RSM	$\bar{R}_{SM}(t)$	
VSM	$\bar{V}_{SM}(t)$	

#### B. Output Parameters

REV	$\bar{R}_{EV}(t)$
VEV	$\bar{V}_{EV}(t)$
RMV	$\bar{R}_{MV}(t)$
VMV	$\bar{V}_{MV}(t)$
REM	$\bar{R}_{EM}(t)$
VEM	$\bar{V}_{EM}(t)$

#### C. Computation

$$\bar{R}_{EV} = -\bar{R}_{SE} + \bar{R}_{SV}$$

$$\bar{V}_{EV} = -\bar{V}_{SE} + \bar{V}_{SV}$$

$$\bar{R}_{MV} = -\bar{R}_{SM} + \bar{R}_{SV}$$

$$\bar{V}_{MV} = -\bar{V}_{SM} + \bar{V}_{SV}$$

$$\bar{R}_{EM} = -\bar{R}_{SE} + \bar{R}_{SM}$$

$$\bar{V}_{EM} = -\bar{V}_{SE} + \bar{V}_{SM}$$

This subroutine is used in 4-body program only.

### Subroutine UPX

#### A. Input Parameters

<u>Parameters</u>	<u>Symbol</u>	<u>Definition</u>
XD	$\bar{x}_d$	
FD	$f_d$	
TESTRD	$ \bar{\psi}_d $	
GD	$\bar{g}_d$	
TSID	$\bar{\psi}_d$	
LTD	$(L^T)_d$	
LD	$L_d$	
FGD		$(f + \bar{v}^T \bar{\psi})_d$
GGD		$(\bar{g} + L \bar{v})_d$
S11D, S12D, S21D, S22D	$\phi_d(t_f, t_o)$	
UVID, UVFD	$\bar{\lambda}_d(t_o), \bar{\lambda}_d(t_f)$	

#### B. Output Parameters

Same as input parameters relabelled as X, F, TESTR G, TSI, LT, L  
 FG, GG, SII, S12, S21, S22, UVI, UVF.

#### C. Computation

Set output parameters = input parameters with new names.

### Subroutine LAMB

#### A. Input Parameters

<u>Parameters</u>	<u>Symbol</u>	<u>Definition</u>
T0	$t_0$	
TF	$t_f$	
RSV	$\bar{R}_{SV}(t_0)$	
VSV	$\bar{V}_{SV}(t_0)$	Initial estimate
RSE	$\bar{R}_{SE}(t_0)$	
VSE	$\bar{V}_{SE}(t_0)$	
RSM	$\bar{R}_{SM}(t_0)$	
VSM	$\bar{V}_{SM}(t_0)$	
KNR		Lambert iteration parameter
ITLMAX		Maximum number of iterations
ERRMIN		Convergence criterion
RSVTAR	$\bar{R}_{SVTAR}$	

#### B. Output Parameters

RSVF	$\bar{R}_{SV}(t_f)$	
VSVF	$\bar{V}_{SV}(t_f)$	
RSEF	$\bar{R}_{SE}(t_f)$	
VSEF	$\bar{V}_{SE}(t_f)$	
RSMF	$\bar{R}_{SM}(t_f)$	
VSMF	$\bar{V}_{SM}(t_f)$	
VSV	$\bar{V}_{SV}(t_0)$	Final solution
S11, S12, S21, S22	$\varphi(t_f, t_0)$	State transition matrix

### C. Computation

Call FOURBY to advance states to  $t_f$ . Newton-Raphson method is used which iterates on  $\bar{V}_{SV}(t_o)$  until terminal constraint violation is less than ERRMIN or the number of iteration exceeds ITERL. The desired change in initial velocity is given by

$$d\bar{V} = -(\varphi_{12})^{-1} (\bar{R}_{SVTAR} - \bar{R}_{SV}(t_f))$$

The subroutine has a built-in safeguard against inversion of a singular matrix when the transfer is 2-dimensional.

### D. Internal Parameters

VIV

Dummy iteration variables of initial velocity.

ERR

Error vector of terminal constraint violation

TESTR

Magnitude of ERR.

Subroutine LAMB3

**A. Input Parameters**

<u>Parameters</u>	<u>Symbol</u>	<u>Definition</u>
T0	$t_o$	
TF	$t_f$	
REV	$\bar{R}_{EV}(t_o)$	
VEV	$\bar{V}_{EV}(t_o)$	Initial estimate
REM	$\bar{R}_{EM}(t_o)$	
VEM	$\bar{V}_{EM}(t_o)$	
KNR		
ITLMAX		
ERRMIN		
REVTAR		

**B. Output Parameters**

REVF	$\bar{R}_{EV}(t_f)$	
VEVF	$\bar{V}_{EV}(t_f)$	
REMF	$\bar{R}_{EM}(t_f)$	
VEMF	$\bar{V}_{EM}(t_f)$	
VEV	$\bar{V}_{EV}(t_o)$	Final Solution
S11, S12, S21, S22	$\phi(t_f, t_o)$	

**C. Computation**

Call THRBDY to advance states to  $t_f$ . Use Newton-Raphson method to iterate on  $\bar{V}_{EV}(t_o)$  until terminal constraint violation is less than ERMIN or the number of iteration exceeds ITERL.

The desired change in initial velocity is given by

$$d\bar{V} = -(\phi_{12})^{-1} (\bar{R}_{EVTAR} - \bar{R}_{EV}(t_f))$$

The subroutine has a built-in safeguard against inversion of a singular matrix when the transfer is 2-dimensional.

b. Internal Parameters

Same as listed under LAMB.

Subroutine COMF

A. Input Parameters

Parameter	Symbol	Definition
TSTART	$t_o$	Starting time
TM	$t_m$	Interior impulse time
TEND	$t_f$	Terminal time
RSVO	$\bar{R}_{SV}(t_o)$	
VSVI	$\bar{V}_{SV}^+(t_o)$	
VSVO	$\bar{V}_{SV}^-(t_o)$	
RSEO	$\bar{R}_{SE}(t_o)$	
VSEO	$\bar{V}_{SE}(t_o)$	
RSMO	$\bar{R}_{SM}(t_o)$	
VSMO	$\bar{V}_{SM}(t_o)$	
ERRMIN		Allowable position error
JLINC		Number of increments in solving Lambert problem
KNRSAV		Lambert iteration parameter
ITERD		Outer loop iteration number
ITLMAX		Maximum number of Lambert iterations
VSVMPD	$\bar{V}_{SV}^+(t_m)$ , OLD	
RSVMD	$\bar{R}_{SV}(t_m)$ , OLD	
RSVTAR	$\bar{R}_{SVTAR}$	Target position
VSVTAR	$\bar{V}_{SVTAR}$	Target velocity
S11D	$\phi_{11}(t_f, t_m)$ OLD	
S12D	$\phi_{12}(t_f, t_m)$ OLD	

**B. Output Parameters**

RSVM	$\bar{R}_{SV}(t_m)$	
VSVMP	$\bar{V}_{SV}^+(t_m)$	
VSVMM	$\bar{V}_{SV}^-(t_m)$	
DV	$\Delta V$	
UVI	$\bar{U}_{VI}$	
UVM	$\bar{U}_{VM}$	
UVF	$\bar{U}_{VF}$	
SMI11		
SMI12		
SMI21	$\varphi(t_m, t_o)$	State transition matrix from $t_o$ to $t_m$ .
SMI22		
SFM11		
SFM12		
SFM21	$\varphi(t_f, t_m)$	State transition matrix from $t_m$ to $t_f$ .
SFM22		

**C. Computation**

Step 1. Call FOURBY to advance states from  $t_o$  to  $t_m$ .

Step 2. If ITERD  $\neq 0$ , go to step 4.

Step 3. Set  $\bar{V}_{SVX}^+(t_m) = \bar{V}_{SV}^+(t_m)$

$$\bar{R}_{SVX}(t_m) = \bar{R}_{SV}(t_m)$$

Go to step 6.

Step 4. Solve second leg Lambert problem in increments

$$\bar{R}_{SVX}(t_m) = \bar{R}_{SV}(t_m)_{OLD}$$

$$\bar{V}_{SVX}^+(t_m) = \bar{V}_{SV}^+(t_m)_{OLD}$$

$$d\bar{R}_m = (\bar{R}_{SV}(t_m) - \bar{R}_{SV}(t_m)_{OLD}) / ILINC$$

$$\text{Set } \varphi_{11}(t_f, t_m) = \varphi_{11, OLD}$$

$$\varphi_{12}(t_f, t_m) = \varphi_{12, OLD}$$

ITERL = 0

Step 5.  $d\bar{V}_m = -\varphi_{12}(t_f, t_m)^{-1} \varphi_{11}(t_f, t_m) d\bar{R}_m$

$$\bar{R}_{SVX}(t_m) = \bar{R}_{SVX}(t_m) + d\bar{R}_m$$

$$\bar{V}_{SVX}^+(t_m) = \bar{V}_{SVX}^+(t_m) + d\bar{V}_m$$

Step 6. Call LAMB

$$ITERL = ITERL + 1$$

If  $ITERL < ILINC$ , go to step 5.

Step 7.  $\bar{V}_{SV}^+(t_m) = \bar{V}_{SVX}^+(t_m)$

Step 8.  $\Delta\bar{V}_o = \bar{V}_{SV}^+(t_o) - \bar{V}_{SV}^-(t_o)$

$$\Delta\bar{V}_m = \bar{V}_{SV}^+(t_m) - \bar{V}_{SV}^-(t_m)$$

$$\Delta\bar{V}_f = \bar{V}_{SVTAR} - \bar{V}_{SV}(t_f)$$

$$\bar{u}_{VI} = \text{unit}(\Delta\bar{V}_o)$$

$$\bar{u}_{VM} = \text{UNIT}(\Delta\bar{V}_m)$$

$$\bar{u}_{VF} = \text{UNIT}(\Delta\bar{V}_f)$$

$$\Delta V = |\Delta\bar{V}_o| + |\Delta\bar{V}_m| + |\Delta\bar{V}_f|$$

Step 9. EXIT

Subroutine COMF3

**A. Input Parameters**

<u>Parameters</u>	<u>Symbol</u>	<u>Definition</u>
TSTART	$t_o$	
TM	$t_m$	
TEND	$t_f$	
REVO	$\bar{R}_{EV}(t_o)$	
VEVOP	$\bar{V}_{EV}^+(t_o)$	
VEVO	$\bar{V}_{EV}^-(t_o)$	
REMO	$\bar{R}_{EM}(t_o)$	
VEMO	$\bar{V}_{EM}(t_o)$	
ERRMIN		Allowable position error
ILINC		Number of increments to solve Lambert problem
KNRSAV		Lambert iteration parameter
ITERD		Iteration number of outer loop
ITLMAX		Maximum Lambert iterations
VEVMPD	$\bar{V}_{EV}(t_m)_{OLD}$	
REVMD	$\bar{R}_{EV}(t_m)_{OLD}$	
REVTAR	$\bar{R}_{EVTAR}$	
VEVTAR	$\bar{V}_{EVTAR}$	
S1D	$\phi_{11}(t_f, t_m)_{OLD}$	
S2D	$\phi_{12}(t_f, t_m)_{OLD}$	

**B. Output Parameters**

REV M	$\bar{R}_{EV}(t_m)$
V <sub>EVMP</sub>	$\bar{V}_{EV}^+(t_m)$
V <sub>EVMM</sub>	$\bar{V}_{EV}^-(t_m)$
DV	$\Delta V$
UVI	$\bar{u}_{VI}$
UVM	$\bar{u}_{VM}$
UVF	$\bar{u}_{VF}$
SMI11	$\varphi(t_m, t_o)$
SMI12	
SMI21	
SMI22	
SFM11	$\varphi(t_f, t_m)$
SFM12	
SFM21	
SFM22	
DVM	$\Delta \bar{V}_m$

**C. Computation**

Step 1. Call THREBDY to advance states from  $t_o$  to  $t_m$ .

Step 2. If ITERD  $\neq 0$ , go to step 4.

Step 3. Set  $\bar{V}_{EVX}^+(t_m) = \bar{V}_{EV}^+(t_m)$

$$\bar{R}_{EVX}(t_m) = \bar{R}_{EV}(t_m)$$

Go to step 6.

Step 4. Solve second leg Lambert problem

$$\bar{R}_{EVX}(t_m) = \bar{R}_{EV}(t_m)_{OLD}$$

$$\bar{V}_{EVX}^+(t_m) = \bar{V}_{EV}^+(t_m)_{OLD}$$

$$\delta \bar{R}_M = (\bar{R}_{EV}(t_m) - \bar{R}_{EV}(t_m)_{OLD}) / ILINC$$

$$Set \varphi_{11}(t_f, t_m) = \varphi_{11, OLD}$$

$$\varphi_{12}(t_f, t_m) = \varphi_{12, OLD}$$

$$ITERL = 0$$

Step 5.  $d\bar{V}_m = -\varphi_{12}(t_f, t_m)^{-1} \varphi_{11}(t_f, t_m) d\bar{R}_m$

$$\bar{R}_{EVX}(t_m) = \bar{R}_{EVX}(t_m) + d\bar{R}_m$$

$$\bar{V}_{EVX}^+(t_m) = \bar{V}_{EVX}^+(t_m) + d\bar{V}_m$$

Step 6. Call LAMB3

$$ITERL = ITERL + 1$$

If  $ITERL < ILINC$ , go to step 5.

Step 7.  $\bar{V}_{EV}^+(t_m) = \bar{V}_{EVX}^+(t_m)$

Step 8.  $\Delta\bar{V}_o = \bar{V}_{EV}^+(t_o) - \bar{V}_{EV}^-(t_o)$

$$\Delta\bar{V}_m = \bar{V}_{EV}^+(t_m) - \bar{V}_{EV}^-(t_m)$$

$$\Delta\bar{V}_f = \bar{V}_{EVTAR} - \bar{V}_{EV}(t_f)$$

$$\bar{u}_{V1} = \text{unit}(\Delta\bar{V}_o)$$

$$\bar{u}_{VM} = \text{unit}(\Delta\bar{V}_m)$$

$$\bar{u}_{VF} = \text{unit}(\Delta\bar{V}_f)$$

$$\Delta V = |\Delta\bar{V}_o| + |\Delta\bar{V}_M| + |\Delta\bar{V}_f|$$

Step 9. EXIT

Subroutine COMG

**A. Input Parameters**

Parameters	Symbol	Definition
SMI11	$\varphi_{11}(t_m, t_o)$	
SMI12	$\varphi_{12}(t_m, t_o)$	
SMI21	$\varphi_{21}(t_m, t_o)$	
SMI22	$\varphi_{22}(t_m, t_o)$	
SFM11	$\varphi_{11}(t_f, t_m)$	
SFM12	$\varphi_{12}(t_f, t_m)$	
SFM21	$\varphi_{21}(t_f, t_m)$	
SFM22	$\varphi_{22}(t_f, t_m)$	
UVI	$\bar{u}_{VI}$	
UVM	$\bar{u}_{VM}$	
UVF	$\bar{u}_{VF}$	
VTMM	$v^-(t_m)$	
VTMP	$v^+(t_m)$	

**B. Output Parameter**

G	$\bar{g}$	Cost gradient $g = \frac{\partial \Delta V}{\partial (V^+(t_o), t_m)}$
DUVI	$\dot{\lambda}(t_o)$	
DUVMM	$\dot{\lambda}^-(t_m)$	
DUVMP	$\dot{\lambda}^+(t_m)$	

**C. Computation**

$$\dot{\lambda}(t_o) = \varphi_{mo, 12}^{-1} (\bar{u}_{VM} - \varphi_{mo, 11} \bar{u}_{VI})$$

$$\dot{\lambda}^-(t_m) = \varphi_{mo, 21} \bar{u}_{VI} + \varphi_{mo, 22} \dot{\lambda}(t_0)$$

$$\dot{\lambda}^+(t_m) = \varphi_{fm, 12}^{-1} (\bar{u}_{VF} - \varphi_{fm, 11} \bar{u}_{VM})$$

$$\frac{d}{dt} |\dot{\lambda}_m^-| = \dot{\lambda}_m^- \cdot \bar{u}_{VM}$$

$$\frac{d}{dt} |\dot{\lambda}_m^+| = \dot{\lambda}_m^+ \cdot \bar{u}_{VM}$$

$$\frac{\partial \Delta V}{\partial V_o} = \varphi_{mo, 12}^T (\dot{\lambda}_m^+ - \dot{\lambda}_m^-)$$

$$\frac{\partial \Delta V}{\partial t_m} = -\dot{\lambda}_m^+ \cdot (V_m^+ - V_M^-)$$

$$\bar{g} = \left( \frac{\partial \Delta V^T}{\partial V_o}, \frac{\partial \Delta V}{\partial t_m} \right)$$

NOTE: In addition to the output parameters the following parameters are also printed out after each iteration.

<u>Parameter</u>	<u>Symbol</u>
PVMMAG	$\frac{d}{dt}  \dot{\lambda}_m^- $
PVP MAG	$\frac{d}{dt}  \dot{\lambda}_m^+ $

**Subroutine PVEC**

**A. Input Parameters**

<u>Parameters</u>	<u>Symbol</u>	<u>Definition</u>
T	t	
R	R	
V	V	
PV0	PV(t <sub>o</sub> )	
STM	$\varphi(t, t_o)$	State transition matrix
IPVTM		IPVTM = 0, Advance PV only 1, Also monitor max. value of primer vector magnitude.

**B. Output Parameters**

PV	PV(t)	$PV(t) = (\bar{\lambda}(t), \dot{\bar{\lambda}}(t))$
LM	$ \bar{\lambda} $	
LDM	$\frac{d}{dt}  \bar{\lambda} $	

The following parameters are transmitted through COMMON/CTM/.

TTM	t <sub>m</sub>	Time of maximum $ \bar{\lambda} $
RTM	$\bar{R}(t_m)$	
VTM	$\bar{V}(t_m)$	
LTM	$ \bar{\lambda}(t_m) $	
LDTM	$\frac{d}{dt}  \bar{\lambda}(t_m) $	
PVTM	$\bar{\lambda}(t_m)$	
PVDTM	$\dot{\bar{\lambda}}(t_m)$	
STNTM	$\varphi(t_m', t_o)$	$t_m' = \text{time when the primer vector magnitude is maximum.}$

C. Computation

$$\begin{pmatrix} \bar{\lambda}(t) \\ \dot{\bar{\lambda}}(t) \end{pmatrix} = \varphi(t, t_0) \begin{pmatrix} \bar{\lambda}(t_0) \\ \dot{\bar{\lambda}}(t_0) \end{pmatrix}$$

If  $|\text{IPVTM}| \neq 0$ , monitor  $|\bar{\lambda}(t)|$  to determine maximum value.

Subroutine DISP

Both input and output parameters are transmitted through COMMON/TDATA/.

**A. Input Parameters**

Parameters	Symbol	Definition
RSV	$\bar{R}_{SV}$ S	
VSV	$\bar{V}_{SV}$ S	
REV	$\bar{R}_{EV}$ E	
VEV	$\bar{V}_{EV}$ E	
RMV	$\bar{R}_{MV}$ M	
VMV	$\bar{V}_{MV}$ M	
RSE	$\bar{R}_{SE}$ S	
VSE	$\bar{V}_{SE}$ S	
RSM	$\bar{R}_{SM}$ S	
VSM	$\bar{V}_{SM}$ S	
RDM	$\bar{R}_{EM}$ E	
VEM	$\bar{V}_{EM}$ E	

**B. Output Parameters**

RSL1	$\bar{R}_{SL1}$ S	
VSL1	$\bar{V}_{SL1}$ S	
RDVD	$\bar{R}_{DV}^D$	
VDVD	$\bar{V}_{DV}^D$	
RDSD	$\bar{R}_{DS}^D$	
VDSD	$\bar{V}_{DS}^D$	

Position and velocity of vehicle  
in D-frame

RDMD	$\bar{R}_{DM}^D$	
VMDM	$\bar{V}_{DM}^D$	
RDLID	$\bar{R}_{DL1}^D$	
VDLID	$\bar{V}_{DL1}^D$	
ANGV	$ANG_V$	Angle at vehicle between LOS to sun and earth
ANGE	$ANG_E$	Angle at earth between LOS to sun and vehicle
ANGS	$ANG_S$	Angle at sun between LOS to vehicle and earth

### C. Computation

The position and velocity of 4-body L<sub>1</sub> point in S-frame are computed by

$$\bar{R}_{SL1} = (1 - \gamma_{L1}) (\bar{R}_{SE} + \frac{\mu_M}{\mu_E + \mu_M} \bar{R}_{EM})$$

$$\bar{V}_{SL1} = (1 - \gamma_{L1}) (\bar{V}_{SE} + \frac{\mu_M}{\mu_E + \mu_M} \bar{V}_{EM})$$

An earth centered rotating frame (D-frame) for display is used to suppress the motion of the earth which is significant due to its orbital eccentricity around the sun and the presence of the moon.

Define:

$$\bar{u}X_D^S = \text{unit } (\bar{R}_{SE})$$

$$\bar{u}Z_D^S = \text{unit } (\bar{R}_{SE} \times \bar{V}_{SE})$$

$$\bar{u}Y_D^S = \bar{u}Z_D^S \times \bar{u}X_D^S$$

The transformation from the inertial S-frame to a frame parallel to the rotating D-frame is given by the matrix

$$C_S^D = ((\bar{u}X_D^S)^T, (\bar{u}Y_D^S)^T, (\bar{u}Z_D^S)^T)$$

The D-frame rotates with respect of S-frame with an angular velocity defined by

$$\bar{\omega}_{SD}^S = \bar{u}z_D^S (\bar{u}y_{DS}^S \cdot \bar{v}_{SE}^S) / |\bar{r}_{SE}|$$

The transforming from S-frame to D-frame for typical position and velocity vectors are as follows:

$$\bar{r}_{SD}^S = \bar{r}_{SE}^S$$

$$\bar{v}_{SD}^S = \bar{v}_{SE}^S$$

$$\bar{r}_{DV}^D = C_S^D \bar{r}_{DV}^S = C_S^D (\bar{r}_{SV}^S - \bar{r}_{SD}^S)$$

$$\bar{v}_{DV}^D = C_S^D (\bar{v}_{SV}^S - \bar{v}_{SD}^S - \bar{\omega}_{SD}^S \times \bar{r}_{DV}^S)$$

The angles at the vehicle, sun and earth are computed by

$$\bar{u}r_{SE} = \text{UNIT}(\bar{r}_{SE})$$

$$\bar{u}r_{EV} = \text{UNIT}(\bar{r}_{EV})$$

$$\bar{u}r_{SV} = \text{UNIT}(\bar{r}_{SV})$$

$$\text{ANG}_V = \cos^{-1}(\bar{u}r_{EV} \cdot \bar{u}r_{SV})/\text{DTR}$$

$$\text{ANG}_E = \cos^{-1}(-\bar{u}r_{SE} \cdot \bar{u}r_{EV})/\text{DTR}$$

$$\text{ANG}_S = 180 - (\text{ANG}_V + \text{ANG}_E)$$

DTR = Degree to radian conversion

Subroutine DISP3

Both input and output parameters are transmitted through COMMON/TDATAS/.

A. Input Parameters

<u>Parameters</u>	<u>Symbol</u>	<u>Definition</u>
REV	$\bar{R}_{EV}^e$	
VEV	$\bar{V}_{EV}^e$	
RMV	$\bar{R}_{MV}^m$	
VMV	$\bar{V}_{MV}^m$	
REM	$\bar{R}_{EM}^e$	
VEM	$\bar{V}_{EM}^e$	

B. Output Parameters

REL	$\bar{R}_{EL}^e$
VEL	$\bar{V}_{EL}^e$
RDVD	$\bar{R}_{DV}^d$
VDVD	$\bar{V}_{DV}^d$
RDED	$\bar{R}_{DE}^d$
VDED	$\bar{V}_{DE}^d$
RDLD	$\bar{R}_{DL}^D$
VDLD	$\bar{V}_{DL}^D$
ANGV	$ANG_V$
ANGE	$ANG_E$
ANGM	$ANG_M$

### C. Computation

The position and velocity of 3-body libration point L in e-frame are computed by

$$\bar{R}_{EL} = (1 - \gamma) \bar{R}_{EM}$$

$$\bar{V}_{EL} = (1 - \gamma) \bar{V}_{EM}$$

where  $\gamma > 0$  for  $L_1$  and  $\gamma < 0$  for  $L_2$ .

A moon centered rotating frame (d-frame) for display is used to suppress the motion of the moon. Define

$$\bar{u}_{XD}^e = \text{UNIT}(\bar{R}_{EM}^e)$$

$$\bar{u}_{ZD}^e = \text{unit}(\bar{R}_{EM}^e \times \bar{V}_{EM}^e)$$

$$\bar{u}_{YD}^e = \bar{u}_{ZD}^e \times \bar{u}_{XD}^e$$

The transformation from the inertial e-frame to a frame parallel to the rotating d-frame is given by the matrix

$$C_e^d = ((\bar{u}_{XD}^e)^T, (\bar{u}_{YD}^e)^T, (\bar{u}_{ZD}^e)^T)$$

The d-frame rotates with respect to the e-frame with an angular velocity

$$\bar{\omega}_{ed}^e = \bar{u}_{ZD}^e \left( \bar{u}_{YD}^e \cdot \frac{\bar{V}_{EM}^e}{|\bar{R}_{EM}^e|} \right)$$

The transformations from the e-frame to d-frame for typical position and velocity vectors are as follows:

$$\bar{R}_{ED}^e = \bar{R}_{EM}^e$$

$$\bar{V}_{ED}^e = \bar{V}_{EM}^e$$

$$\bar{R}_{DV}^d = C_e^d \bar{R}_{DV}^e = C_e^d (\bar{R}_{EV}^e - \bar{R}_{ED}^e)$$

$$\bar{V}_{DV}^d = C_e^d (\bar{V}_{EV}^e - \bar{V}_{ED}^e - \bar{\omega}_{ed}^e \times \bar{R}_{DV}^e)$$

The angles at the vehicle, earth and moon are computed by:

$$\bar{u}R_{MV} = \text{UNIT}(\bar{R}_{MV})$$

$$\bar{u}R_{EM} = \text{UNIT}(\bar{R}_{EM})$$

$$\bar{u}R_{EV} = \text{UNIT}(\bar{R}_{EV})$$

$$\text{ANG}_V = \cos^{-1}(\bar{u}R_{MV} \cdot \bar{u}R_{EV})/\text{DTR}$$

$$\text{ANG}_M = \cos^{-1}(-\bar{u}R_{EM} \cdot \bar{u}R_{MV})/\text{DTR}$$

$$\text{ANG}_E = 180 - (\text{ANG}_V + \text{ANG}_M)$$

DTR = Degree to radian conversion

Subroutine PTRAJ

Input parameters are transmitted through COMMON/TDATA/. If  
IPTRAJ = 1, the following parameters are printed at each time step.

T	T(DAY)	H	$\bar{R}_{SV}$	$\bar{R}_{EV}$	$\bar{R}_{MV}$
$\bar{R}_{SV}$	S		$\bar{V}_{SV}$	S	
$\bar{R}_{EV}$	E		$\bar{V}_{EV}$	E	
$\bar{R}_{MV}$	M		$\bar{V}_{MV}$	M	
$\bar{R}_{SE}$	S		$\bar{V}_{SE}$	S	
$\bar{R}_{SM}$	S		$\bar{V}_{SM}$	S	
$\bar{R}_{EM}$	E		$\bar{V}_{EM}$	E	
$\bar{R}_{SL1}$	S		$\bar{V}_{SL1}$	S	
$\bar{R}_{DV}$	D		$\bar{V}_{DV}$	D	
$\bar{R}_{DS}$	D		$\bar{V}_{DS}$	D	
$\bar{R}_{DM}$	D		$\bar{V}_{DM}$	D	
$\bar{R}_{DL1}$	D		$\bar{V}_{DL1}$	D	
ANG <sub>V</sub>		ANG <sub>E</sub>	ANG <sub>S</sub>	H(DAY)	

If IPV = 1, the primer vector history below is printed.

$$\begin{array}{ccc} \bar{\lambda} & & \dot{\bar{\lambda}} \\ |\bar{\lambda}| & \frac{d}{dt} |\bar{\lambda}| & \end{array}$$

Subroutine PTRAJ3

Input parameters are transmitted through COMMON/TDATA3/. If  
 IPTRAJ = 1, the following parameters are printed at each time step.

T	TDAY	H	H(DAY)	$ \bar{R}_{EV} $	$ \bar{R}_{MV} $
$\bar{R}_{EV}^e$				$\bar{V}_{EV}^e$	
$\bar{R}_{MV}^m$				$\bar{V}_{MV}^m$	
$\bar{R}_{EM}^e$				$\bar{V}_{EM}^e$	
$\bar{R}_{EL}^e$				$\bar{V}_{EL}^e$	
$\bar{R}_{DV}^d$				$\bar{V}_{DV}^d$	
$\bar{R}_{DE}^d$				$\bar{V}_{DE}^d$	
$\bar{R}_{DL}^d$				$\bar{V}_{DL}^d$	
ANG <sub>V</sub>	ANG <sub>E</sub>	ANG <sub>M</sub>			

If IIV = 1, the primor vector history is printed

$$\dot{\lambda}$$

$$|\lambda| \quad \frac{d}{dt} |\lambda|$$

### Subroutine FDATA

Input parameters are transmitted through COMMON/TDATA/. If IFILEX or IFILE is position nonzero the following double precision parameters are filed sequentially in unformatted form.

<u>Parameter</u>	<u>File Location</u>	<u>Parameter</u>	<u>File Location</u>
t	+ 1	$\bar{V}_{DS}$ <sup>D</sup>	54 - 56
h	2	$\bar{R}_{DM}$ <sup>D</sup>	57 - 59
$\bar{V}_{SV}$	3 - 5	$\bar{V}_{DM}$ <sup>D</sup>	60 - 62
$\bar{V}_{SV}$	6 - 8	$\bar{R}_{DLI}$ <sup>D</sup>	63 - 65
$\bar{R}_{EV}$	9 - 11	$\bar{V}_{DLI}$ <sup>D</sup>	66 - 68
$\bar{V}_{EV}$	12 - 14	$\lambda, \dot{\lambda}$	69 - 74
$\bar{R}_{MV}$	15 - 17	$ \bar{A} $	75
$\bar{V}_{MV}$	18 - 20	$\frac{d}{dt}  \bar{A} $	76
$\bar{R}_{SE}$	21 - 23	ANG <sub>V</sub>	77
$\bar{V}_{SE}$	24 - 26	ANG <sub>E</sub>	78
$\bar{R}_{SM}$	27 - 29	ANG <sub>S</sub>	79
$\bar{V}_{SM}$	30 - 32	$ \bar{R}_{SV} $	80
$\bar{R}_{EM}$	33 - 35	$ \bar{V}_{SV} $	81
$\bar{V}_{EM}$	36 - 38	$ \bar{R}_{EV} $	82
$\bar{R}_{SLI}$	39 - 41	$ \bar{V}_{EV} $	83
$\bar{V}_{SLI}$	42 - 44	$ \bar{R}_{MV} $	84
$\bar{R}_{DV}$ <sup>D</sup>	45 - 47	$ \bar{V}_{MV} $	85
$\bar{V}_{DV}$ <sup>D</sup>	48 - 50	Blank	86 - 100
$\bar{R}_{DS}$ <sup>D</sup>	51 - 53	Total	100

Subroutine FDATA3

Input parameters are transmitted through COMMON/TDATA3/. If IFILEX or IFILE is positive nonzero, the following double precision parameters are filed sequentially in unformatted form.

<u>Parameter</u>	<u>File Location</u>	<u>Parameter</u>	<u>File Location</u>
t	+1	$\bar{v}_{DL}^d$	42 - 44
h	2	$\bar{\lambda}, \dot{\bar{\lambda}}$	45 - 50
$\bar{R}_{EV}$	3 - 5	$ \bar{\lambda} $	51
$\bar{v}_{EV}$	6 - 8	$\frac{d}{dt}  \bar{\lambda} $	52
$\bar{R}_{MV}$	9 - 11	ANG <sub>V</sub>	53
$\bar{v}_{MV}$	12 - 14	ANG <sub>E</sub>	54
$\bar{R}_{EM}$	15 - 17	ANG <sub>M</sub>	55
$\bar{v}_{EM}$	18 - 20	$ \bar{R}_{EV} $	56
$\bar{R}_{EL}$	21 - 23	$ \bar{v}_{EV} $	57
$\bar{v}_{EL}$	24 - 26	$ \bar{R}_{MV} $	58
$\bar{R}_{DV}^d$	27 - 29	$ \bar{v}_{MV} $	59
$\bar{v}_{DV}^d$	30 - 32	$ \bar{R}_{EM} $	60
$\bar{R}_{DE}^d$	33 - 35	$ \bar{v}_{EM} $	61
$\bar{v}_{DE}^d$	36 - 38	Blank	62 - 75
$\bar{R}_{DL}^d$	39 - 41	Total	75

## TROUBLE SHOOTING

In this section we list a number of common troubles, their causes and suggested corrective actions.

<u>Trouble</u>	<u>Diagnosis</u>	<u>Action</u>
Integration too slow.	Allowable single step position error too small. Input error.	Increase ERRMAX or ERRMXM. Check input.
TWOBDY fails to converge or gives strange answers.	Bad input state vector or gravitational constants.	Check input.
FOURBY (THRBDY) gives strange answers.	Bad input to TWOBDY.	Check input.
Slow to satisfy constraint.	Allowable terminal error too small.	Increase ERRMIN or EPSTSI.
LAMB (LAMB3) fails to converge.	Bad nominal trajectory.	Search for new nominal closer to satisfy constraint. Reduce KNR.
ETP2I (ETP2I3) fails to satisfy constraint.	Bad nominal trajectory.	Search for new nominal closer to satisfy constraint. Reduce KDX.
ETP2I (ETP2I3) fails to reduce $\Delta V$ .	Bad V-matrix.	Reduce EPSV. Try new estimate of independent variables.
PTP3I (PtP3I3) fails to reduce $\Delta V$ .	Bad V-matrix.	Reduce EPSV. Try new estimate of independent variables.

### Helpful Suggestions

1. It pays to search for a nominal trajectory which comes close to satisfy terminal constraint. This is not so important in a short transfer, which will converge even if the nominal trajectory misses the target badly. For long transfer, a bad nominal trajectory will prolong iterations due to increased nonlinearity, which reduces permissible changes in the independent variables.

2. A capability to plot trajectory is very helpful to show whether a nominal trajectory is heading in the right direction. It is not difficult to adjust the independent variables properly after examining a plot of the trajectory but it is very difficult to determine what action to take by looking at a printout.
3. It is generally better to run the programs by a succession of short runs instead of a single long run. The pauses between short runs enable the user to interpret the results and make necessary changes. It is not possible nor practical to fully automate a program to take into account all possible contingencies.
4. When a run is continued, use the current independent variables, V-matrix, KDX, KNR, etc. to maintain continuity.

## EXAMPLE 1

### A. Purpose

This example may be used to check out Program TRAJ and associated subroutines. It is a 4-body transfer from noon July 4, 1978 from a 100 n. mi. earth parking orbit to L<sub>1</sub> in 36 days.

### B. Input Parameters

<u>Card No.</u>	<u>Format</u>	<u>Parameter</u>	<u>Value</u>
1	4D20.11	GL1	1.001098D-02
		AUM	1.49597893D+11
		UTIME	5.81323577632D+01
		UVELM	3.35742409867D-05
2	3D20.11	MS	9.99996959568D-01
		ME	3.00348453188D-06
		MM	3.69431224671D-08
3	4I5	IMODE	1
		IPV	1
		IPTRAJ	1
		IFILE	0
4	4D20.11	RSE0(1)	1.98930090999D-01
		(2)	-9.970505898501D-01
		(3)	6.79027012471D-05
		VSE0(1)	9.64906589348D-01
5	4D20.11	(2)	1.92157060597D-01
		(3)	-1.47749626270D-05

		RSM0 (1)	1.99125783494D-01
		(2)	-9.94358817445D-01
6	4D20.11	(3)	-1.68002571823D-04
		VSM0 (1)	9.32348120275D-01
		(2)	1.95028878329D-01
		(3)	-2.62545160637D-04
7	3D20.11	TDAY0	1.099D+03
		TTRIPD	3.6D+01
		ERRMXM	1.524D+02
8	4D20.11	REVmag	4.38739157152D-05
		VEVmag	3.69220795569D-01
		OINCD	2.85D+01
		OBLD	2.34457874302D+01
9	2D20.11	LOND	3.59181042981D+02
		THED	-3.51880454048D+01
10	4D20.11	$\lambda$ (1)	5.86468563221D-01
		(2)	8.06463656568D-01
		(3)	7.53060089751D-02
		$\lambda$ (1)	-3.43647891554D+03
11	2D20.11	(2)	2.47056772744D+03
		(3)	3.04177095939D+02

C. Output Parameters

A printout of the trajectory at each time step is submitted with this guide in a separate package. The state vectors at the terminal time is

RSV(1)	7.17957115972D-01
(2)	-7.01342803746D-01
(3)	4.27257573439D-05
VSV(1)	6.79829811710D-01
(2)	7.15967885505D-01
(3)	-6.21512714224D-04

The vehicle intercepts the  $I_1$  point after 36 days. The trajectories with respect to earth and moon are shown in Figures 2a to 2f. The primer vector magnitude history is shown in Figure 2g. The  $\Delta V$  of this transfer is 354.57 m/s. Note that the initial earth parking orbit has an inclination of 28.5 deg. If this restriction is removed, the  $\Delta V$  of the same transfer of 36 days is about 288 m/s (Ref. 2).

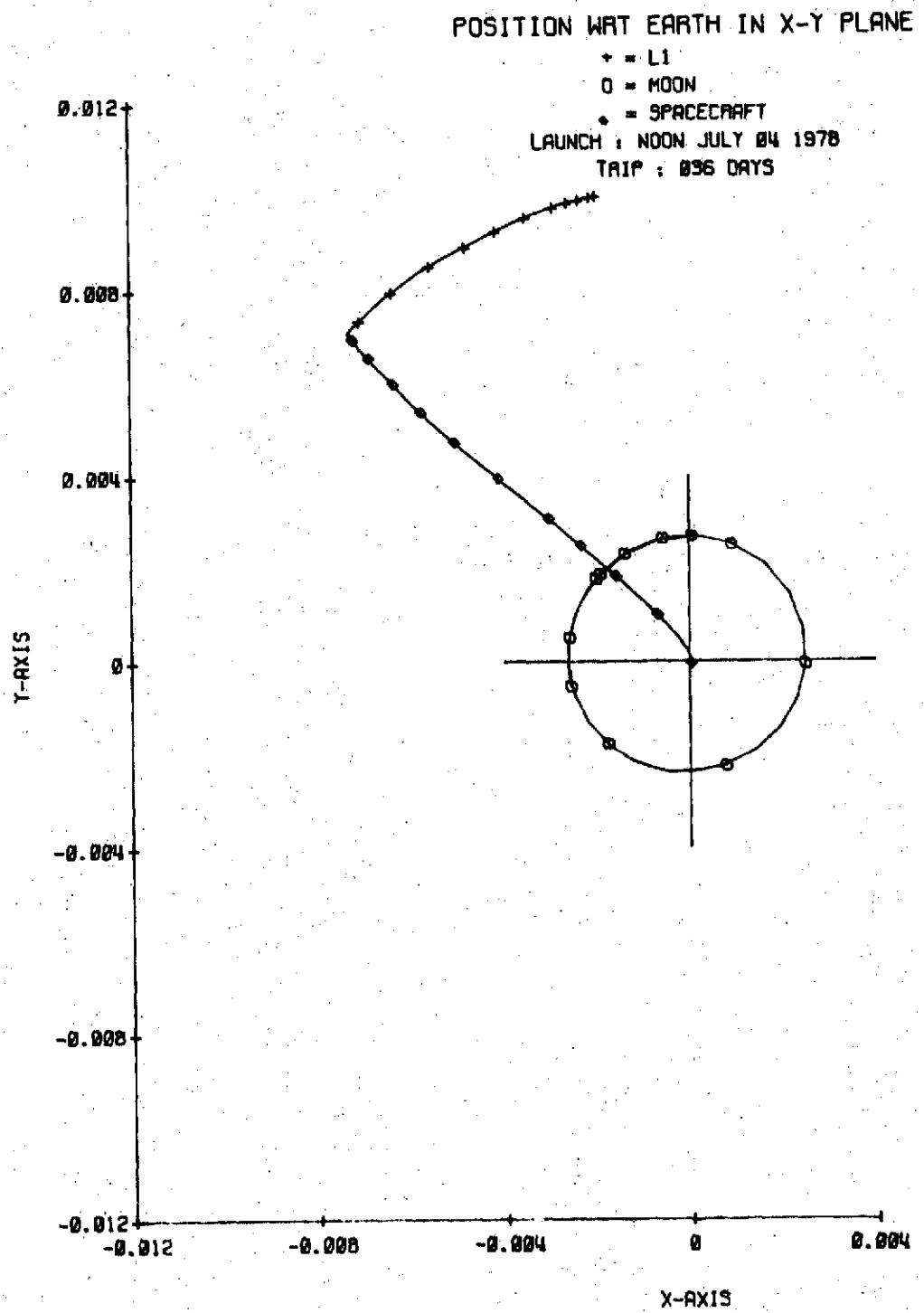


Figure 2a 2-Impulse Transfer (Example 1)

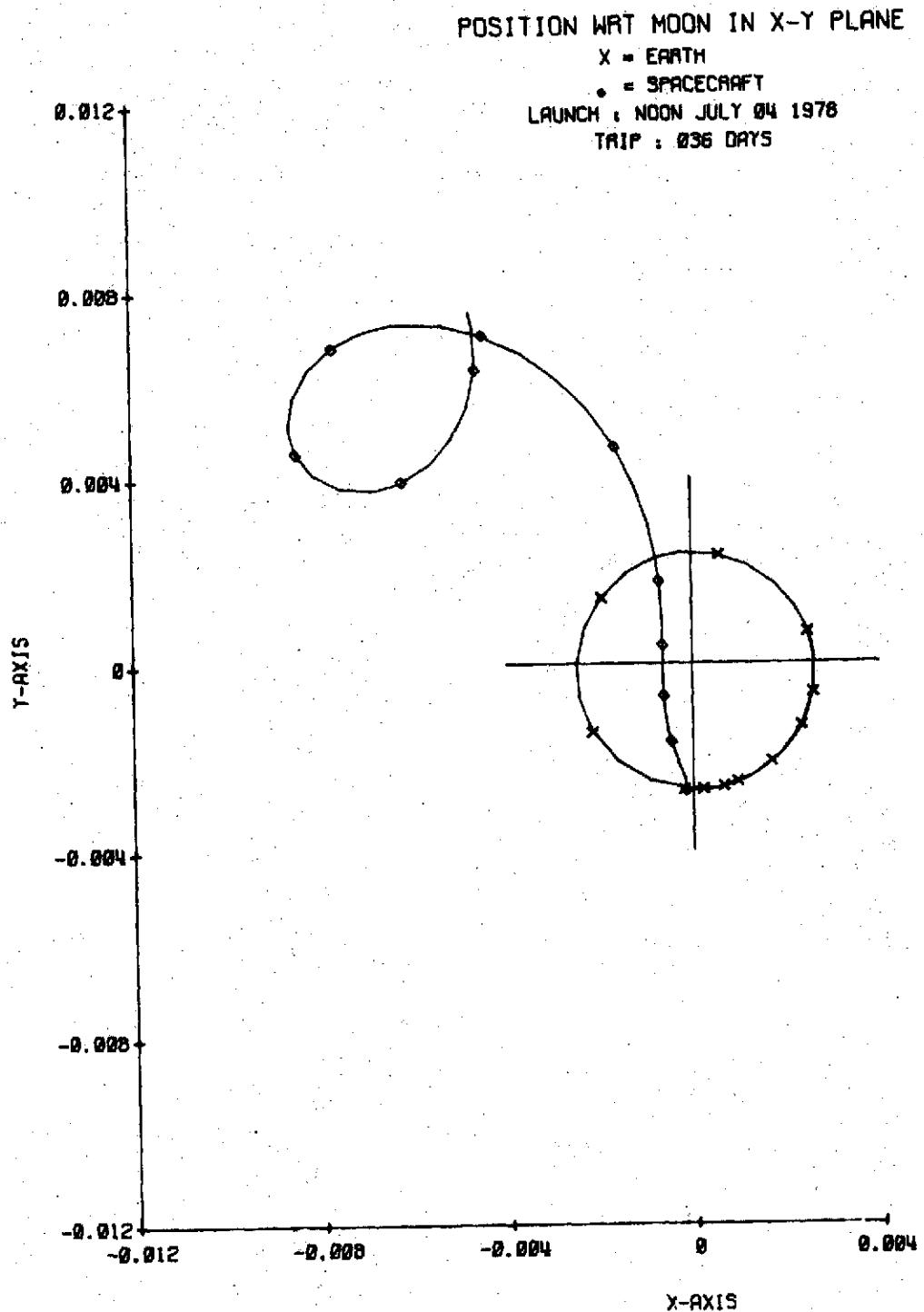


Figure 2b - 2-Impulse Transfer (Example 1)

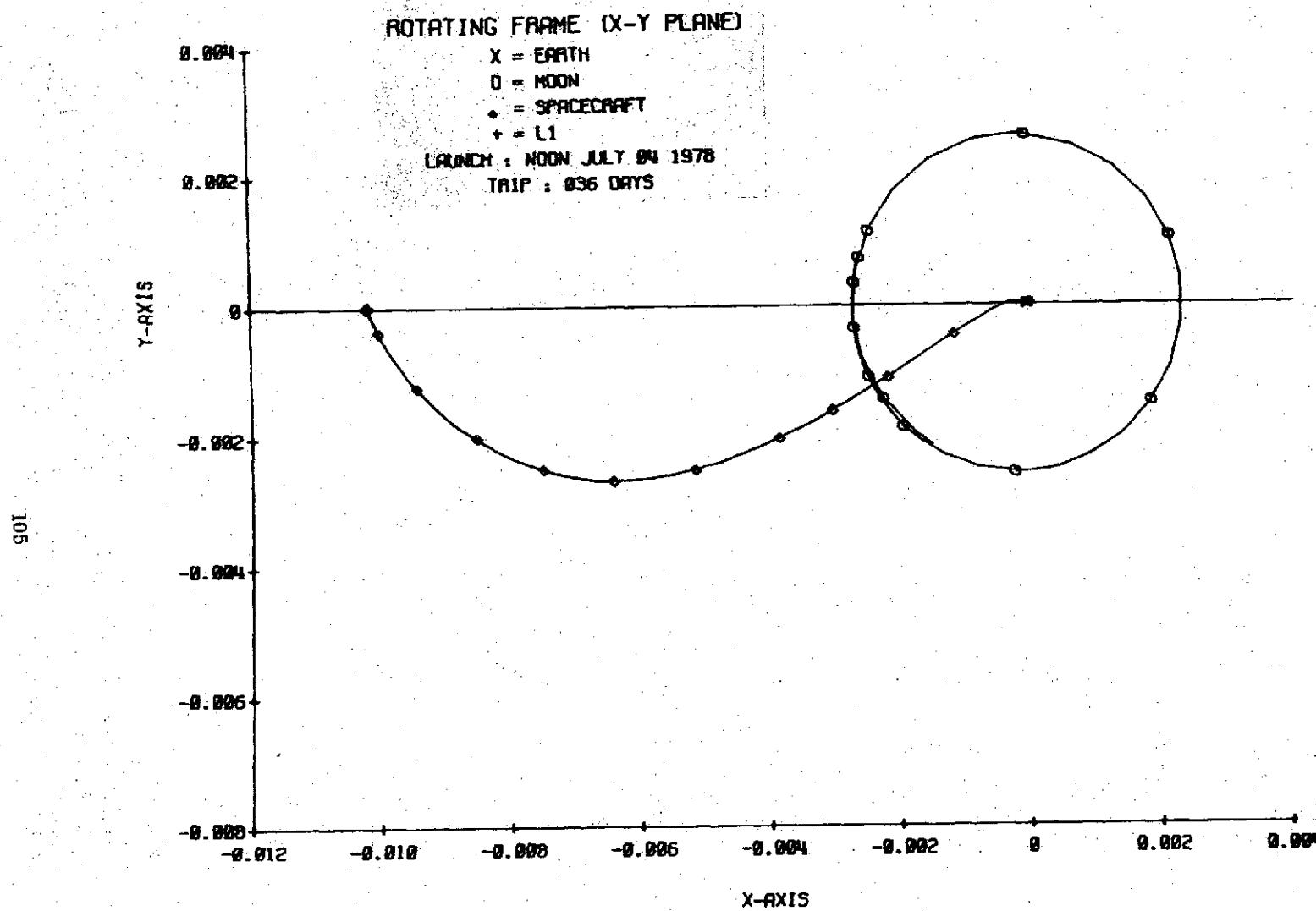


Figure 2c 2-Impulse Transfer (Example 1)

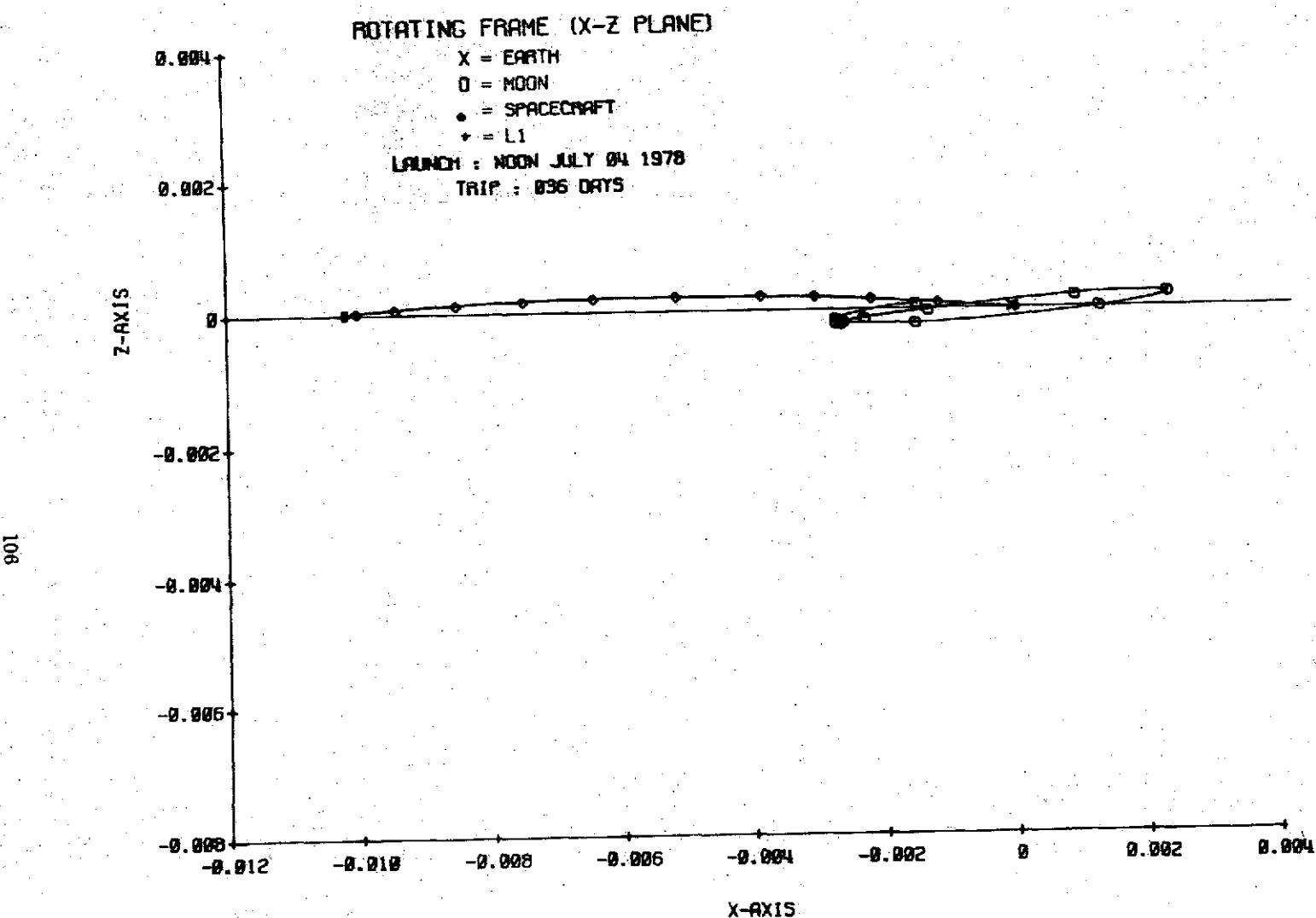


Figure 2d 2-Impulse Transfer (Example 1)

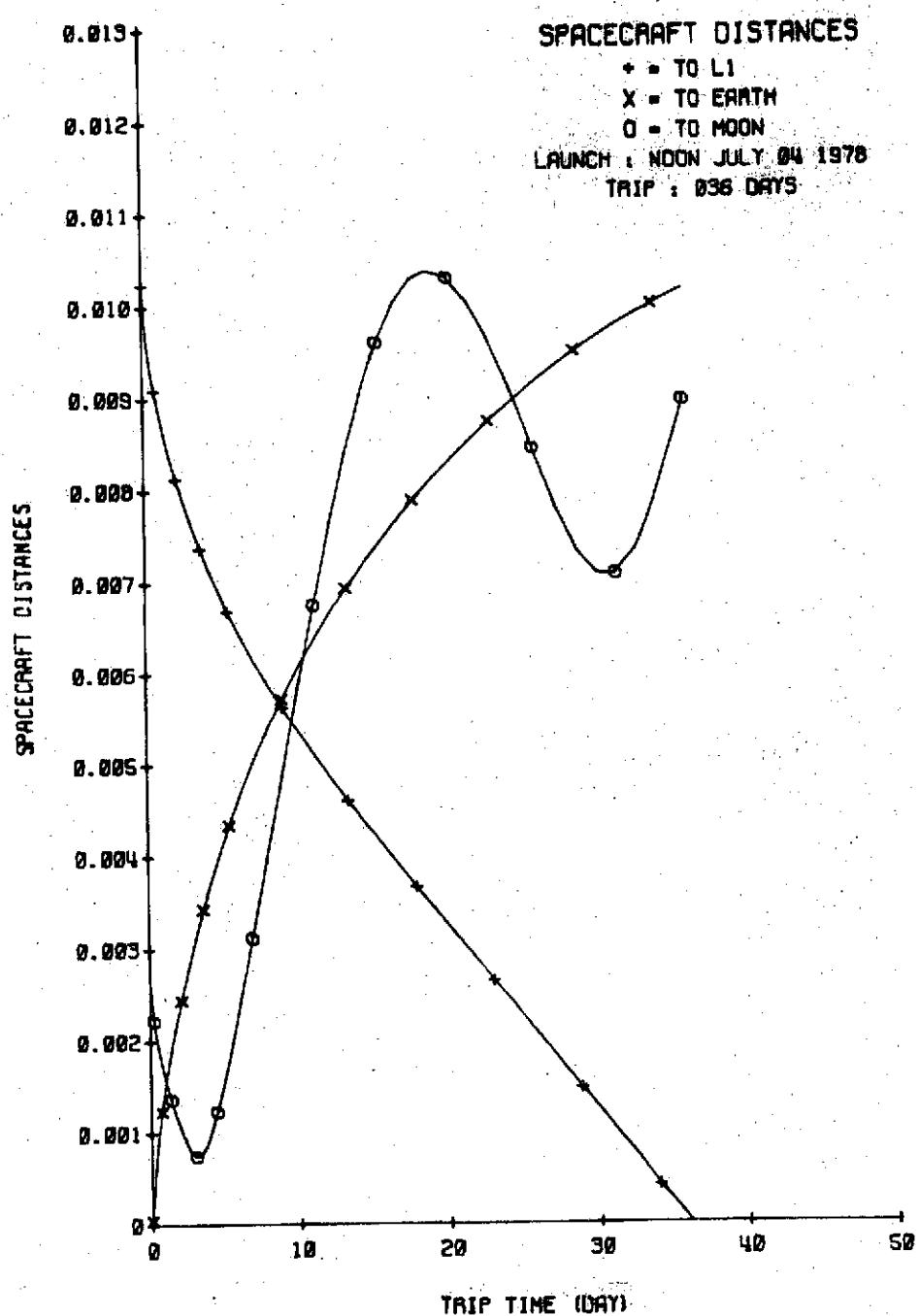


Figure 2e 2-Impulse Transfer (Example 1)

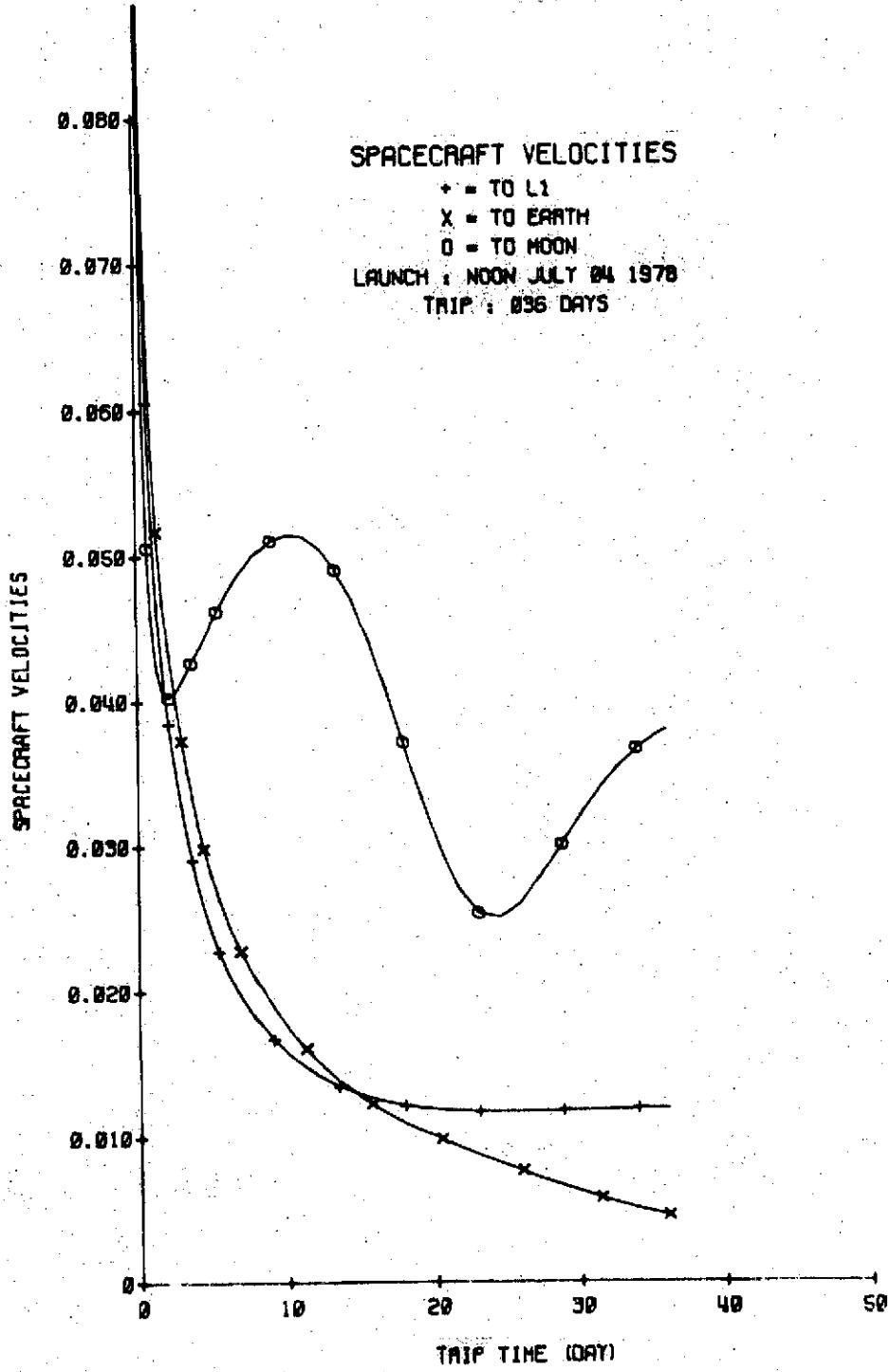


Figure 2f 2-Impulse Transfer (Example 1)

PRIME VECTOR MAGNITUDE

LAUNCH : NOON JULY 04 1978

TRIP : 036 DAYS

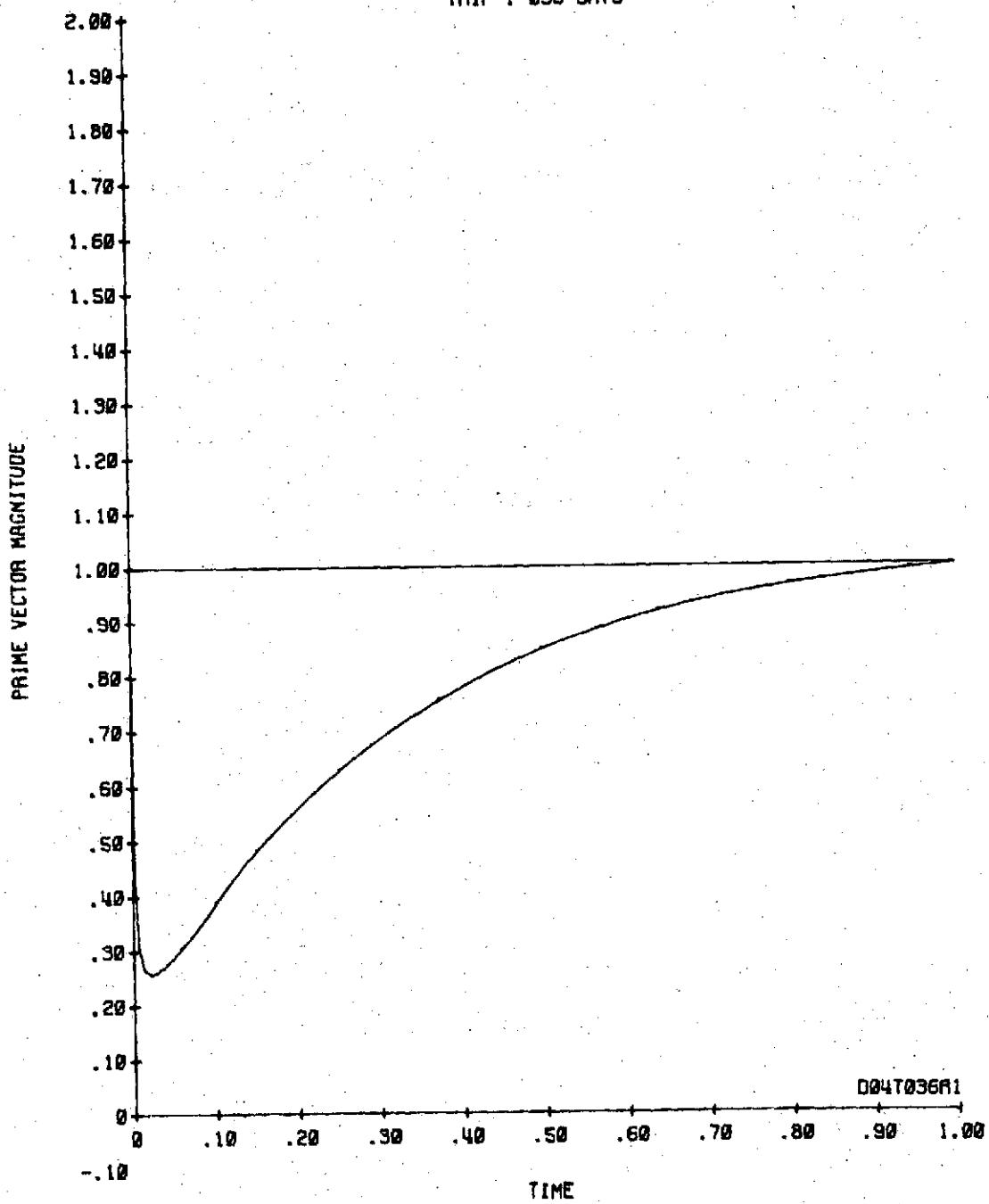


Figure 2g 2-Impulse Transfer (Example 1)

## EXAMPLE 2

### A. Purpose

This example may be used to check out Program EXLAM and associated subroutines. It is a 4-body transfer from noon July 4, 1978 from a given position at earth to a given point in space in 36 days.

### B. Input Parameters

\* Same as in Ex. 1

<u>Card No.</u>	<u>Format</u>	<u>Parameter</u>	<u>Value</u>
1	4D20.11	GL1	*
		AUM	*
		UTIME	*
		UVELM	*
2	3D20.11	MS	*
		ME	*
		MM	*
3	4I5	IMODE	2
		ITLMAX	50
		IPTJX	0
		IFILEX	0
4	4D20.11	RSE0(1)	1.98930091D-01
		(2)	-9.97050589850D-01
		(3)	6.79027012471D-05
		VSE0(1)	9.64906589348D-01
5	4D20.11	(2)	1.92157060597D-01
		(3)	-1.47749626270D-05

		RSM0(1)	1.99125783494D-01
		(2)	-9.94358817445D-01
6	4D20.11	(3)	-1.68002571823D-04
		VSM0(1)	9.32348120275D-01
		(2)	1.95028878329D-01
		(3)	-2.62545160637D-04
7	3D20.11	TDAY0	1.099D+03
		TRIPD	3.6D+01
		ERRMXM	1.524D+02
8	4D20.11	RSVTAR	7.17957115972D-01
			-7.01342803746D-01
			4.27257573439D-05
		ERRMIN	1.0D-10
9	1D20.11	KNR	1.0D+00
10	4D20.11	REV0(1)	3.55098760149D-05
		(2)	-2.56858251705D-05
		(3)	-2.05123643240D-06
		VEVOP(1)	2.16833393469D-01
11	2D20.11	(2)	2.97557757082D-01
		(3)	2.76469306727D-02

C. Output Parameters

A printout of Lambert iterations is submitted with this guide in a separate package. The initial state vector is:

RSVO(1)	1.98965600875D-01
(2)	-9.97076275675D-01
(3)	6.58514648147D-05
VSVI(1)	1.18173998282D+00
(2)	4.89714817679D-01
(3)	2.78321557101D-02

The iteration history is as follows:

<u>ITER</u>	<u>Error( ψ )</u>
1	3.9725 D-05 Initial miss
2	1.6349D-04
3	3.4139D-05
4	2.0172D-05
5	1.7986D-05
6	1.6351D-05
7	9.6429D-09
8	6.1105D-12 < ERRMIN

The converged solution is

VSVI(1)	1.18164961297D+00
(2)	4.89491098961D-01
(3)	3.06148929077D-02

### EXAMPLE 3

#### A. Purpose

This example may be used to check out Program ETP2I and associated subroutines. It is a 4-body transfer from noon July 4, 1978 to L<sub>1</sub> in 44 days. The earth parking orbit has an inclination of 28.5 deg.

#### B. Output Parameters

- \* Same as in Ex. 1
- \*\* Same as in Ex. 2

<u>Card No.</u>	<u>Format</u>	<u>Parameter</u>	<u>Value</u>
1	4D20.11	GL1	*
		AUM	*
		UTIME	*
		UVELM	*
2	3D20.11	MS	*
		ME	*
		MM	*
3	4D20.11	REVMAG	*
		OINCD	*
		OBLD	*
		ERRMXM	*
4	2D20.11	TDAYO	*
		TTRIPD	4.40D+01
5	3D20.11	VEVMAG	3.69195894918D-01
		LOND	3.40D+02
		THED	0. D+00

6	4D20.11	RSE0(1)	*
		(2)	*
		(3)	*
		VSE0(1)	*
7	4D20.11	(2)	*
		(3)	*
		RSM0(1)	*
		(2)	*
8	4D20.11	(3)	*
		VSM0(1)	*
		(2)	*
		(3)	*
9	4D20.11	EPS	1.0D-11
		EPSTSI	1.0D-10
		KDX	1.0D+00
		EPSV	1.0D-03
10	14	ICOMV	1
		ITERMX	50
		IFILEX	0
		ITAR	0
11	3D20.11	AYM	0
		AZM	0
		ATARD	0

C. Output Parameters

The state vector at the terminal time is:

RSV(1)	8.04147100281D-01
(2)	-5.98272665021D=01
(3)	3.54443603861D-05
VSV(1)	5.80886320061D-01
(2)	8.02081814322D-01
(3)	-4.43809910137D-04

The converged initial conditions are:

VEVMAG	10997.18 m/s
LOND	358.32 deg
THED	-23.43 deg

The costs are:

$ \Delta V_o $	3204.20 m/s
$ \Delta V_f $	377.80 m/s
	3582.00

Ref. 2 indicates that  $|\Delta V_f|$  is 263.31 m/s for the 44 day transfer without the inclination angle constraint.

A printout of the iterations together with the trajectory at each time step is submitted in a separate package.

The trajectory is shown in Figure 3a to 3f. The primer vector history is shown in Figure 3g.

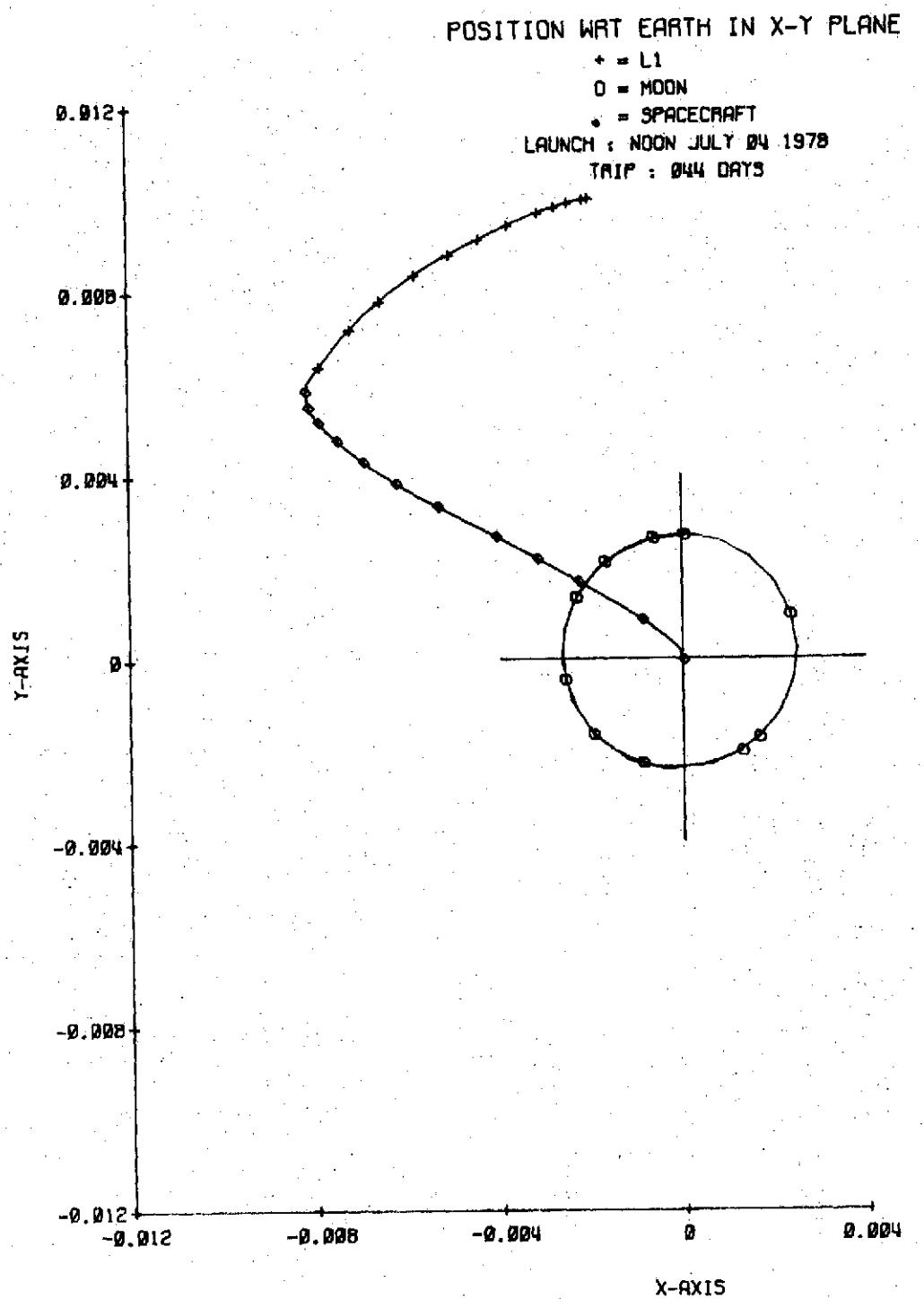


Figure 3a 2-Impulse Transfer (Example 3)

POSITION WRT MOON IN X-Y PLANE

X = EARTH

• = SPACECRAFT

LAUNCH : NOON JULY 94 1978

TRIP : 844 DAYS

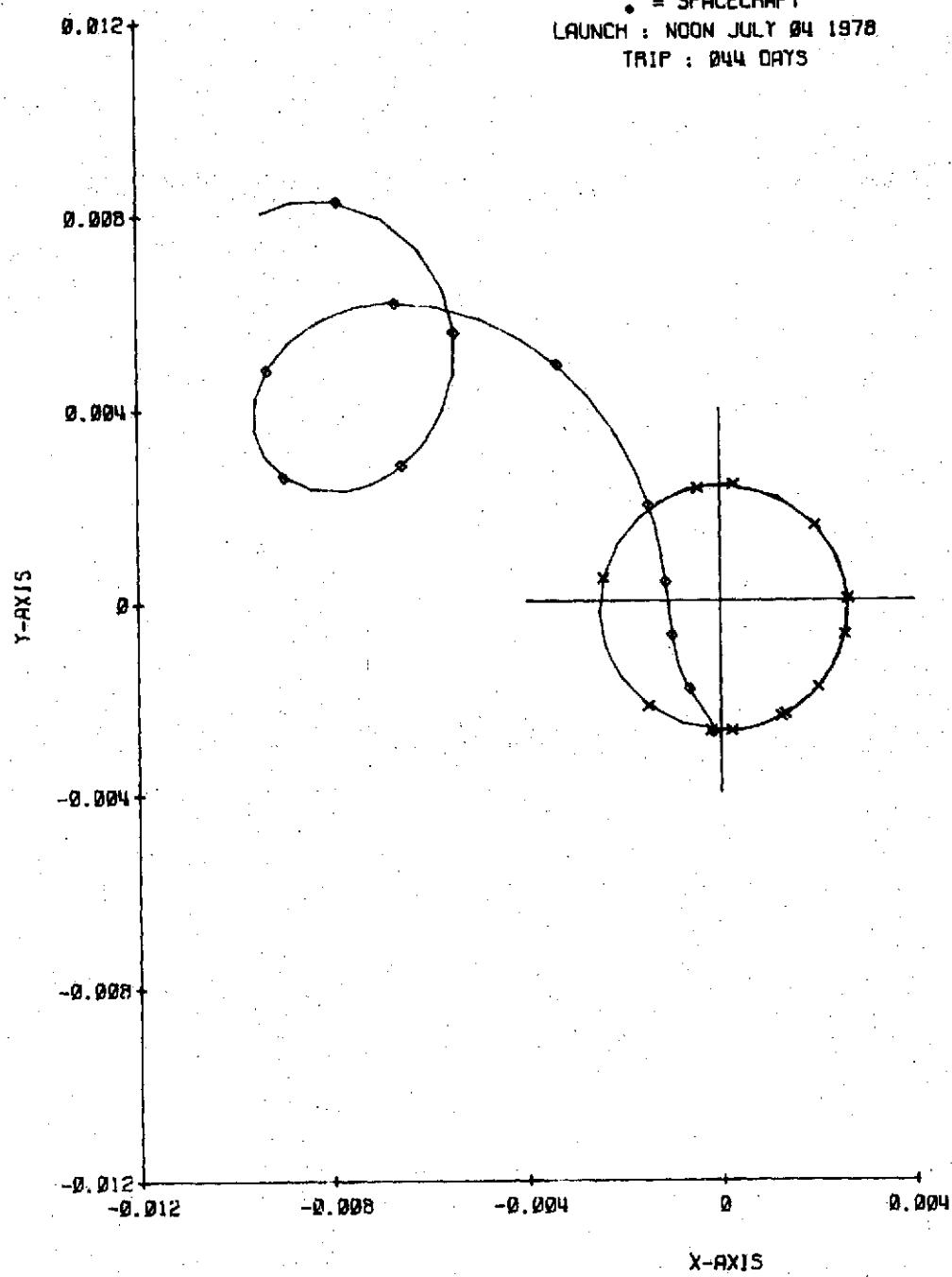


Figure 3b 2-Impulse Transfer (Example 3)

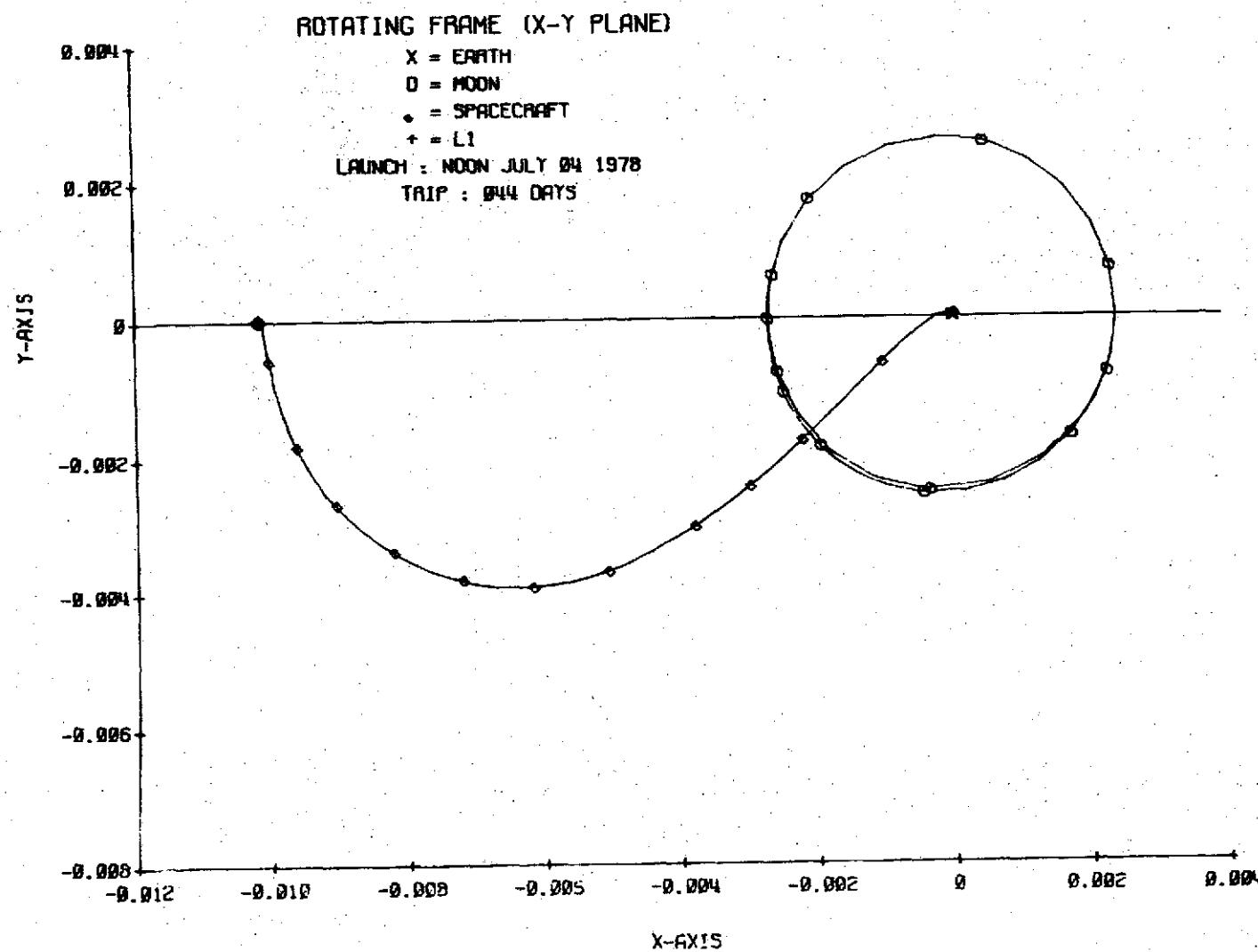


Figure 3c 2-Impulse Transfer (Example 3).

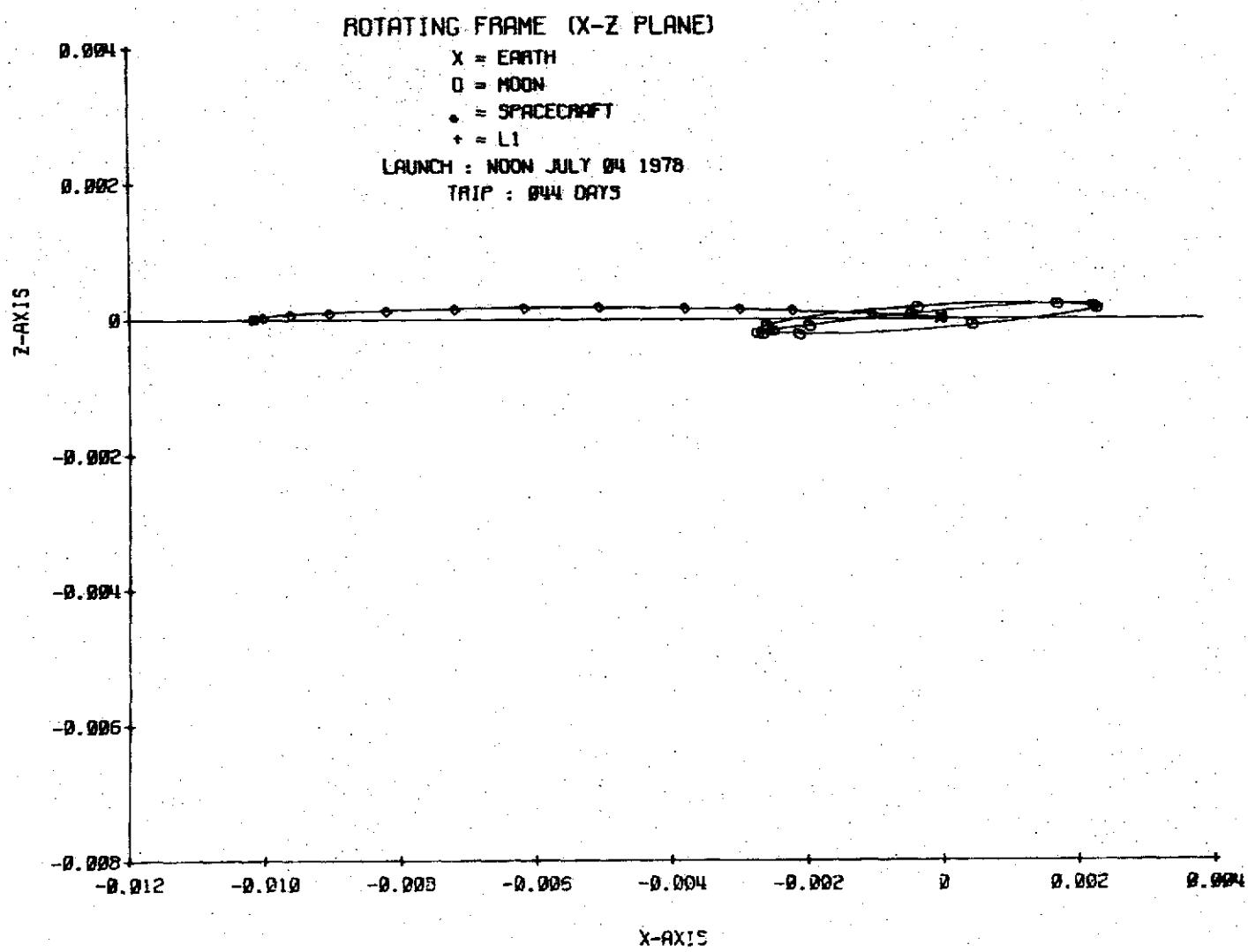


Figure 3d 2-Impulse Transfer (Example 3)

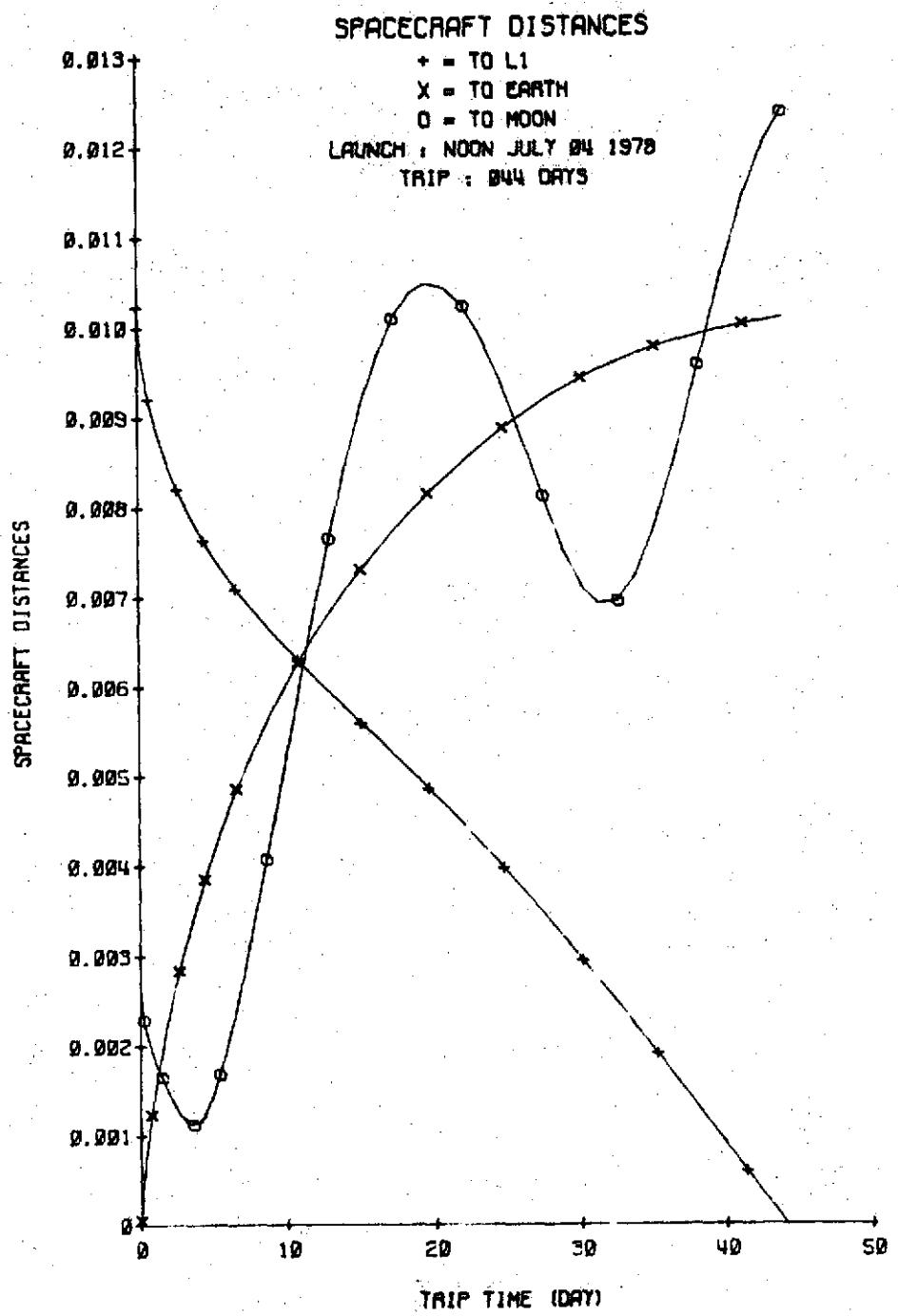


Figure 3e 2-Impulse Transfer (Example 3)

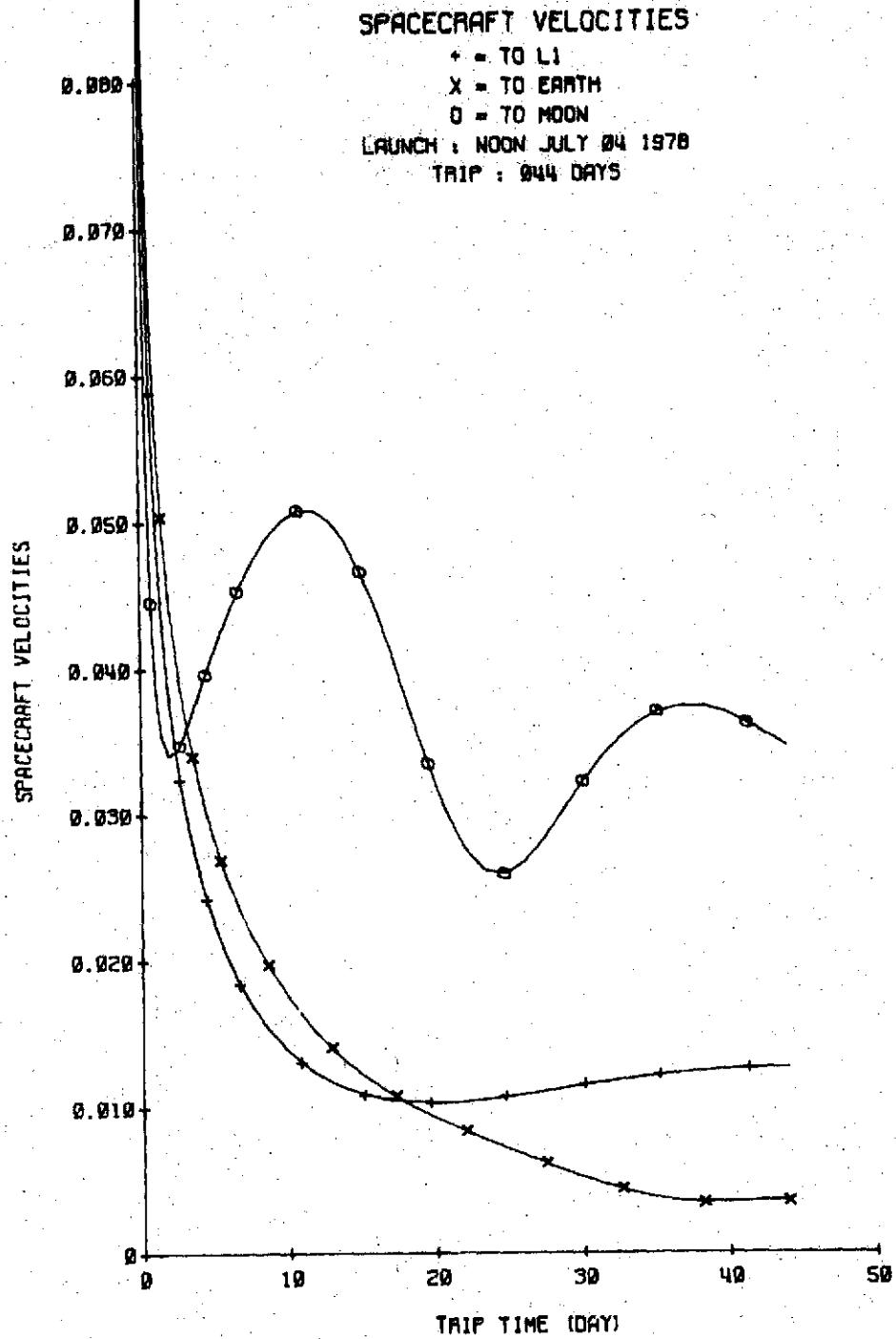


Figure 3f 2-Impulse Transfer (Example 3)

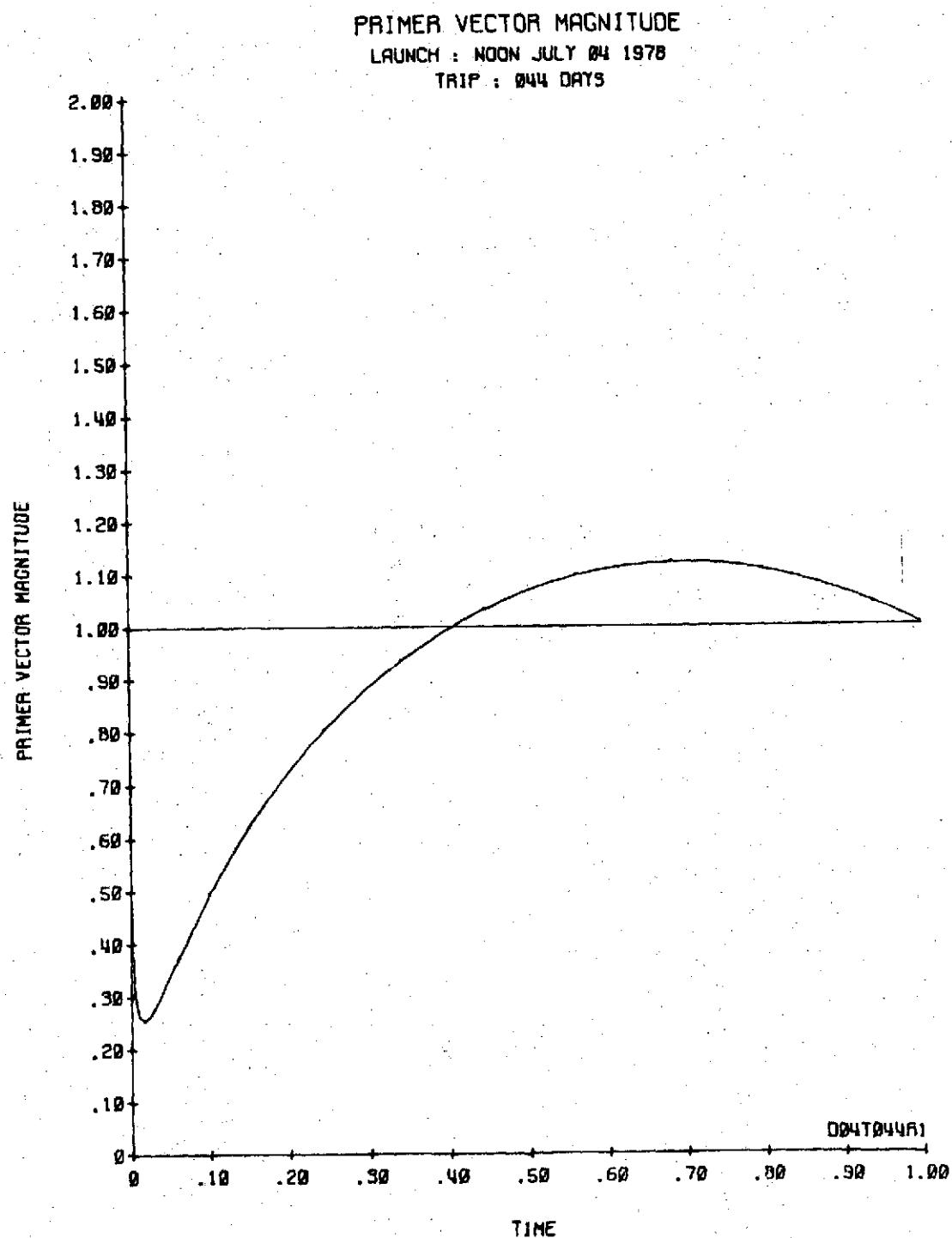


Figure 3g 2-Impulse Transfer (Example 3)

## EXAMPLE 4

### A. Purpose

This example may be used to check out Program PTP3I and associated subroutines. It is a 4-body 3-impulse transfer from noon July 4, 1978 to L<sub>1</sub> in 44-days. The 2-impulse transfer shown in Ex. 3 was used as the reference.

### B. Input Parameters

\* Same as in Ex. 1.

The starting independent variables ( $\bar{v}_o$ ,  $t_m$ ) shown here are values near the end of a sequence of computer runs.

<u>Card No.</u>	<u>Format</u>	<u>Parameter</u>	<u>Value</u>
1	4D20.11	GL1	*
		AUM	*
		UTIME	*
2	3D20.11	UVELM	*
		MS	*
		ME	*
3	3D20.11	MM	*
		TSTART	1.89051337719D+01
		TM	1.96168629221D+01
4	4D20.11	TEND	1.96620272076D+01
		RSE0(1)	*
		(2)	*
5	4D20.11	(3)	*
		VSE0(1)	*
		(2)	*
		(3)	*

		RSM0(1)	*
		(2)	*
6	4D20.11	(3)	*
		VSM0(1)	*
		(2)	*
		(3)	*
7	4D20.11	RSV0(1)	1.98969880525D-01
		(2)	-9.97069044391D-01
		(3)	6.68331499258D-05
		VSV0(1)	1.07508453453D+00
8	2D20.11	(2)	4.284116257881D-01
		(3)	2.23856828208D-02
9	4D20.11	VSVI(1)	1.12559555237D+00
		(2)	5.23005315320D-01
		(3)	3.22363348080D-02
		VSVMP(1)	6.12270768134D-01
10	2D20.11	(2)	7.70222061894D-01
		(3)	-3.40110040616D-04
11	4D20.11	RSVTAR(1)	8.04147100222D-01
		(2)	-5.98272665036D-01
		(3)	3.54443659015D-05
		VSVTAR(1)	5.74883737675D-01
12.	2D20.11	(2)	7.90914481955D-01
		(3)	-5.54211553533D-05

13	3D20.11	KNR	1.0D+00
		ERRMIN	1.0D-10
		ERRMXM	1.524D+02
14	3D20.11	FMINM	3.4D+03
		EPS	1.0D-02
		EPSV	1.0D-04
15	15	ICOMV	0
		ITLMAX	100
		ILINC	2
		ITDMAX	100
		IFILEX	0
16	4D20.11	V(1, 1)	1.50704497134D-04
		V(1, 2)	1.08127195736D-04
		V(1, 3)	-1.88527012972D-03
		V(1, 4)	-1.33164676422D-01
17	4D20.11	V(2, 1) = V(1, 2)	
		V(2, 2)	-1.72891113995D-04
		V(2, 3)	1.25136470933D-03
		V(2, 4)	1.00119585112D-01
18	4D20.11	V(3, 1) = V(1, 3)	
		V(3, 2) = V(2, 3)	
		V(3, 3)	-3.48824401009D-03
		V(3, 4)	-3.68585896226D-01

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4D20.11

$$V(4, 1) = V(1, 4)$$

$$V(4, 2) = V(2, 4)$$

$$V(4, 3) = V(3, 4)$$

$$V(4, 4) = -3.32401335566D+01$$

### C. Output Parameters

The trajectory is shown in Figure 4a to 4f. The primer vector history is shown in Figure 4g. The interior impulse applied at about 41.9 days is nearly at the end of the 44-day transfer. The costs are

Initial impulse	3207.35 m/s
Interior impulse	273.44 m/s
Terminal impulse	<u>97.64</u>
	3578.43

The 3-Impulse transfer costs about 3.50 m/s less than the 2-Impulse transfer.

### D. Comment

The 3-impulse transfer is difficult to generate, especially when the 2-impulse transfer is nearly optimal. First, the difficulty is to break away from the 2-impulse transfer. Secondly, the cost gradient must be reduced several orders of magnitude lower than necessary in order to satisfy the condition

$$\dot{\lambda}_m^+ \cdot \bar{\lambda}_m \approx \dot{\lambda}_m^- \cdot \bar{\lambda}_m$$

while the cost remains practically unchanged. To accomplish this it may be necessary to reduce the single step allowable position error by an order of magnitude.

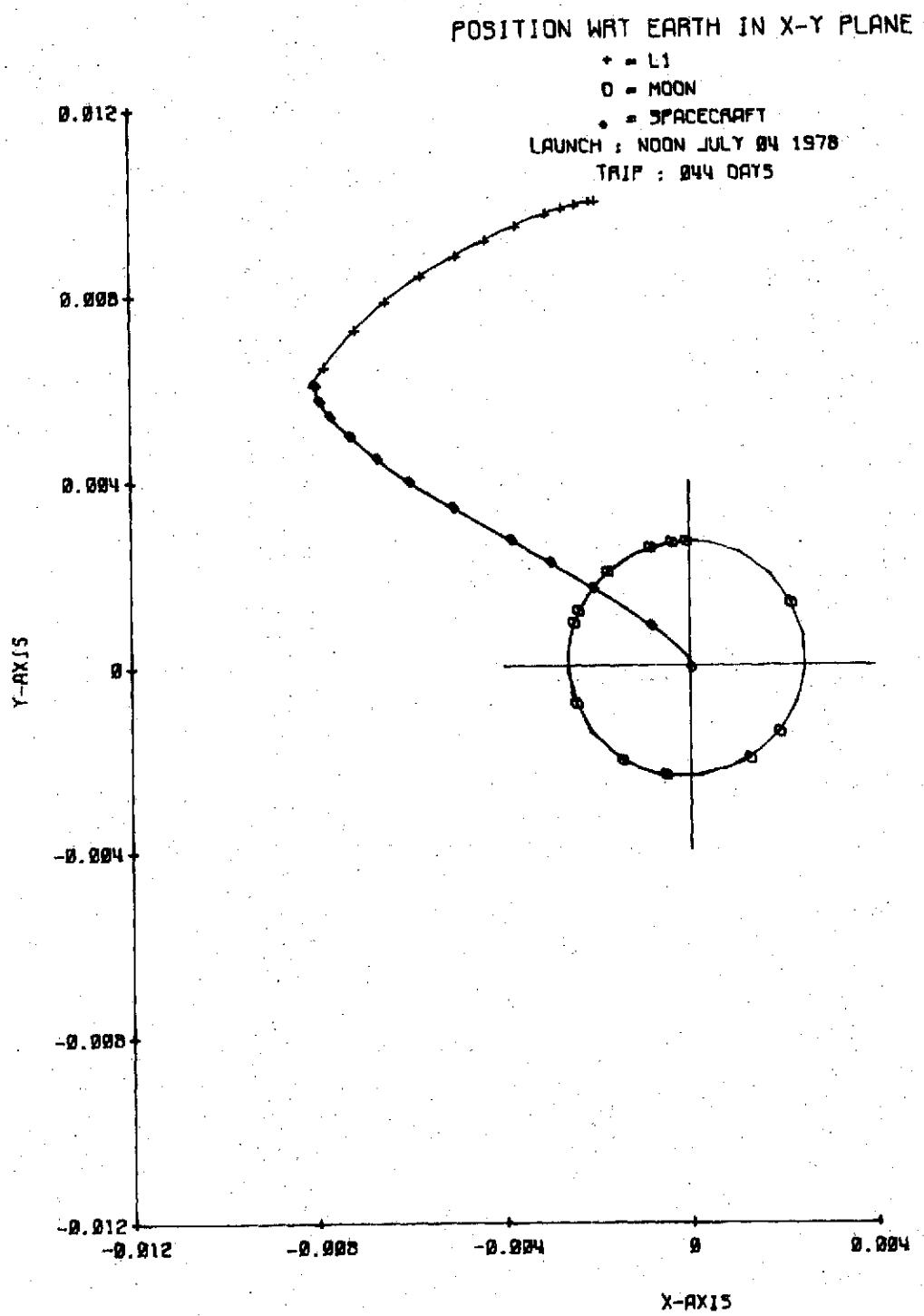


Figure 4a 3-Impulse Transfer (Example 4)

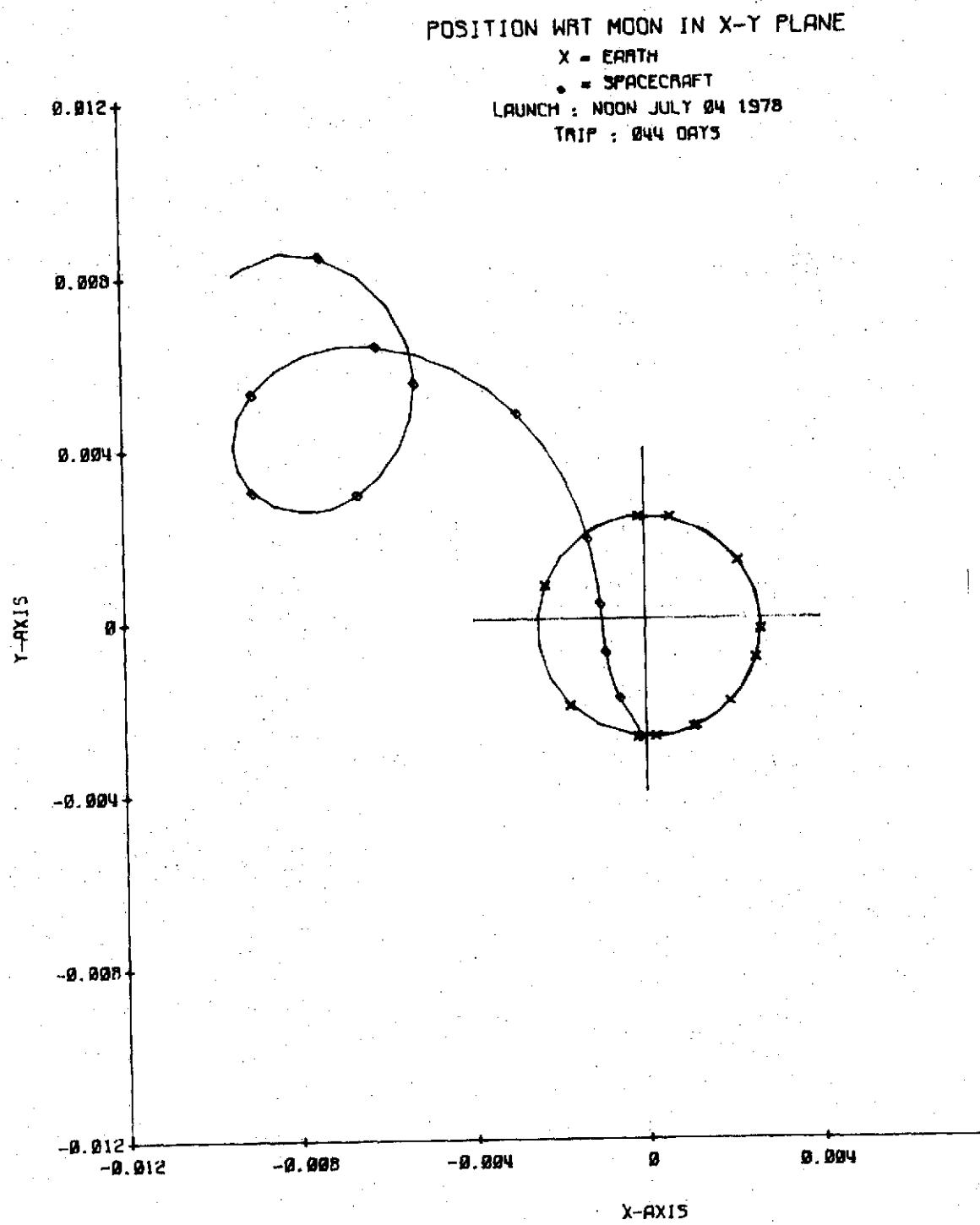


Figure 4b 3-Impulse Transfer (Example 4)

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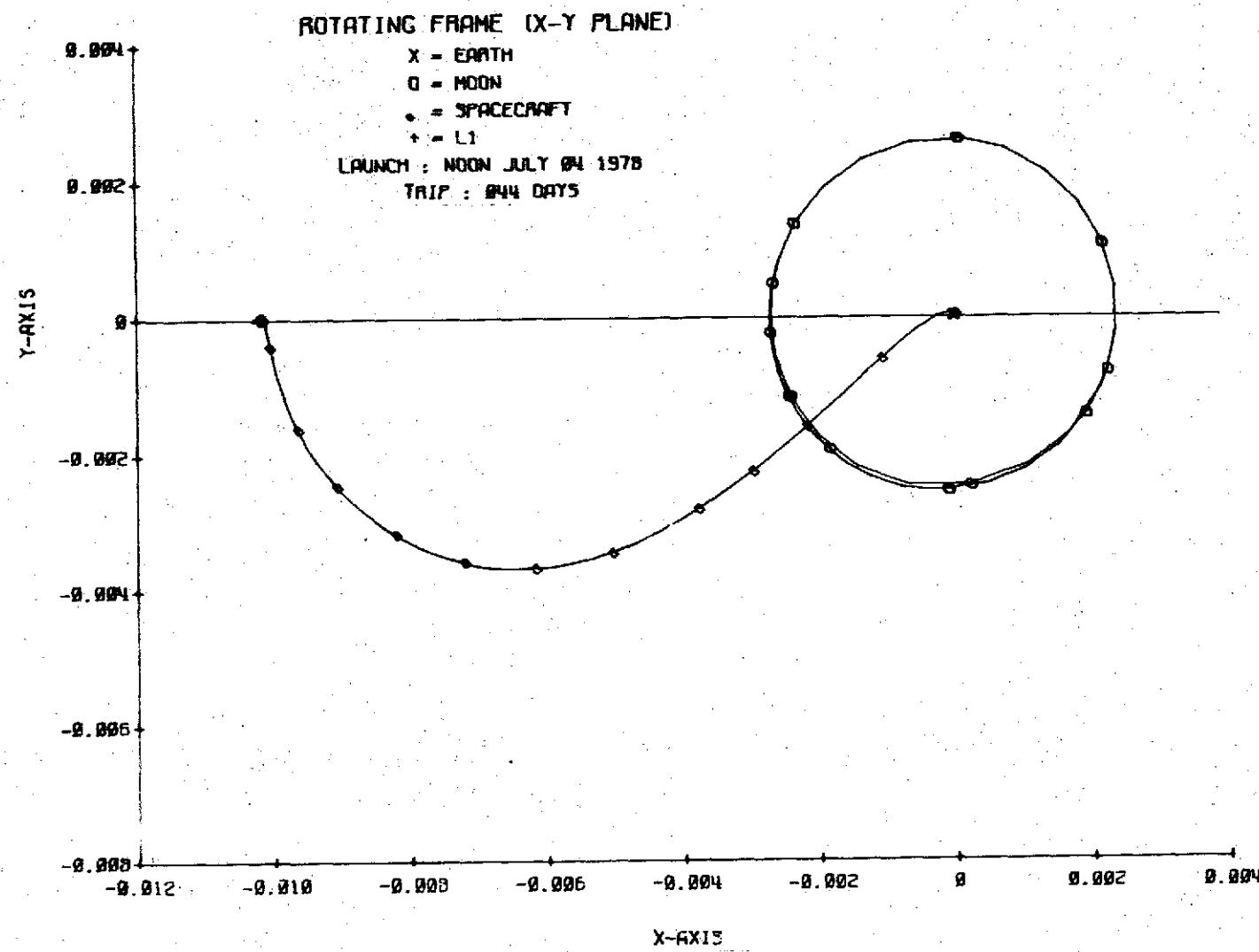


Figure 4c 3-Impulse Transfer (Example 4)

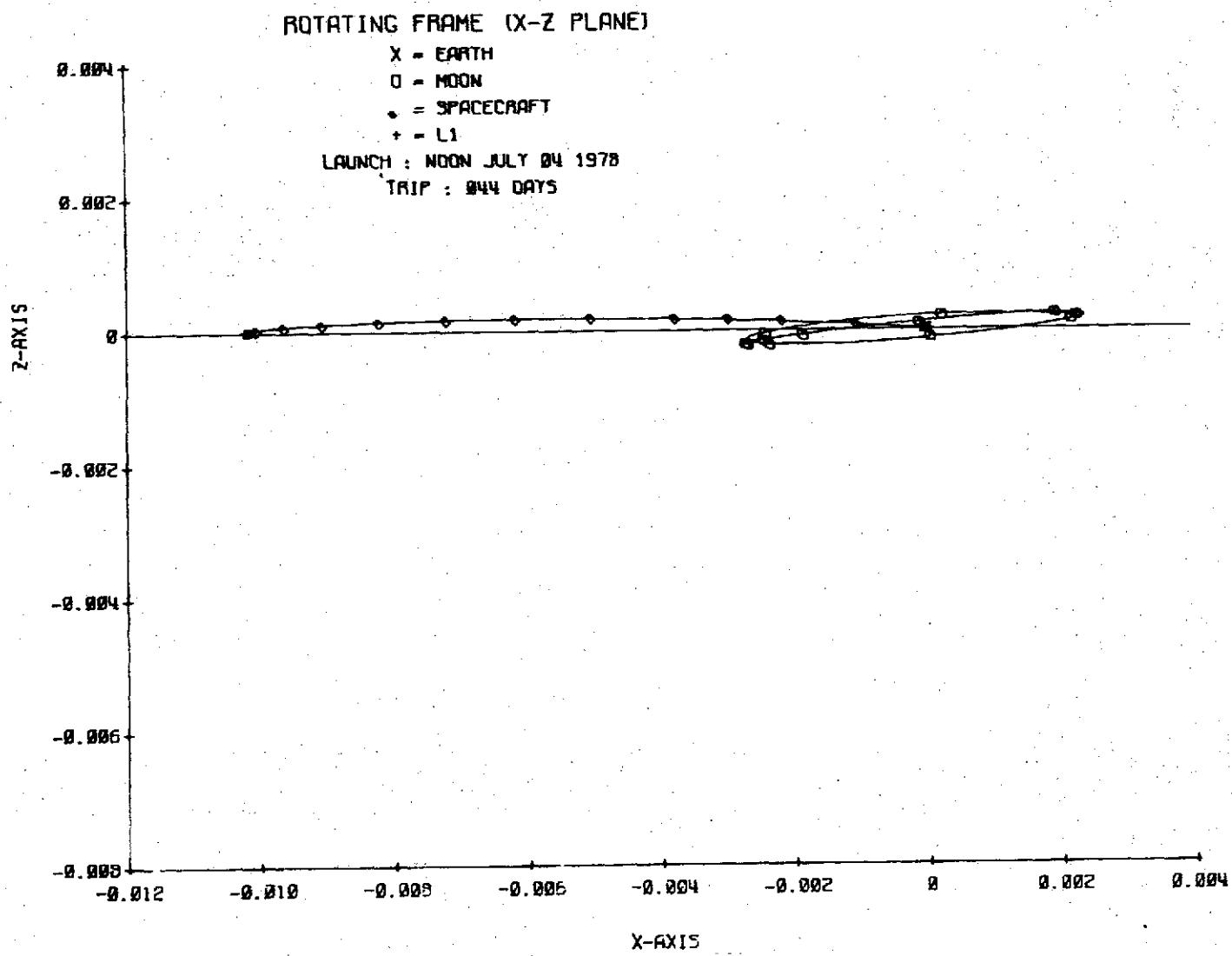


Figure 4d 3-Impulse Transfer (Example 4)

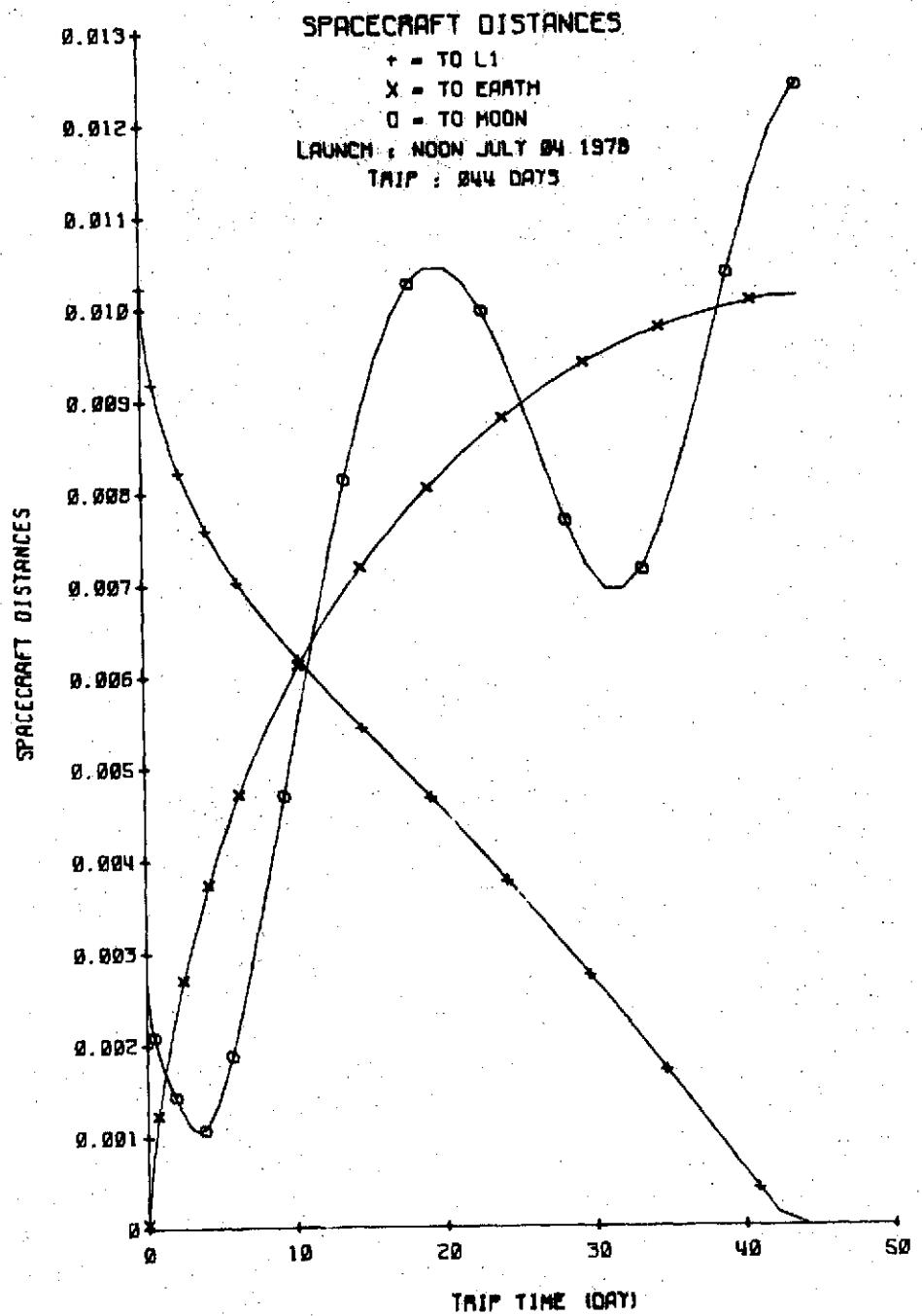


Figure 4e 3-Impulse Transfer (Example 4)

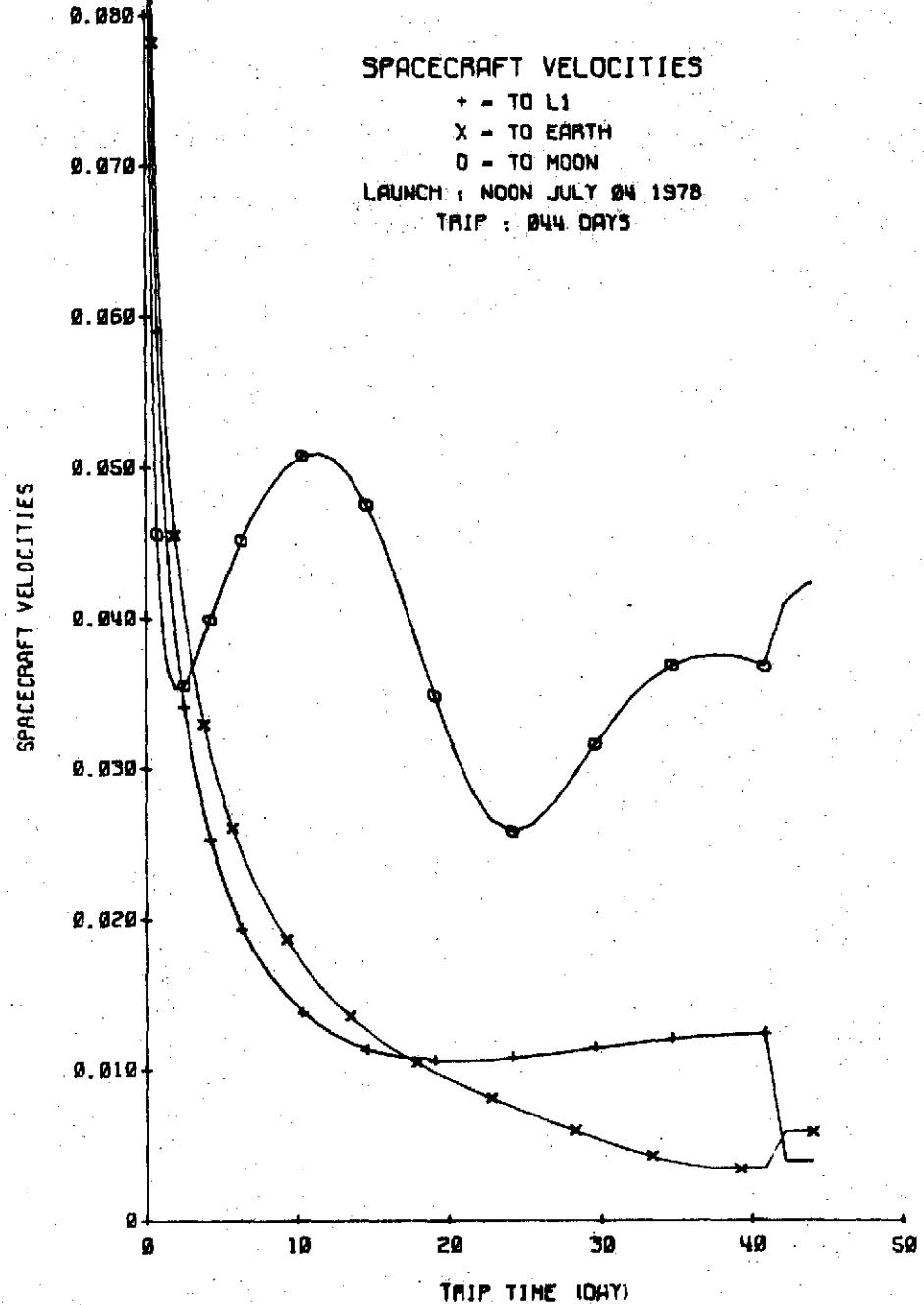


Figure 4f 3-Impulse Transfer (Example 4)

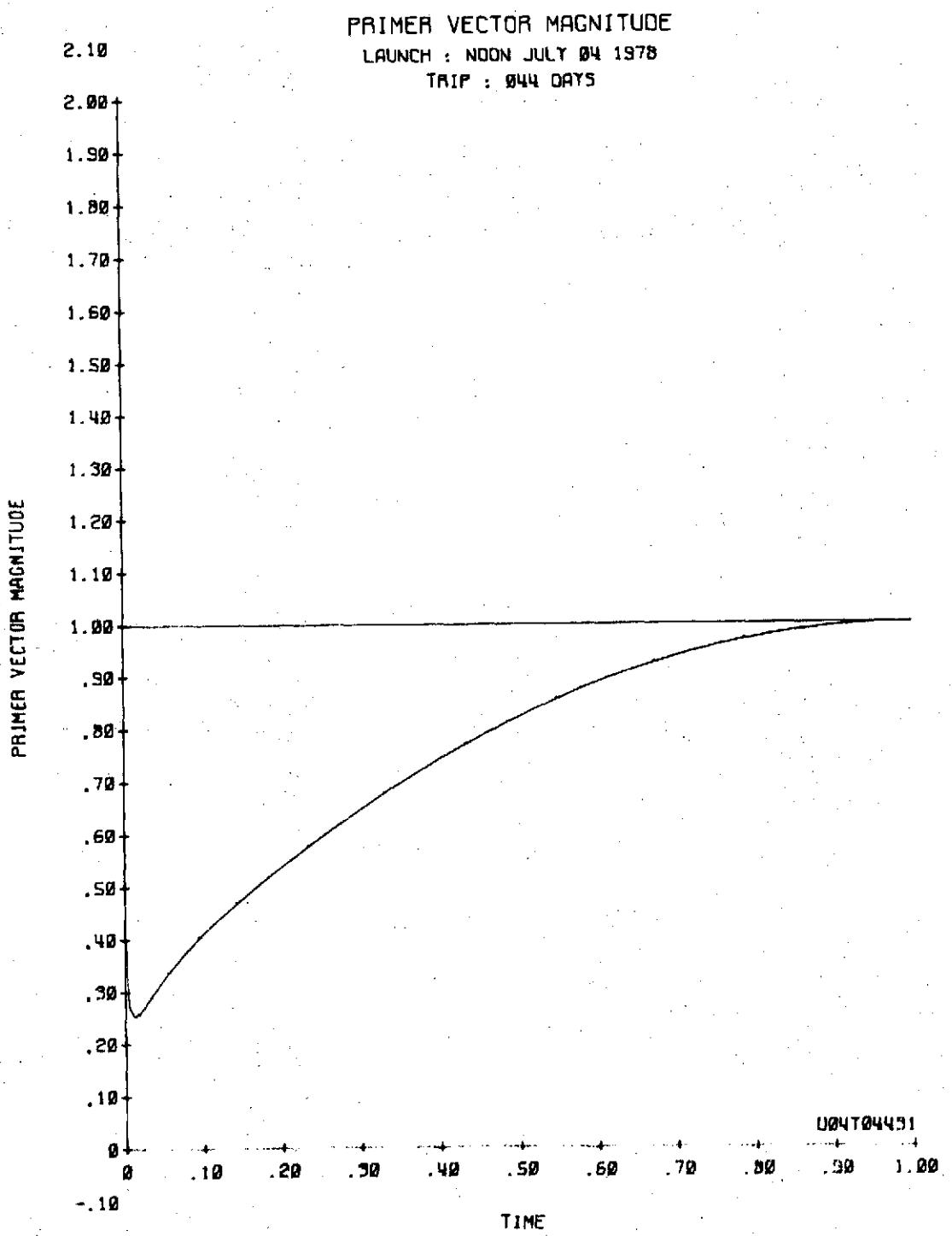


Figure 4g 3-Impulse Transfer (Example 4)

**PROGRAM AND SUBROUTINE LISTING**

TRAJ	LAMB
TRAJ3	LAMB3
EXLAM	DISP
EXLAM3	DISP3
ETP2I	PTRAJ
ETP2I3	PTRAJ3
PTP3I	FDATA
PTP3I3	FDATA3
FOURBY	COMAUG
THRBDY	COMDX
TWOBDY	UPX
CSTEP	PVEC
CSTEP3	RVEMV
DELRV	MXV
DELRV3	VVT
COMIC	DOT
COMIC3	VMAG
COMFG	INVERT
COMFG3	UNITV
COMF	VXV
COMF3	MTRANS
COMG	MXM
CTAR	
CTAR3	

C PROGRAM TRAJ  
 C PROGRAM PROPAGATES GIVEN STATES FROM TSTART TO TEND  
 IMPLICIT REAL\*8(A-H,L-M,D-Z)  
 DIMENSION RSEO(3),VSEO(3),RSMO(3),VSMO(3),REVO(3),VEVO(3),  
 1RSVO(3),VSVO(3),VSVI(3),VEVOP(3),PVO(6),RSVF(3),VSVF(3),RSEF(3),  
 2VSF(3),RSMF(3),VSMF(3),S11(3,3),S12(3,3),S21(3,3),S22(3,3)  
 COMMON/CONST/MS,ME,MM,GL1,AUM,UTIME,UVELM,ERRMAX,DTR  
 COMMON/FLAG/IMTX,IPV,IPTRAJ,IPVTM,IFILE,ITER,ITAR  
 READ(5,100)GL1,AUM,UTIME,UVELM  
 READ(5,100)MS,ME,MM  
 READ(5,101)IMODE,IPV,IPTRAJ,IFILE  
 READ(5,100)RSEO,VSEO,RSMO,VSMO  
 READ(5,100)TDAY0,TRIPD,ERRMXM  
 DTR=1.7453292519943296D-2  
 ERRMAX=ERRMXM/AUM  
 TDAYF=TDAY0+TRIPD  
 TSTART=TDAY0/UTIME  
 TEND=TDAYF/UTIME  
 IMTX=0  
 IPVTM=0  
 ITER=0  
 WRITE(6,102)GL1,AUM,UTIME,UVELM,ERRMXM,ERRMAX,MS,ME,MM  
 WRITE(6,103)TDAY0,TRIPD,TDAYF,TSTART,TEND  
 WRITE(6,105)RSEO,VSEO,RSMO,VSMO  
 GO TO 1,2,3,IMODE  
 1 READ(5,100)REVMAG,VEVMAG,OINCD,OBLD,LOND,THED  
 OINC=DTR\*DINCD  
 OBL=DTR\*OBLD  
 LON=DTR\*LOND  
 THE=DTR\*THED  
 CALL COMIC(REVMAG,VEVMAG,LON,THE,OINC,OBL,RSEO,VSEO,  
 1REVO,VEVO,RSVO,VSVO,VSVI)  
 WRITE(6,106)REVMAG,VEVMAG,OINCD,OBLD,LOND,THED  
 GO TO 6  
 2 READ(5,100)REVO,VEVOP  
 DO 201 I=1,3  
 RSVO(I)=RSEO(I)+REVO(I)  
 201 VSVI(I)=VSEO(I)+VEVOP(I)  
 WRITE(6,107)REVO,VEVOP  
 GO TO 6  
 3 READ(5,100)RSVO,VSVI  
 6 WRITE(6,108)RSVO,VSVI  
 IF(IPV.EQ.0) GO TO 7  
 READ(5,100)PVO  
 IMTX=1  
 IPVTM=1  
 WRITE(6,109)PVO  
 7 WRITE(6,104)IMODE,IPTRAJ,IFILE,IMTX,IPV,IPVTM  
 CALL FOURBY(TSTART,TEND,RSVO,VSVI,RSEO,VSEO,RSMO,VSMO,  
 1PVO,RSVF,VSVF,RSEF,VSEF,RSMF,VSMF,S11,S12,S21,S22)  
 WRITE(6,110)RSVF,VSVF,RSEF,VSEF,RSMF,VSMF  
 100 FORMAT(4D20.11)  
 101 FORMAT(4I5)  
 102 FORMAT(1H ,40X,'FOUR-BODY TRAJECTORY'/1H0,T8,'GL1',T28,'AUM',  
 1T48,'UTIME',T68,'UVELM',T88,'ERRMXM',T108,'ERRMAX'/1H ,  
 21P6D20.11/1H ,T8,'MS',T28,'ME',T48,'MM'/1H ,1P3D20.11)  
 103 FORMAT(1H0,T8,'TDAY0',T28,'TRIPD',T48,'TDAYF',T68,'TSTART',

```
1T88,'TEND'/1H ,1P5D20.11)
104 FORMAT(1HO,T8,'IMODE',T28,'IPTRAJ',T48,'IFILE',T68,'IMTX',T88,
1'IPV',T108,'IPVTM!/1H ,I10,5I20)
5 FORMAT(1HO,T8,'RSE0',T68,'VSE0'/1H ,1P6D20.11/1H ,T8,'RSM0',
1T68,'VSM0'/1H ,1P6D20.11)
106 FORMAT(1HO,T8,'REVMAG',T28,'VEVMAG',T48,'OINCD',T68,'OBLD',
1T88,'LOND',T108,'THED'/1H ,1P6D20.11)
107 FORMAT(1HO,T8,'REVO',T68,'VEVOP'/1H ,1P6D20.11)
108 FORMAT(1HO,T8,'RSV0',T68,'VSVI'/1H ,1P6D20.11)
109 FORMAT(1HO,T8,'PVO'/1H ,1P6D20.11)
110 FORMAT(1HO,T8,'RSVF',T68,'VSVF'/1H ,1P6D20.11/1H ,T8,'RSEF',
1T68,'VSEF'/1H ,1P6D20.11/1H ,T8,'RSMF',T68,'VSMF'/1H ,1P6D20.11)
RETURN
END
```

```

C PROGRAM TRAJ3
C PROGRAM PROPAGATES GIVEN STATES FROM TSTART TO TEND IN
C EARTH-MOON-VEHICLE SPACE.
C IMPLICIT REAL*8(A-H,L-M,O-Z)
C DIMENSION REM0(3),VEM0(3),REVO(3),VEVO(3),VEVOP(3),REVF(3),
C 1VEVF(3),REMf(3),VEMf(3),S11(3,3),S12(3,3),S21(3,3),S22(3,3)
C COMMON/FLAG/IMTX,IPV,IPTRAJ,IPVTM,IFILE,ITER
C COMMON/CONST3/ME,MM,GAMMA,UDM,UTIME,UVELM,ERRMAX,DTR
C READ(5,100)GAMMA,UDM,UTIME,UVELM
C READ(5,100)ME,MM
C READ(5,101)IMODE,IPV,IPTRAJ,IFILE
C READ(5,100)REM0,VEM0
C READ(5,100)TDAY0,TRIPD,ERRMXM
C DTR=1.7453292519943296D-2
C ERRMAX=ERRMXM/UDM
C TDAYF=TDAY0+TRIPD
C TSTART=TDAY0/UTIME
C TEND=TDAYF/UTIME
C IMTX=0
C IPVTM=0
C ITER=0
C WRITE(6,102)GAMMA,UDM,UTIME,UVELM,ERRMXM,ERRMAX,ME,MM
C WRITE(6,103)TDAY0,TRIPD,TDAYF,TSTART,TEND
C WRITE(6,105)REM0,VEM0
C GO TO (1,2),IMODE
1 READ(5,100)REVMAG,VEVMAG,OINCD,LOND,THED
C OINC=DTR*OINCD
C LON=DTR*LOND
C THE=DTR*THED
C CALL COMIC3(REVMAG,VEVMAG,LON,THE,OINC,REVO,VEVO,VEVOP)
C WRITE(6,106)REVMAG,VEVMAG,OINCD,LOND,THED
C GO TO 3
2 READ(5,100)REVO,VEVOP
3 WRITE(6,107)REVO,VEVOP
C IF(IPV.EQ.0) GO TO 4
C READ(5,100)PVO
C IMTX=1
C IPVTM=1
C WRITE(6,108)PVO
4 WRITE(6,104)IMODE,IPTRAJ,IFILE,IMTX,IPV,IPVTM
C CALL THRBDY(TSTART,TEND,REVO,VEVOP,REM0,VEM0,PVO,REVF,VEVF,
C 1REMf,VEMf,S11,S12,S21,S22)
C WRITE(6,109)REVF,VEVF,REMf,VEMf
100 FORMAT(4D20.11)
101 FORMAT(4I5)
102 FORMAT(1H ,40X,'THREE-BODY TRAJECTORY'/1H0,T8,'GAMMA',T28,
C 1'UDM',T48,'UTIME',T68,'UVELM',T88,'ERRMXM',T108,'ERRMAX'/1H ,
C 21P6D20.11/1H ,T8,'ME',T28,'MM'/1H ,1P2D20.11)
103 FORMAT(1H0,T8,'TDAY0',T28,'TRIPD',T48,'TDAYF',T68,'TSTART',
C 1T88,'TEND'/1H ,1P5D20.11)
104 FORMAT(1H0,T8,'IMODE',T28,'IPTRAJ',T48,'IFILE',T68,'IMTX',
C 1T88,'IPV',T108,'IPVTM'/1H ,1I0,5I20)
105 FORMAT(1H0,T8,'REM0',T68,'VEM0'/1H ,1P6D20.11)
106 FORMAT(1H0,T8,'REVMAG',T28,'VEVMAG',T48,'OINCD',T68,'LOND',
C 1T88,'THED'/1H ,1P5D20.11)
107 FORMAT(1H0,T8,'REVO',T68,'VEVOP'/1H ,1P6D20.11)
108 FORMAT(1H0,T8,'PVO'/1H ,1P6D20.11)

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109. FORMAT(1H0,T8,'REVF',T68,'VEVF'/1H ,1P6D20.11/1H0,T8,'REMF',
1T68,'VEMF'/1H ,1P6D20.11)
RETURN
END
```

C PROGRAM EXLAM  
 C PROGRAM SOLVES 2-POINT BOUNDARY VALUE PROBLEM OF TRANSFER FROM  
 C A GIVEN INITIAL POSITION TO A GIVEN FINAL POSITION IN FIXED TIME.  
 IMPLICIT REAL\*8(A-H,K-M,O-Z)  
 DIMENSION RSEO(3),VSEO(3),RSMO(3),VSMO(3),REVO(3),VEVO(3),  
 1RSVO(3),VSVO(3),VSVI(3),VEVOP(3),RSVF(3),VSVF(3),RSEF(3),  
 2VSEF(3),RSMF(3),VSMF(3),S11(3,3),S12(3,3),S21(3,3),S22(3,3),  
 3RSVTAR(3),PVO(6)  
 COMMON/CONST/MS,ME,MM,GL1,AUM,UTIME,UVELM,ERRMAX,DTR  
 COMMON/FLAG/IMTX,IPV,IPTRAJ,IPVTM,IFILE,ITER,ITAR  
 READ(5,100)GL1,AUM,UTIME,UVELM  
 READ(5,100)MS,ME,MM  
 READ(5,101)IMODE,ITLMAX,IPTJX,IFILEX  
 READ(5,100)RSEO,VSEO,RSMO,VSMO  
 READ(5,100)TDAY0,TRIPD,ERRMXM  
 READ(5,100)RSVTAR,ERRMIN  
 READ(5,100)KNR  
 DTR=1.7453292519943296D-2  
 ERRMAX=ERRMXM/AUM  
 TDAYF=TDAY0+TRIPD  
 TSTART=TDAY0/UTIME  
 TEND=TDAYF/UTIME  
 IMTX=1  
 IPV=0  
 IPVTM=0  
 IPTRAJ=0  
 IFILE=0  
 WRITE(6,102)GL1,AUM,UTIME,UVELM,ERRMXM,ERRMAX,MS,ME,MM,ERRMIN,  
 1KNR  
 WRITE(6,103)TDAY0,TRIPD,TDAYF,TSTART,TEND  
 WRITE(6,104)IMODE,ITLMAX,IPTJX,IFILEX,IPTRAJ,IFILE  
 WRITE(6,105)RSEO,VSEO,RSMO,VSMO,RSVTAR  
 GO TO (1,2,3),IMODE  
 1 READ(5,100)REVMAG,VEVMAG,OINCD,OBLD,LOND,THED  
 OINC=DTR\*OINCD  
 OBL=DTR\*OBLD  
 LON=DTR\*LOND  
 THE=DTR\*THED  
 CALL COMIC(REVMAG,VEVMAG,LON,THE,OINC,OBL,VCIR,RSEO,VSEO,  
 1REVO,VEVO,RSVO,VSVO,VSVI)  
 WRITE(6,106)REVMAG,VEVMAG,OINCD,OBLD,LOND,THED  
 GO TO 6  
 2 READ(5,100)REVO,VEVOP  
 DO 201 I=1,3  
 RSVO(I)=RSEO(I)+REVO(I)  
 201 VSVI(I)=VSEO(I)+VEVOP(I)  
 WRITE(6,107)REVO,VEVOP  
 GO TO 6  
 3 READ(5,100)RSVO,VSVI  
 6 WRITE(6,108)RSVO,VSVI  
 CALL LAMB(TSTART,TEND,RSVO,VSVI,RSEO,VSEO,RSMO,VSMO,KNR,ITLMAX,  
 1ERRMIN,RSVTAR,RSVF,VSVF,RSEF,VSEF,RSMF,VSMF,S11,S12,S21,S22)  
 IPTRAJ=IPTJX  
 IFILE=IFILEX  
 IMTX=0  
 IF(IPTRAJ.GT.0) GO TO 7  
 IF(IFILE.GT.0) GO TO 7

GO TO 8

7 CALL FOURBY(TSTART,TEND,RSVO,VSVI,RSEO,VSEO,RSMO,VSMO,PVO,  
1RSVF,VSVF,RSEF,VSEF,RSMF,VSMF,S11,S12,S21,S22)

8 CONTINUE

100 FORMAT(4D20.11)

101 FORMAT(4I5)

102 FORMAT(1H ,40X,'FOUR-BODY LAMBERT PROBLEM'/1H0,T8,'GL1',T28,  
1'AUM',T48,'UTIME',T68,'UVELM',T88,'ERRMXM',T108,'ERRMAX'/1H ,  
2IP6D20.11/1H ,T8,'MS',,T28,'ME',T48,'MM',T68,'ERRMIN',T88,  
3'KNR'/1H ,1P5D20.11)

103 FORMAT(1H0,T8,'TDOY0',T28,'TRIPO',T48,'TDAYF',T68,'TSTART',  
1T88,'TEND'/1H ,1P5D20.11)

104 FORMAT(1H ,T8,'IMODE',T28,'ITLMAX',T48,'IPTJX',T68,'IFILEX',  
1T88,'IPTRAJ',T108,'FILE'/1H ,I10,5120)

105 FORMAT(1H0,T8,'RSEO',T68,'VSEO'/1H ,1P6D20.11/1H ,T8,'RSMO',  
1T68,'VSMO'/1H ,1P6D20.11/1H ,T8,'RSVTAR'/1H ,1P3D20.11)

106 FORMAT(1H0,T8,'REVMAG',T28,'VEVMAG',T48,'OINCD',T68,'DBLD',  
1T88,'LOND',T108,'THED'/1H ,1P6D20.11)

107 FORMAT(1H0,T8,'REVO',T68,'VEVOP'/1H ,1P6D20.11)

108 FORMAT(1H0,T8,'RSVO',T68,'VSVI'/1H ,1P6D20.11)

RETURN

END

PROGRAM EXLAM3  
 PROGRAM SOLVES 2-POINT BOUNDARY VALUE PROBLEM OF TRANSFER FROM  
 A GIVEN INITIAL POSITION TO A GIVEN FINAL POSITION IN FIXED  
 TIME.  
 IMPLICIT REAL\*8(A-H,K-M,O-Z)  
 DIMENSION REMO(3),VEMO(3),REVTAR(3),REVO(3),VEVO(3),VEVOP(3),  
 IREVF(3),VEVF(3),REMFI(3),VEMF(3),S11(3,3),S12(3,3),S21(3,3),  
 2S22(3,3),PVO(6)  
 COMMON/CONST3/ME,MM,GAMMA,UDM,UTIME,UVELM,ERRMAX,DTR  
 COMMON/FLAG/IMTX,IPV,IPTRAJ,IPVTM,IFILE,ITER,ITAR  
 READ(5,100)GAMMA,UDM,UTIME,UVELM  
 READ(5,100)ME,MM  
 READ(5,101)IMODE,ITLMAX,IPTJX,IFILEX  
 READ(5,100)REMO,VEMO  
 READ(5,100)TDAY0,TRIPD,ERRMXM  
 READ(5,100)REVTAR,ERRMIN  
 READ(5,100)KNR  
 DTR=1.7453292519943296D-2  
 ERRMAX=ERRMXM/UDM  
 TDAYF=TDAY0+TRIPD  
 TSTART=TDAY0/UTIME  
 TEND=TDAYF/UTIME  
 IMTX=1  
 IPV=0  
 IPVTM=0  
 IFILE=0  
 WRITE(6,102)GAMMA,UDM,UTIME,UVELM,ERRMXM,ERRMAX,ME,MM,ERRMIN,KNR  
 WRITE(6,103)TDAY0,TRIPD,TDAYF,TSTART,TEND  
 WRITE(6,104)IMODE,ITLMAX,IPTJX,IFILEX  
 WRITE(6,105)REMO,VEMO,REVTAR  
 GO TO (1,2),IMODE  
 1 READ(5,100)REVMAG,VEVMAG,OINCD,LOND,THED  
 OINC=DTR\*DINCD  
 LON=DTR\*LOND  
 THE=DTR\*THED  
 CALL COMIC3(REVMAG,VEVMAG,LON,THE,OINC,REVO,VEVO,VEVOP)  
 WRITE(6,106)REVMAG,VEVMAG,OINCD,LOND,THED  
 GO TO 3  
 2 READ(5,100)REVO,VEVOP  
 3 WRITE(6,107)REVO,VEVOP  
 CALL LAMB3(TSTART,TEND,REVO,VEVOP,REMO,VEMO,KNR,ITLMAX,ERRMIN,  
 1REVTAR,REVF,VEVF,REMFI,VEMF,S11,S12,S21,S22)  
 WRITE(6,108)REF,VVF,REMFI,VEMF  
 IPTRAJ=IPTJX  
 IFILE=IFILEX  
 IMTX=0  
 IF(IPTRAJ.EQ.0) GO TO 4  
 IF(IFILE.EQ.0) GO TO 4  
 GO TO 5  
 4 CALL THRBDY(TSTART,TEND,REVO,VEVOP,REMO,VEMO,PVO,REF,VVF,  
 1REMFI,VEMF,S11,S12,S21,S22)  
 5 CONTINUE  
 100 FORMAT(4D20.11)  
 101 FORMAT(4I5)  
 102 FORMAT(1H,'3-BODY LAMBERT PROBLEM',1H0,T8,'GAMMA',T28,  
 1'UDM',T48,'UTIME',T68,'UVELM',T88,'ERRMXM',T108,'ERRMAX',1H,  
 21P6D20.11/1H ,T8,'ME',T28,'MM',T48,'ERRMIN',T68,'KNR',1H )

31P4D20.11)

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103 FORMAT(1H0,T8,'TDAY0',T28,'TRIPD',T48,'TDAYF',T68,'TSTART',
1T88,'TEND'/1H ,1P5D20.11)
P4 FORMAT(1H ,T8,'IMODE',T28,'ITLMAX',T48,'IPTJX',T68,'IFILEX'/
11H ,I10,3I20)
105 FORMAT(1H0,T8,'REMO',T68,'VEMO'/1H ,1P6D20.11/1H ,T8,'REVSTAR'/
11H ,1P3D20.11)
106 FORMAT(1H0,T8,'REVMAG',T28,'VEVMAG',T48,'OINCD',T68,'THED'/1H ,
11P4D20.11)
107 FORMAT(1H0,T8,'REVO',T68,'VEVOP'/1H ,1P6D20.11)
108 FORMAT(1H0,T8,'REVF',T68,'VEVF'/1H ,1P6D20.11/1H ,T8,'REMFI',
1T68,'VEMF'/1H ,1P6D20.11)
RETURN
END
```

PROGRAM ETP21  
 PROGRAM COMPUTES FUEL OPTIMAL 2-IMPULSE TRANSFER FROM A PARKING  
 ORBIT OF GIVEN INCLINATION TO A GIVEN FINAL POSITION AND VELOCITY  
 IN FIXED TIME.  
 IMPLICIT REAL\*8(A-H,K-M,O-Z)  
 DIMENSION RSE0(3),VSE0(3),RSM0(3),VSM0(3),XD(3),X(3),XS(3),  
 1RSVTAR(3),VSVTAR(3),V(3,3),GS(3),TSIS(3),LTS(3,3),LS(3,3),  
 2S11S(3,3),S12S(3,3),S21S(3,3),S22S(3,3),GGS(3),VSAV(3,3),G(3),  
 3TSI(3),LT(3,3),L(3,3),GG(3),S11(3,3),S12(3,3),S21(3,3),  
 4S22(3,3),DX(3),DELX(3),UVI(3),UVF(3),TEMP(3,3),DUM(3),UVID(3)  
 DIMENSION R(3),RMVO(3),VMVO(3),RSVO(3),VSVI(3),UVIS(3),UVFS(3),  
 1GD(3),TSID(3),LTD(3,3),LD(3,3),S11D(3,3),S12D(3,3),S21D(3,3),  
 2S22D(3,3),RSVF(3),VSVF(3),RSEF(3),VSEF(3),RSMF(3),VSMF(3),  
 3DUVI(3),REVO(3),VEVO(3),UVFD(3),PVO(6),GGD(3),VSVO(3)  
 COMMON/FLAG/IMTX,IPV,IPTRAJ,IPVTM,IFILE,ITER,ITAR  
 COMMON/CONST/MS,ME,MM,GL1,AUM,UTIME,UVELM,ERRMAX,DTR  
 COMMON/TARG/AY,AZ,ATAR,RSVTAR,VSVTAR  
 READ(5,100)GL1,AUM,UTIME,UVELM  
 READ(5,100)MS,ME,MM  
 READ(5,100)REVMAG,DINCD,OBLD,ERRMXM  
 READ(5,100)TDAY0,TTRIPD  
 READ(5,100)VEVMAG,LOND,THED  
 READ(5,100)RSE0,VSE0,RSM0,VSM0  
 READ(5,100)EPS,EPSTSI,KDX,EPSV  
 READ(5,101)ICOMV,ITERMX,IFILEX,ITAR  
 IF(ITAR.GT.0) GO TO 21  
 READ(5,100)AYM,AZM,ATARD  
 GO TO 22  
 21 READ(5,100)RSVTAR,VSVTAR  
 22 IF(ICOMV.GT.0) GO TO 19  
 OPTION TO INPUT VARIANCE MATRIX (ICOMV=0)  
 READ(5,100)((V(I,J),J=1,3),I=1,3)  
 GO TO 1  
 19 DO 20 I=1,3  
 DO 20 J=1,3  
 V(I,J)=0.  
 IF(I.EQ.J) V(I,J)=1.0  
 20 CONTINUE  
 1 IPV=0  
 IPVTM=0  
 IPTRAJ=0  
 IFILE=0  
 IMTX=1  
 ITER=0  
 ITERD=0  
 DTR=1.7453292519943296D-2  
 ERRMAX=ERRMXM/AUM  
 IF(ITAR.GT.0) GO TO 23  
 AY=AYM/AUM  
 AZ=AZM/AUM  
 ATAR=DTR\*ATARD  
 23 TDAYF=TDAY0+TTRIPD  
 TTRIP=TTRIPD/UTIME  
 TSTART=TDAY0/UTIME  
 TEND=TDAYF/UTIME  
 ALPHA=1.0D-3  
 BETA=10.

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ALPHAM=ALPHA/(1.-ALPHA)
BETAM=BETA/(BETA-1.)
WRITE(6,102)
WRITE(6,103)GL1,AUM,UTIME,UVELM,ERRMXM,ERRMAX
WRITE(6,104)MS,ME,MM,OINCD,OBLD
WRITE(6,105)TDAYO,TTRIPD,TDAYF,TSTART,TTRIP,TEND
WRITE(6,106)RSEO,VSEO
WRITE(6,107)RSMO,VSMO
WRITE(6,108)VEVMAG,LOND,THED,REVMAG
WRITE(6,109)ALPHA,BETA,EPS,EPSTSI,KDX,EPSV
WRITE(6,110)ICOMV,ITERMX,IFILEX,ITAR
IF(ITAR.GT.0) GO TO 24
WRITE(6,124)AYM,AZM,ATARD
GO TO 25
24 WRITE(6,125)RSVTAR,VSVTAR
25 LON=DTR*LOND
THE=DTR*THED
OINC=DTR*OINCD
OBL=DTR*OBLD
XS(1)=VEVMAG
XS(2)=LON
XS(3)=THE
C COMPUTE INITIAL NOMINAL TRAJECTORY
CALL COMFG(TSTART,TEND,REVMAG,XS,OINC,DBL,RSEO,VSEO,RSMO,VSMO,
IFS,TESTRS,GS,TSIS,LTS,S11S,S12S,S21S,S22S,UVIS,UVFS)
ITER=1
CALL COMAUG(FS,GS,TSIS,LTS,V,LS,FGS,GGS)
IF(ICOMV.EQ.0) GO TO 200
C OPTION TO COMPUTE TRIAL VARIANCE MATRIX (ICOMV=1)
GGSMAG=VMAG(GGS)
DO 2 I=1,3
DO 2 J=1,3
V(I,J)=V(I,J)*EPSV/GGSMAG
2 CONTINUE
200 WRITE(6,111)((V(I,J),J=1,3),I=1,3)
C SAVE VARIANCE MATRIX
DO 3 I=1,3
DO 3 J=1,3
3 VSAV(I,J)=V(I,J)
KV=1.
KDXSAV=KDX
IF(TESTRS.GT.EPSTSI)GO TO 8
C UPDATE VARIABLES
CALL UPX(XS,FS,TESTRS,GS,TSIS,LTS,LS,FGS,GGS,S11S,S12S,S21S,
S22S,UVIS,UVFS,X,F,TESTR,G,TSI,LT,L,FG,GG,S11,S12,S21,S22,
2UVI,UVF)
WRITE(6,112)X,F,FG,TESTR
WRITE(6,113)TSI,G
WRITE(6,114)LT
WRITE(6,115)GG
C ACCELERATED GRADIENT PROJECTION ITERATION LOOP
4 ITERD=ITERD+1
5 DO 501 I=1,3
DO 501 J=1,3
501 V(I,J)=KV*VSAV(I,J)
6 CALL MXV(V,GG,R,3,3)
P=DOT(GG,R,3)

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IF((P-2.*FG).LE.EPS) GO TO 7
LAM=2.*FG/P
CALL VVT(R,TEMP,3)
DO 601 I=1,3
DO 601 J=1,3
601 VSAV(I,J)=V(I,J)+(LAM-1.)*TEMP(I,J)/P
GO TO 5
7 CALL MXV(V,GG,DX,3,3)
C FORM TRIAL NEW INDEPENDENT VARIABLES
DO 701 I=1,3
701 XS(I)=X(I)-DX(I)
WRITE(6,116)ITERD,DX
WRITE(6,117)XS,KV
WRITE(6,111)((V(I,J),J=1,3),I=1,3)
CALL COMFG(TSTART,TEND,REVMAG,XS,DINC,LBL,RSEO,VSEO,RSMO,VSMO,
1FS,TESTRS,GS,TSIS,LTS,S11S,S12S,S21S,S22S,UVIS,UVFS)
CALL COMAUG(FS,GS,TSIS,LTS,V,LS,FGS,GGS)
IF(TESTRS.LT.EPSTS1) GO TO 11
C CONSTRAINT RESTORATION
8 WRITE(6,118)
801 CALL COMDX(LTS,LS,TSIS,DX)
WRITE(6,119)DX
9 DO 901 I=1,3
DELX(I)=KDX*DX(I)
901 XD(I)=XS(I)+DELX(I)
WRITE(6,120)KDX,DELX
CALL COMFG(TSTART,TEND,REVMAG,XD,DINC,LBL,RSEO,VSEO,RSMO,VSMO,
1FD,TESTRD,GD,TSID,LTD,S11D,S12D,S21D,S22D,UVID,UVFD)
IF(TESTRD.LT.TESTRS) GO TO 10
KDX=KDX/10.
WRITE(6,126)
GO TO 9
10 CALL COMAUG(FD,GD,TSID,LTD,V,LD,FGD,GGD)
CALL UPX(XD,FD,TESTRD,GD,TSID,LTD,LD,FGD,GGD,S11D,S12D,S21D,
1S22D,UVID,UVFD,XS,FS,TESTRS,GS,TSIS,LTS,LS,FGS,GGS,S11S,S12S,
2S21S,S22S,UVIS,UVFS)
KDX=2.*KDX
IF(KDX.GT.1.0)KDX=1.0
IF(TESTRS.GT.EPSTS1) GO TO 801
KDX=KDXSAV
IF(ITERD.EQ.0) GO TO 11
IF(FS.LT.F) GO TO 11
KV=KV/2.
GO TO 5
C CONSTRAINT RESTORED
11 IF(ITERD.LT.ITERMX)GO TO 300
WRITE(6,127)
GO TO 17
300 IF(ITERD.EQ.0)GO TO 16
C UPDATE VARIANCE MATRIX
CALL MXV(V,GGS,R,3,3)
P=DOT(GGS,R,3)
WRITE(6,121)FS,TESTRS,FGS,TSIS
WRITE(6,122)GS,GGS
WRITE(6,123)P
IF(P.LT.EPS) GO TO 17
GAMMA=-DOT(GG,R,3)/P

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IF(GAMMA.EQ.(-1.)) GO TO 12
IF(GAMMA.GE.ALPHAM)GO TO 13
LAM=ALPHA
GO TO 14
12 IF(GAMMA.LE.(-BETAM)) GO TO 13
LAM=BETA
GO TO 14
13 LAM=GAMMA/(GAMMA+1.)
14 CALL VVT(R,TEMP,3)
DO 15 I=1,3
DO 15 J=1,3
15 V(I,J)=V(I,J)+(LAM-1.)*TEMP(I,J)/P
IF(FGS.LT.FG) GO TO 16
GO TO 6
16 KV=1.
CALL UPX(XS,FS,TESTRS,GS,TSIS,LTS,LS,FGS,GGS,S11S,S12S,S21S,
1S22S,UVIS,UVFS,X,F,TESTR,G,TSI,LT,L,FG,GG,S11,S12,S21,S22,
2UVI,UVF)
IF(ITERD.EQ.0) GO TO 4
DO 161 I=1,3
DO 161 J=1,3
161 VSAV(I,J)=V(I,J)
GO TO 4
17 CALL UPX(XS,FS,TESTRS,GS,TSIS,LTS,LS,FGS,GGS,S11S,S12S,S21S,
1S22S,UVIS,UVFS,X,F,TESTR,G,TSI,LT,L,FG,GG,S11,S12,S21,S22,
2UVI,UVF)
C COMPUTE PRIMER VECTOR DERIVATIVE
CALL MXV(S11,UVI,DUM,3,3)
CALL INVERT(S12,TEMP)
DO 18 I=1,3
18 DUM(I)=UVF(I)-DUM(I)
CALL MXV(TEMP,DUM,DUVI,3,3)
DO 400 I=1,3
PVO(I)=UVI(I)
400 PVO(I+3)=DUVI(I)
IPV=1
IPVTM=1
IPTRAJ=1
IFILE=IFILEX
C GENERATE OPTIMAL TRAJECTORY AND PRIMER VECTOR HISTORY
VEVMAG=X(1)
LON=X(2)
THE=X(3)
CALL COMIC(REVMAG,VEVMAG,LON,THE,OINC,OBL,RSEO,VSEO,REVO,VEVO,
1RSVO,VSVO,VSVI)
CALL FOURBY(TSTART,TEND,RSVO,VSVI,RSEO,VSEO,RSMO,
1VSMO,PVO,RSVF,VSVF,RSEF,VSEF,RSMF,VSMF,S11,S12,S21,S22)
100 FORMAT(4D20.11)
101 FORMAT(4I5)
102 FORMAT(1H ,T8,'4-BODY 2-IMPULSE OPTIMAL TRANSFER FROM EARTH'/
11H ,T8,'TO HALO TARGET AT L1. ITERATE ON VELOCITY MAGNITUDE'/
21H ,T8,'LONGITUDE OF NODE AND ORBITAL ANGLE FROM NODE USING'/
31H ,T8,'ACCELERATED GRADIENT PROJECTION AND DAVIDON VARIANCE'/
41H ,T8,'METHOD')
103 FORMAT(1H0,T8,'GL1',T28,'AUM',T48,'UTIME',T68,'UVELM',T88,
1'ERRMXM',T108,'ERRMAX'/1H ,1P6D20.11)
104 FORMAT(1H ,T8,'MS',T28,'ME',T48,'MM',T68,'OINCD',T88,'OBLD'/

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11H ,1P5D20.11)
105 FORMAT(1H ,T8,'TDOAY0',T28,'TTRIPD',T48,'TDAYF',T68,'TSTART',
1T88,'TTRIP',T108,'TEND'/1H ,1P6D20.11)
6 FORMAT(1H ,T8,'RSE0',T68,'VSE0'/1H ,1P6D20.11)
107 FORMAT(1H ,T8,'RSMO',T68,'VSMO'/1H ,1P6D20.11)
108 FORMAT(1H ,T8,'VEVMAG',T28,'LOND',T48,'THED',T68,'REVMAG'/
11H ,1P4D20.11)
109 FORMAT(1H ,T8,'ALPHA',T28,'BETA',T48,'EPS',T68,'EPSTS1',T88,
1'KDX',T108,'EPSV'/1H ,1P6D20.11)
110 FORMAT(1H ,T8,'JCOMV',T28,'ITERMX',T48,'IFILEX',T68,'ITAR'/
11H ,I10,3I20)
111 FORMAT(1H0,T8,'V'/1H ,1P6D20.11/1H ,1P3D20.11)
112 FORMAT(1H0,T8,'X',T68,'F',T88,'FG',T108,'TESTR'/1H ,1P6D20.11)
113 FORMAT(1H ,T8,'TSI',T68,'G'/1H ,1P6D20.11)
114 FORMAT(1H ,T8,'LT'/1H ,1P6D20.11/1H ,1P3D20.11)
115 FORMAT(1H ,T8,'GG'/1H ,1P3D20.11)
116 FORMAT(1H1,T8,'ITERD',T28,'DX'/1H ,I10,10X,1P3D20.11)
117 FORMAT(1H ,T8,'XS',T68,'KV'/1H ,1P4D20.11)
118 FORMAT(1H0,T8,'CONSTRAINT RESTROATION')
119 FORMAT(1H0,T8,'DX'/1H ,1P3D20.11)
120 FORMAT(1H ,T8,'KDX',T28,'DELX'/1H ,1P4D20.11)
121 FORMAT(1H ,T8,'FS',T28,'TESTRS',T48,'FGS',T68,'TSIS'/1H ,
11P6D20.11)
122 FORMAT(1H ,T8,'GS',T68,'GGS'/1H ,1P6D20.11)
123 FORMAT(1H ,T8,'P'/1H ,1P6D20.11)
124 FORMAT(1H0,T8,'AYM',T28,'AZM',T48,'ATARD'/1H ,1P3D20.11)
125 FORMAT(1H0,T8,'INPUT TARGET'/1H0,T8,'RSVTAR',T68,'VSVTAR'/
11H ,1P6D20.11)
126 FORMAT(1H0,T8,'-----')
127 FORMAT(1H0,T8,'NO. OF DAVIDON ITERATIONS HAS REACHED MAXIMUM')
RETURN
END
```

C PROGRAM ETP213  
 C PROGRAM COMPUTES FUEL OPTIMAL 2-IMPULSE TRANSFER FROM A PARKING  
 C ORBIT OF GIVEN INCLINATION TO A GIVEN FINAL POSITION AND VELOCITY  
 C IN FIXED TIME IN EARTH-MOON-VEHICLE SPACE.  
 IMPLICIT REAL\*8(A-H,K-M,O-Z)  
 DIMENSION REM0(3),VEM0(3),XD(3),X(3),XS(3),REVTAR(3),VEVTAR(3),  
 1V(3,3),GS(3),TSIS(3),LTS(3,3),LS(3,3),S11S(3,3),S12S(3,3),  
 2S21S(3,3),GGS(3),VSAV(3,3),G(3),TSI(3),LT(3,3),L(3,3),GG(3),  
 3S11(3,3),S12(3,3),S21(3,3),S22(3,3),DX(3),DELX(3),UVI(3),UVF(3),  
 4TEMP(3,3),DUM(3),UVID(3),S22S(3,3),PVO(6),GGD(3)  
 DIMENSION R(3),REVO(3),VEVO(3),VEVOP(3),UVIS(3),UVFS(3),UVFD(3),  
 1GD(3),TSID(3),LTD(3,3),LD(3,3),S11D(3,3),S12D(3,3),S21D(3,3),  
 2S22D(3,3),REVF(3),VEVF(3),REM(3),VEMF(3),DUVI(3)  
 COMMON/FLAG/IMTX,IPV,IPTRAJ,IPVTM,IFILE,ITER,ITAR  
 COMMON/CONST3/ME,MM,GAMMA,UDM,UTIME,UVELM,ERRMAX,DTR  
 COMMON/TARG/AY,AZ,ATAR,REVTAR,VEVTAR  
 READ(5,100) GAMMA,UDM,UTIME,UVELM  
 READ(5,100) ME,MM  
 READ(5,100) REVMAG,OINCD,ERRMXM  
 READ(5,100) TDAY0,TTRIPD  
 READ(5,100) VEVmag,LOND,THED  
 READ(5,100) REM0,VEM0  
 READ(5,100) EPS,EPSTSI,KDX,EPSV  
 READ(5,101) ICOMV,ITERMX,IFILEX,ITAR  
 IF(ITAR.GT.0) GO TO 21  
 READ(5,100) AYM,AZM,ATARD  
 GO TO 22  
 21 READ(5,100) REVTAR,VEVTAR  
 22 IF(ICOMV.GT.0) GO TO 19  
 C OPTION TO INPUT VARIANCE MATRIX (ICOMV=0)  
 READ(5,100) ((V(I,J),J=1,3),I=1,3)  
 GO TO 1  
 19 DO 20 I=1,3  
 DO 20 J=1,3  
 V(I,J)=0.  
 IF(I.EQ.J) V(I,J)=1.0  
 20 CONTINUE  
 1 IPV=0  
 IPVTM=0  
 IPTRAJ=0  
 IFILE=0  
 IMTX=1  
 ITER=0  
 ITERD=0  
 DTR=1.7453292519943296D-2  
 ERRMAX=ERRMXM/UDM  
 IF(ITAR.GT.0) GO TO 23  
 AY=AYM/AUM  
 AZ=AZM/AUM  
 ATARD=DTR\*ATARD  
 23 TDAYF=TDAY0+TTRIPD  
 TTRIP=TTRIPD/UTIME  
 TSTART=TDAY0/UTIME  
 TEND=TDAYF/UTIME  
 ALPHA=1.0D-3  
 BETA=10.  
 ALPHAM=ALPHA/(1.-ALPHA)

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BETAM=BETA/(BETA-1.)
WRITE(6,102)
WRITE(6,103)GAMMA,UDM,UTIME,UVELM,ERRMXM,ERRMAX
WRITE(6,104)ME,MM,OINCD
WRITE(6,105)TDOYO,TTRIPD,TDAYF,TSTART,TTRIP,TEND
WRITE(6,106)REMO,VEMO
WRITE(6,108)VEVMAG,LOND,THED,REVMAG
WRITE(6,109)ALPHA,BETA,EPS,EPSTSI,KDX,EPSV
WRITE(6,110)ICOMV,ITERMX,IFILEX,ITAR
IF(ITAR.GT.0) GO TO 24
WRITE(6,124)AYM,AZM,ATARD
GO TO 25
24 WRITE(6,125)REVTAR,VEVTAR
25 LON=DTR*LOND
THE=DTR*THED
OINC=DTR*OINCD
XS(1)=VEVMAG
XS(2)=LON
XS(3)=THE
C COMPUTE INITIAL NOMINAL TRAJECTORY
CALL COMFG3(TSTART,TEND,REVMAG,XS,OINC,REMO,VEMO,FS,TESTRS,GS,
1TSIS,LTS,S11S,S12S,S21S,S22S,UVIS,UVFS)
ITER=1
CALL COMAUG(FS,GS,TSIS,LTS,V,LS,FGS,GGS)
IF(ICOMV.EQ.0) GO TO 200
C OPTION TO COMPUTE TRIAL VARIANCE MATRIX (ICOMV=1)
GGSMAG=VMAG(GGS)
DO 2 I=1,3
DO 2 J=1,3
V(I,J)=V(I,J)*EPSV/GGSMAG
2 CONTINUE
200 WRITE(6,111) ((V(I,J),J=1,3),I=1,3)
C SAVE VARIANCE MATRIX
DO 3 I=1,3
DO 3 J=1,3
3 VSAV(I,J)=V(I,J)
KV=1.
KDXSAV=KDX
IF(TESTRS.GT.EPSTSI)GO TO 8
C UPDATE VARIABLES
CALL UPX(XS,FS,TESTRS,GS,TSIS,LTS,LS,FGS,GGS,S11S,S12S,S21S,
1S22S,UVIS,UVFS,X,F,TESTR,G,TSI,LT,L,FG,GG,S11,S12,S21,S22,
2UVI,UVF)
WRITE(6,112)X,F,FG,TESTR
WRITE(6,113)TSI,G
WRITE(6,114)LT
WRITE(6,115)GG
C ACCELERATED GRADIENT PROJECTION ITERATION LOOP
4 ITERD=ITERD+1
5 DO 501 I=1,3
DO 501 J=1,3
501 V(I,J)=KV*VSAV(I,J)
6 CALL MXV(V,GG,R,3,3)
P=DOT(GG,R,3)
IF((P-2.*FG).LE.EPS) GO TO 7
LAM=2.*FG/P
CALL VVT(R,TEMP,3)

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DO 601 I=1,3
DO 601 J=1,3
601 VSAV(I,J)=V(I,J)+(LAM-1.)*TEMP(I,J)/P
GO TO 5
7 CALL MXV(V,GG,DX,3,3)
C FORM TRIAL NEW INDEPENDENT VARIABLES
DO 701 I=1,3
701 XS(I)=X(I)-DX(I)
WRITE(6,116)ITERD,DX
WRITE(6,117)XS,KV
WRITE(6,111) ((V(I,J),J=1,3),I=1,3)
CALL COMFG3(TSTART,TEND,REVMAG,XS,DINC,REMO,VEMO,FS,TESTRS,GS,
1TSIS,LTS,S11S,S12S,S21S,S22S,UVIS,UVFS)
CALL COMAUG(FS,GS,TSIS,LTS,V,LS,FGS,GGS)
IF(TESTRS.LT.EPSTS1) GO TO 11
C CONSTRAINT RESTORATION
8 WRITE(6,118)
801 CALL COMDX(LTS,LS,TSIS,DX)
WRITE(6,119)DX
9 DO 901 I=1,3
DELX(I)=KDX*DX(I)
901 XD(I)=XS(I)+DELX(I)
WRITE(6,120)KDX,DELX
CALL COMFG3(TSTART,TEND,REVMAG,XD,DINC,REMO,VEMO,FD,TESTRD,GD,
1TSID,LTD,S11D,S12D,S21D,S22D,UVID,UVFD)
IF(TESTRD.LT.TESTRS) GO TO 10
KDX=KDX/10.
GO TO 9
10 CALL COMAUG(FD,GS,TSID,LTD,V,LD,FGD,GGD)
CALL UPX(XD,FD,TESTRD,GS,TSID,LTD,LD,FGD,GGD,S11D,S12D,S21D,
1S22D,UVID,UVFD,XS,FS,TESTRS,GS,TSIS,LTS,LS,FGS,GGS,S11S,S12S,
2S21S,S22S,UVIS,UVFS)
KDX=2.*KDX
IF(KDX.GT.1.) KDX=1.
IF(TESTRS.GT.EPSTS1) GO TO 801
KDX=KDXSAV
IF(ITER.EQ.0) GO TO 11
IF(FS.LT.F) GO TO 11
KV=KV/2.
GO TO 5
C CONSTRAINT RESTORED
11 IF(ITERD.LT.ITERMX)GO TO 300
WRITE(6,126)
GO TO 17
300 IF(ITERD.EQ.0)GO TO 16
C UPDATE VARIANCE MATRIX
CALL MXV(V,GGS,R,3,3)
P=DOT(GGS,R,3)
WRITE(6,121)FS,TESTRS,FGS,TSIS
WRITE(6,122)GS,GGS
WRITE(6,123)P
IF(P.LT.EPS) GO TO 17
GAMMA=-DOT(GG,R,3)/P
IF(GAMMA.EQ.(-1.)) GO TO 12
IF(GAMMA.GE.ALPHAM)GO TO 13
LAM=ALPHA
GO TO 14

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12 IF(GAMMA.LE.(-BETAM)) GO TO 13
  LAM=BETA
  GO TO 14
13 LAM=GAMMA/(GAMMA+1.)
14 CALL VVT(R,TEMP,3)
  DO 15 I=1,3
  DO 15 J=1,3
15 V(I,J)=V(I,J)+(LAM-1.)*TEMP(I,J)/P
  IF(FGS.LT.FG) GO TO 16
  GO TO 6
16 KV=1.
  CALL UPX(XS,FS,TESTRS,GS,TSIS,LTS,LS,FGS,GGS,S11S,S12S,S21S,
  1S22S,UVIS,UVFS,X,F,TESTR,G,TSI,LT,L,FG,GG,S11,S12,S21,S22,
  2UVI,UVF)
  IF(ITERD.EQ.0) GO TO 4
  DO 161 I=1,3
  DO 161 J=1,3
161 VSAV(I,J)=V(I,J)
  GO TO 4
17 CALL UPX(XS,FS,TESTRS,GS,TSIS,LTS,LS,FGS,GGS,S11S,S12S,S21S,
  1S22S,UVIS,UVFS,X,F,TESTR,G,TSI,LT,L,FG,GG,S11,S12,S21,S22,
  2UVI,UVF)
C COMPUTE PRIMER VECTOR DERIVATIVE
  CALL MXV(S11,UVI,DUM,3,3)
  CALL INVERT(S12,TEMP)
  DO 18 I=1,3
18 DUM(I)=UVF(I)-DUM(I)
  CALL MXV(TEMP,DUM,DUVI,3,3)
  DO 400 I=1,3
  PVO(I)=UVI(I)
400 PVO(I+3)=DUVI(I)
  IPV=1
  IPVTM=1
  IPTRAJ=1
  IFILE=IFILEX
C GENERATE OPTIMAL TRAJECTORY AND PRIMER VECTOR HISTORY
  VEVmag=X(1)
  LON=X(2)
  THE=X(3)
  CALL COMIC3(REVMAG,VEVMAG,LON,THE,OINC,REVO,VEVO,VEVOP)
  CALL THRBDY(TSTART,TEND,REVO,VEVOP,REMO,VEMO,PVO,REVf,VEVF,
  1REMF,VEMF,S11,S12,S21,S22)
100 FORMAT(4D20.11)
101 FORMAT(4I5)
102 FORMAT(1H ,T8,'3-BODY 2-IMPULSE OPTIMAL TRANSFER FROM EARTH'/
  11H ,T8,'TO HALO ORBIT AT L1 OR L2. ITERATE ON VELOCITY'/
  21H ,T8,'MAGNITUDE, LONGITUDE OF NODE AND ORBITAL ANGLE FROM'/
  31H ,T8,'NODE USING ACCELERATED GRADIENT PROJECTION AND'/
  41H ,T8,'DAVIDON VARIANCE METHOD')
103 FORMAT(1H0,T8,'GAMMA',T28,'UDM',T48,'UTIME',T68,'UVELM',T88,
  1'ERRMXM',T108,'ERRMAX'/1H ,1P6D20.11)
104 FORMAT(1H ,T8,'ME',T28,'MM',T48,'OINCD'/
  11H ,1P5D20.11)
105 FORMAT(1H ,T8,'TDAY0',T28,'TTRIPD',T48,'TDAYF',T68,'TSTART' ,
  1T88,'TTRIP',T108,'TEND'/1H ,1P6D20.11)
106 FORMAT(1H ,T8,'REMO',T68,'VEMO'/1H ,1P6D20.11)
108 FORMAT(1H ,T8,'VEVMAG',T28,'LOND',T48,'THED',T68,'REVMAG'/

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11H ,1P4D20.11)
109 FORMAT(1H ,T8,'ALPHA',T28,'BETA',T48,'EPS',T68,'EPSTSI',T88,
 1'KDX',T108,'EPSV'/1H ,1P6D20.11)
110 FORMAT(1H ,T8,'ICOMV',T28,'ITERMX',T48,'IFILEX',T68,'ITAR'/
 1H ,I10,3I20)
111 FORMAT(1H0,T8,'V'/1H ,1P6D20.11/1H ,1P3D20.11)
112 FORMAT(1H0,T8,'X',T68,'F',T88,'FG',T108,'TESTR'/1H ,1P6D20.11)
113 FORMAT(1H ,T8,'TSI',T68,'G'/1H ,1P6D20.11)
114 FORMAT(1H ,T8,'LT'/1H ,1P6D20.11/1H ,1P3D20.11)
115 FORMAT(1H ,T8,'GG'/1H ,1P3D20.11)
116 FORMAT(1H1,T8,'ITERD',T28,'DX'/1H ,I10,10X,1P3D20.11)
117 FORMAT(1H ,T8,'XS',T68,'KV'/1H ,1P4D20.11)
118 FORMAT(1H0,T8,'CONSTRAINT RESTROATION')
119 FORMAT(1H0,T8,'DX'/1H ,1P3D20.11)
120 FORMAT(1H ,T8,'KDX',T28,'DELX'/1H ,1P4D20.11)
121 FORMAT(1H ,T8,'FS',T28,'TESTRS',T48,'FGS',T68,'TSIS'/1H ,
 11P6D20.11)
122 FORMAT(1H ,T8,'GS',T68,'GGS'/1H ,1P6D20.11)
123 FORMAT(1H ,T8,'P'/1H ,1PD20.11)
124 FORMAT(1H0,T8,'AYM',T28,'AZM',T48,'ATARD'/1H ,1P3D20.11)
125 FORMAT(1H0,T8,'INPUT TARGET'/1H0,T8,'REVTAR',T68,'VEVTAR'/1H ,
 11P6D20.11)
126 FORMAT(1H0,T8,'NO. OF DAVIDON ITERATIONS HAS REACHED MAXIMUM')
      RETURN
      END
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C PROGRAM PTP3I
C PROGRAM COMPUTES FUEL OPTIMAL 3-IMPULSE TRANSFER FROM A GIVEN
C INITIAL POSITION TO A GIVEN FINAL POSITION AND VELOCITY IN
C FIXED TIME.
IMPLICIT REAL*8(A-H,K-M,O-Z)
DIMENSION X(4),G(4),V(4,4),XS(4),GS(4),R(4),DX(4),RSVO(3),
1VSVO(3),RSEO(3),VSEO(3),RSMO(3),VSMO(3),VSVI(3),
2TEMP1(4,4),SFM11S(3,3),SFM12S(3,3),SFM21S(3,3),SFM22S(3,3),
3SMI11S(3,3),SMI12S(3,3),SMI21S(3,3),SMI22S(3,3),RSVM(3),
4VSVMP(3),RSVMS(3),VSVMPS(3),DUVIS(3),DUVMMMS(3),
5DUVMP(3),DG(4),VS(4,4),DXC(4),XC(4),RSVMC(3),VSVMPC(3),
6UVIC(3),UVMC(3),UVFC(3),DUVIC(3),DUVMMC(3),DUVMP(3),RC(4),
7SMI11C(3,3),SMI12C(3,3),SMI21C(3,3),SMI22C(3,3),SFM11C(3,3),
8SFM12C(3,3),SFM21C(3,3),SFM22C(3,3),RSVMD(3),VSVMPC(3),UVIS(3),
9UVMS(3),UVFS(3),S(4),SFM11(3,3),SFM12(3,3),SFM21(3,3),
1SFM22(3,3),UVI(3),UVM(3),UVF(3),DUVI(3),DUVMM(3),DUVMP(3),
2SMI11(3,3),SMI12(3,3),SMI21(3,3),SMI22(3,3),PVO(6),PVM(6),
3RSVTAR(3),VSVTAR(3),SFM11D(3,3),SFM12D(3,3)

DIMENSION VSVM(3),RSEM(3),VSEM(3),RSMM(3),VSMM(3),
1RSVF(3),VSVF(3),RSEF(3),VSEF(3),RSMF(3),VSMF(3)
DIMENSION DGC(4),VC(4,4),GC(4),VSVMMS(3),VSVMPC(3)
COMMON/CONST/MS,ME,MM,GL1,AUM,UTIME,UVELM,ERRMAX,DTR
COMMON/FLAG/IMTX,IPV,IPTRAJ,IPVTM,IFILE,ITER,ITAR
READ(5,100)GL1,AUM,UTIME,UVELM
READ(5,100)MS,ME,MM
READ(5,100)TSTART,TM,TEND
READ(5,100)RSEO,VSEO,RSMO,VSMO
READ(5,100)RSVO,VSVO
READ(5,100)VSVI,VSVMP
READ(5,100)RSVTAR,VSVTAR
READ(5,100)KNR,ERRMIN,ERRMXM
READ(5,100)FMINM,EPS,EPSV
READ(5,101)ICOMV,ITLMAX,ILINC,ITDMAX,IFILEX
IFI(ICOMV.GT.0)GO TO 190
OPTION TO INPUT VARIANCE MATRIX(ICOMV=0)
READ(5,100) ((V(I,J),J=1,4),I=1,4)
GO TO 1
190 DO 200 I=1,4
DO 200 J=1,4
V(I,J)=0.
IFI(I.EQ.J) V(I,J)=1.0
200 CONTINUE
1 DTR=1.7453292519943296D-2
ERRMAX=ERRMXM/AUM
FMIN=FMINM*UVELM
KNRSAV=KNR
ALPMIN=1.0D-8
WRITE(6,102)GL1,AUM,UTIME,UVELM,ERRMXM,ERRMAX,MS,ME,MM
WRITE(6,103)TSTART,TM,TEND,RSVO,VSVO,RSEO,VSEO,RSMO,VSMO
WRITE(6,104)VSVI,VSVMP,RSVTAR,VSVTAR
WRITE(6,105)KNR,ERRMIN,FMINM,EPS,EPSV
WRITE(6,106)ICOMV,ITLMAX,ILINC,ITDMAX,IFILEX
IPV=0
IPVTM=0
IFILE=0
IPTRAJ=0
IMTX=1

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ITERD=0
DO 2 I=1,3
2 X(I)=VSVI(I)
X(4)=TM
C COMPUTE INITIAL NOMINAL TRAJECTORY
CALL COMFITSTART,TM,TEND,RSVO,VSVO,VSVI,RSEO,VSEO,RSMO,VSMO,
1ERRMIN,ILINC,KNRSAV,ITERD,ITLMAX,RSVMD,VSVMPD,RSVTAR,VSVTAR,
2SFM11D,SFM12D,RSVM,VSVMM,VSVMP,F,UVI,UVM,UVF,SMI11,
3SMI12,SMI121,SMI122,SFM11,SFM12,SFM21,SFM22)
CALL COMG(SMI11,SMI12,SMI21,SMI22,SFM11,SFM12,VSVMP,VSVMM,UVI,
1UVM,UVF,DUVI,DUVMM,DUVMP,G)
GMAG=DSQRT(DOT(G,G,4))
WRITE(6,108)F,G,GMAG
DO 3 I=1,3
RSVMD(I)=RSVM(I)
VSVMPD(I)=VSVMP(I)
DO 3 J=1,3
SFM11D(I,J)=SFM11(I,J)
3 SFM12D(I,J)=SFM12(I,J)
IF(ICOMV.EQ.0) GO TO 40
C OPTION TO COMPUTE TRIAL VARIANCE MATRIX (ICOMV=1)
DO 4 I=1,4
DO 4 J=1,4
V(I,J)=V(I,J)*EPSV/GMAG
4 CONTINUE
40 WRITE(6,107) ((V(I,J),J=1,4),I=1,4)
C ACCELERATED GRADIENT ITERATION LOOP
5 ITERD=ITERD+1
WRITE(6,109)ITERD
1 CALL MXV(V,G,S,4,4)
DO 50 I=1,4
50 S(I)=-S(I)
SG=DOT(S,G,4)
WRITE(6,110)S,SG
IF(SG.LT.0.)GO TO 51
DO 52 I=1,4
52 S(I)=-S(I)
SG=-SG
WRITE(6,111)S,SG
51 ALP=(FMIN-F)/SG
ALPHA=DMIN1(1.00+0,ALP)
6 DO 61 I=1,4
DX(I)=ALPHA*S(I)
61 XS(I)=X(I)+DX(I)
DO 62 I=1,3
62 VSVI(I)=XS(I)
WRITE(6,112)DX,ALPHA,XS
CALL COMF(TSTART,XS(4),TEND,RSVO,VSVO,VSVI,RSEO,VSEO,RSMO,VSMO,
1ERRMIN,ILINC,KNRSAV,ITERD,ITLMAX,RSVMD,VSVMPD,RSVTAR,VSVTAR,
2SFM11D,SFM12D,RSVMS,VSVMMS,VSVMPS,FS,UVIS,UVMS,UVFS,SMI11S,
3SMI12S,SMI121S,SMI122S,SFM11S,SFM12S,SFM21S,SFM22S)
CALL COMG(SMI11S,SMI12S,SMI21S,SMI22S,SFM11S,SFM12S,VSVMPS,
1VSVMMS,UVIS,UVMS,UVFS,DUVIS,DUVMMMS,DUVMPGS)
GSMAG=DSQRT(DOT(GS,GS,4))
WRITE(6,113)FS,GS,GSMAG
DO 701 I=1,4
701 DG(I)=GS(I)-G(I)

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CALL MXV(V,DG,R,4,4)
DO 71 I=1,4
71 R(I)=R(I)-DX(I)
RMAG=DSQRT(DOT(R,R,4))
P=DOT(DG,R,4)
PMAG=DABS(P)
SGS=DOT(S,GS,4)
WRITE(6,114)DG,P,SGS,R,RMAG
8 CALL VVT(R,TEMP1,4)
DO 81 I=1,4
DO 81 J=1,4
81 V(I,J)=V(I,J)-TEMP1(I,J)/P
82 IF(SGS.GT.0.)GO TO 83
IF(FS.LT.F)GO TO 14
ALPHA=ALPHA/10.0
IF(ALPHA.LT.ALPMIN)GO TO 84
GO TO 6
84 DO 840 I=1,4
DO 840 J=1,4
V(I,J)=0.
IF(I.EQ.J)V(I,J)=1.
840 V(I,J)=V(I,J)*EPSV/GMAG
WRITE(6,122)
GO TO 40
83 CONTINUE
C CUBIC INTERPOLATION BETWEEN X AND XS
Z=3.*(F-FS)/ALPHA+SG+SGS
W2=Z*Z-SG*SGS
IFI(W2.LE.0.)GO TO 13
W=DSQRT(W2)
ALPHAC=ALPHA*(1.-(SGS+W-Z)/(SGS-SG+2.*W))
DO 9 I=1,4
DXC(I)=ALPHAC*S(I)
9 XC(I)=X(I)+DXC(I)
DO 901 I=1,3
901 VSVI(I)=XC(I)
WRITE(6,115)DXC,ALPHAC,XC
CALL COMFT(START,XC(4),TEND,RSVO,VSVO,VSVI,RSEO,VSEO,RSMO,VSMO,
IERRMIN,ILINC,KNRSAV,ITERD,ITLMAX,RSVMD,VSVMPC,RSVTAR,VSVTAR,
2SFM11D,SFM12D,RSVMC,VSVMCC,VSVMPC,FC,UVIC,UVMC,UVFC,SMI11C,
3SMI12C,SMI21C,SMI22C,SFM11C,SFM12C,SFM21C,SFM22C)
CALL COMG(SMI11C,SMI12C,SMI21C,SMI22C,SFM11C,SFM12C,VSVMPC,
1VSVMCC,UVIC,UVMC,UVFC,DUVIC,DUVMMC,DUVMPC,GC)
GCMAG=DSQRT(DOT(GC,GC,4))
WRITE(6,116)FC,GC,GCMAG
DO 902 I=1,4
902 DGC(I)=GC(I)-G(I)
DO 91 I=1,3
RSVMD(I)=RSVMC(I)
VSVMPC(I)=VSVMPC(I)
DO 91 J=1,3
SFM11D(I,J)=SMF11C(I,J)
91 SFM12D(I,J)=SMF12C(I,J)
CALL MXV(V,GC,RC,4,4)
DO 92 I=1,4
92 RC(I)=RC(I)-DXC(I)
RCMAG=DSQRT(DOT(RC,RC,4))

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PC=DOT(DGC,RC,4)
CALL VVT(RC,TEMP1,4)
DO 93 I=1,4
DO 93 J=1,4
93 V(I,J)=V(I,J)-TEMP1(I,J)/PC
  WRITE(6,117)DGC,PC,RC,RCMAG
  IF(FS.GT.F)GO TO 11
  IF(FC.GT.FS)GO TO 14
10 DO 20 I=1,4
  X(I)=XC(I)
20 G(I)=GC(I)
  DO 201 I=1,3
  UVI(I)=UVIC(I)
  UVM(I)=UVMC(I)
  DUVI(I)=DUVIC(I)
  DUVMM(I)=DUVMMC(I)
  DUVMP(I)=DUVMP(I)
  RSVMD(I)=RSVMC(I)
  VSVMRD(I)=VSVMPC(I)
  DO 201 J=1,3
  SFM11D(I,J)=SFM11C(I,J)
201 SFM12D(I,J)=SFM12C(I,J)
  F=FC
  GMAG=GCMAG
  GO TO 16
11 IF(FC.LT.F)GO TO 10
C   FC GRTHN F. REPEAT INTERPOLATION IN REDUCED INTERVAL.
  FS=FC
  ALPHA=ALPHAC
  DO 250 I=1,3
  XS(I)=XC(I)
  GS(I)=GC(I)
  RSVMS(I)=RSVMC(I)
  VSVMPS(I)=VSVMPC(I)
  UVIS(I)=UVIC(I)
  UVMS(I)=UVMC(I)
  DUVIS(I)=DUVIC(I)
  DUVMMS(I)=DUVMMC(I)
  DUVMPS(I)=DUVMP(I)
  DO 250 J=1,3
  SFM11S(I,J)=SFM11C(I,J)
250 SFM12S(I,J)=SFM12C(I,J)
  SGS=DOT(S,GS,4)
  WRITE(6,121)SGS
  GO TO 82
13 IF(FS.GT.F)GO TO 15
14 F=FS
  GMAG=GSMAG
  DO 140 I=1,4
  X(I)=XS(I)
140 G(I)=GS(I)
  DO 141 I=1,3
  UVI(I)=UVIS(I)
  UVM(I)=UVMS(I)
  DUVI(I)=DUVIS(I)
  DUVMM(I)=DUVMS(I)
  DUVMP(I)=DUVMP(I)

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RSVMD(I)=RSVMS(I)
VSVMRD(I)=VSVMPS(I)
DO 141 J=1,3
SFM11D(I,J)=SFM11S(I,J)
141 SFM12D(I,J)=SFM12S(I,J)
15 CONTINUE
16 DO 161 I=1,3
RSVM(I)=RSVMD(I)
VSVMR(I)=VSVMRD(I)
DO 161 J=1,3
SFM11(I,J)=SFM11D(I,J)
161 SFM12(I,J)=SFM12D(I,J)
WRITE(6,118)X,F,GMAG,G,RSVMD,VSVMRD
WRITE(6,107)((V(I,J),J=1,4),I=1,4)
IF(GMAG.LT.EPS)GO TO 18
IF(ITERD.LT.ITDMAX)GO TO 5
WRITE(6,119)
18 IPV=1
IPTRAJ=1
IFILE=IFILEX
WRITE(6,120)
C. GENERATE OPTIMAL TRAJECTORY AND PRIMER VECTOR HISTORY.
DO 30 I=1,3
PVO(I)=UVI(I)
PVO(I+3)=DUVI(I)
PVM(I)=UVM(I)
PVM(I+3)=DUVMP(I)
30 VSVI(I)=X(I)
CALL FOURBY(TSTART,X(4),RSVO,VSVI,RSEO,VSEO,
1RSMO,VSMO,PVO,RSVM,VSVMM,RSEM,VSEM,RSMM,VSMM,SMI11,SMI12,
2SMI21,SMI22)
CALL FOURBY(X(4),TEND,RSVM,VSVMP,RSEM,VSEM,RSMM,VSMM,
1PVM,RSVF,VSVF,RSEF,VSEF,RSMF,VSMF,SFM11,SFM12,SFM21,SFM22)
100 FORMAT(4D20.11)
101 FORMAT(6I5)
102 FORMAT(1H0,40X,'4-BODY 3-IMPULSE BOUNDARY VALUE PROBLEM'/
11H0,T8,'GL1',T28,'AUM',T48,'UTIME',T68,'UVELM',T88,'ERRMXM',
2T108,'ERRMAX'/1H ,1P6D20.11/1H ,T8,'MS',T28,'ME',T48,'MM'/1H ,
31P3D20.11)
103 FORMAT(1H ,T8,'TSTART',T28,'TM',T48,'TEND'/1H ,1P3D20.11/1H ,
1T8,'RSVO',T68,'VSVO'/1H ,1P6D20.11/1H ,T8,'RSEO',T68,'VSEO'/
21H ,1P6D20.11/1H ,T8,'RSMO',T68,'VSMO'/1H ,1P6D20.11)
104 FORMAT(1H0,T8,'VSVI',T68,'VSVMP'/1H ,1P6D20.11/1H ,T8,'RSVTAR',
1T68,'VSVTAR'/1H ,1P6D20.11)
105 FORMAT(1H0,T8,'KNR',T28,'ERRMIN',T48,'FMINM',T68,'EPS',T88,
1*EPSV'/1H ,1P5D20.11)
106 FORMAT(1H0,T8,'ICDMV',T28,'ITLMAX',T48,'ILINC',T68,'ITDMAX',T88,
1*IFILEX'/1H ,I10,4I20)
107 FORMAT(1H0,T8,'V'/1H ,1P6D20.11/1H ,1P6D20.11/1H ,1P4D20.11)
108 FORMAT(1H ,T8,'F',T28,'G',T108,'GMAG'/1H ,1P6D20.11)
109 FORMAT(1H1,T8,'ITERD'/1H ,I10)
110 FORMAT(1H0,T8,'S',T88,'SG'/1H ,1P5D20.11)
111 FORMAT(1H0,T8,'SIGNS OF S AND SG REVERSED'/1H ,T8,'S',T88,'SG'/
11H ,1P5D20.11)
112 FORMAT(1H0,T8,'DX',T88,'ALPHA'/1H ,1P5D20.11/1H ,T8,'XS'/1H ,
11H ,1P4D20.11)
113 FORMAT(1H ,T8,'FS',T28,'GS',T108,'GSMAG'/1H ,1P6D20.11)

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114 FORMAT(1H ,T8,'DG',T88,'P',T108,'SGS'/1H ,1P6D20.11/1H ,T8,
1'R',T88,'RMAG'/1H ,1P5D20.11)
115 FORMAT(1H0,T8,'CUBIC INTERPOLATION BETWEEN X AND XS'/1H0,T8,
1'DXC',T88,'ALPHAC'/1H ,1P5D20.11/1H ,T8,'XC'/1H ,1P4D20.11)
116 FORMAT(1H ,T8,'FC',T28,'GC',T108,'GCMAG'/1H ,1P6D20.11)
117 FORMAT(1H ,T8,'DGC',T88,'PC'/1H ,1P5D20.11/1H ,T8,'RC',T88,
1'RCMAG'/1H ,1P5D20.11)
118 FORMAT(1H0,T8,'OUTPUT OF THIS ITERATION'/1H0,T8,'X',T88,'F',
1T108,'GMAG'/1H ,1P6D20.11/1H ,T8,'G'/1H ,1P4D20.11/1H ,T8,
2'RSVMD',T68,'VSVPD'/1H ,1P6D20.11)
119 FORMAT(1H0,T8,'NO. OF DAVIDON ITERATIONS HAS REACHED MAXIMUM')
120 FORMAT(1H1)
121 FORMAT(1H0,T8,'SGS'/1H ,1P1D20.11)
122 FORMAT(1H0,T8,'RESTART WITH IDENTITY V MATRIX SCALED BY EPSV')
RETURN
END
```

C  
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Q  
**PROGRAM PTP3I3**

PROGRAM COMPUTES FUEL OPTIMAL 3-IMPULSE TRANSFER FROM A GIVEN INITIAL POSITION TO A GIVEN FINAL POSITION AND VELOCITY IN FIXED TIME.

IMPLICIT REAL\*8(A-H,K-M,O-Z)  
DIMENSION X(4),G(4),V(4,4),XS(4),GS(4),R(4),DX(4),REVO(3),  
1VEVO(3),REMO(3),VEMO(3),VEVOP(3),TEMP1(4,4),SFM11S(3,3),  
2SFM12S(3,3),SFM21S(3,3),SFM22S(3,3),SMI11S(3,3),SMI12S(3,3),  
3SMI21S(3,3),SMI22S(3,3),REVM(3),VEVMP(3),REVMS(3),VEVMPS(3),  
4DUVIS(3),DUVMMMS(3),DUVMP(3),DG(4),VS(4,4),DXC(4),XC(4),  
5REVMC(3),VEVMPC(3),UVIC(3),UVMC(3),UVFC(3),DUVIC(3),DUVMMC(3),  
6DUVMP(3),RC(4),SMI11C(3,3),SMI12C(3,3),SMI21C(3,3),SMI22C(3,3),  
7SFM11C(3,3),SFM12C(3,3),SFM21C(3,3),SFM22C(3,3),REVMD(3),  
8VEVMPD(3),UVIS(3),UVMS(3),UVFS(3),S(4),SFM11(3,3),SFM12(3,3),  
9SFM21(3,3),SFM22(3,3),UVI(3),UVM(3),UVF(3),DUVI(3),DUVMM(3),  
1DUVMP(3),SMI11(3,3),SMI12(3,3),SMI21(3,3),SMI22(3,3),PVO(6),  
2PVM(3),REVTAR(3),VEVTAR(3),SFM11D(3,3),SFM12D(3,3),DGC(4),  
3VC(4,4),GC(4),VEVMM(3),REMM(3),VEMM(3),REVF(3),VEVF(3),REM(3),  
4VEMF(3),VEVMMMS(3),VEVM(3)

COMMON/CONST3/ME,MM,GAMMA,UDM,UTIME,UVELM,ERRMAX,DTR

COMMON/FLAG/IMTX,IPV,IPTRAJ,IPVTM,IFILE,ITER,ITAR

READ(5,100)GAMMA,UDM,UTIME,UVELM

READ(5,100)ME,MM

READ(5,100)TSTART,TM,TEND

READ(5,100)REMO,VEMO

READ(5,100)REVO,VEVO

READ(5,100)VEVOP,VEVMP

READ(5,100)REVTAR,VEVTAR

READ(5,100)KNR,ERRMIN,ERRMXM

READ(5,100)FMINM,EPS,EPSV

READ(5,101)ICOMV,ITLMAX,ILINC,ITDMAX,IFILEX

IF(ICOMV.GT.0)GO TO 190

OPTION TO INPUT VARIANCE MATRIX(I=COMV=0)

READ(5,100)((V(I,J),J=1,4),I=1,4)

GO TO 1

190 DO 200 I=1,4

DO 200 J=1,4

V(I,J)=0.

IF(I.EQ.J)V(I,J)=1.0

200 CONTINUE

1 DTR=1.7453292519943296D-2

ERRMAX=ERRMXM/UDM

FMIN=FMINM\*UVELM

KNRSAV=KNR

ALPMIN=1.0D-8

WRITE(6,102)GAMMA,UDM,UTIME,UVELM,ERRMXM,ERRMAX,ME,MM

WRITE(6,103)TSTART,TM,TEND,REVO,VEVO,REMO,VEMO

WRITE(6,104)VEVOP,VEVMP,REVTAR,VEVTAR

WRITE(6,105)KNR,ERRMIN,FMINM,EPS,EPSV

WRITE(6,106)ICOMV,ITLMAX,ILINC,ITDMAX,IFILEX

IPV=0

IPVTM=0

IFILE=0

IPTRAJ=0

IMTX=1

ITERD=0

DO 2 I=1,3

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2 X(I)=VEVOP(I)
X(4)=TM
C COMPUTE INITIAL NOMINAL TRAJECTORY
CALL COMF3(TSTART,TM,TEND,REVO,VEVO,VEVOP,REMO,VEMO,ERRMIN,
11LINC,KNRSAV,ITERD,ITLMAX,REVMD,VEVMPD,REVTAR,VEVTAR,SFM11D,
2SFM12D,REVMS,VEVMMS,VEVMPD,FS,UVIS,UVMS,UVFS,SMI11S,SMI12S,
3SMI121S,SMI22S,SFM11S,SFM12S,SFM21S,SFM22S)
CALL COMG(SMI11S,SMI12S,SMI21S,SMI22S,SFM11S,SFM12S,VEVMPD,VEVMMS,UVIS,
1UVMS,UVFS,DUVIS,DUVMMS,DUVMPD,GS)
GMAG=DSQRT(DOT(G,G,4))
WRITE(6,108)F,G,GMAG
DO 3 I=1,3
REVMD(I)=REVMS(I)
VEVMPD(I)=VEVMPD(I)
DO 3 J=1,3
SFM11D(I,J)=SFM11(I,J)
3 SFM12D(I,J)=SFM12(I,J)
IF(ICOMV.EQ.0)GO TO 40
C OPTION TO COMPUTE TRIAL VARIANCE MATRIX (ICOMV=1)
DO 4 I=1,4
DO 4 J=1,4
V(I,J)=V(I,J)*EPSV/GMAG
4 CONTINUE
40 WRITE(6,107)((V(I,J),J=1,4),I=1,4)
C ACCELERATED GRADIENT ITERATION LOOP
5 ITERD=ITERD+1
WRITE(6,109)ITERD
CALL MXV(V,G,S,4,4)
DO 50 I=1,4
50 S(I)=-S(I)
SG=DOT(S,G,4)
WRITE(6,110)S,SG
IF(SG.LT.0.1)GO TO 51
DO 52 I=1,4
52 S(I)=-S(I)
SG=-SG
WRITE(6,111)S,SG
51 ALP=(FMIN-F)/SG
ALPHA=DMIN1(1.0D+0,ALP)
6 DO 61 I=1,4
DX(I)=ALPHA*S(I)
61 XS(I)=X(I)+DX(I)
DO 62 I=1,3
62 VEVOP(I)=XS(I)
WRITE(6,112)DX,ALPHA,XS
CALL COMF3(TSTART,XS(4),TEND,REVO,VEVO,VEVOP,REMO,VEMO,ERRMIN,
11LINC,KNRSAV,ITERD,ITLMAX,REVMD,VEVMPD,REVTAR,VEVTAR,SFM11D,
2SFM12D,REVMS,VEVMMS,VEVMPD,FS,UVIS,UVMS,UVFS,SMI11S,SMI12S,
3SMI121S,SMI22S,SFM11S,SFM12S,SFM21S,SFM22S)
CALL COMG(SMI11S,SMI12S,SMI21S,SMI22S,SFM11S,SFM12S,VEVMPD,
1VEVMMS,UVIS,UVMS,UVFS,DUVIS,DUVMMS,DUVMPD,GS)
GSMAG=DSQRT(DOT(GS,GS,4))
WRITE(6,113)FS,GS,GSMAG
DO 701 I=1,4
701 DG(I)=GS(I)-G(I)
DO 7 I=1,3
REVMD(I)=REVMS(I)

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VEVMPD(I)=VEVMPS(I)
DO 7 J=1,3
SFM11D(I,J)=SFM11S(I,J)
7 SFM12D(I,J)=SFM12S(I,J)
CALL MXV(V,DG,R,4,4)
DO 71 I=1,4
71 R(I)=R(I)-DX(I)
RMAG=DSQRT(DOT(R,R,4))
P=DOT(DG,R,4)
PMAG=DABS(P)
SGS=DOT(S,GS,4)
WRITE(6,114)DG,P,SGS,R,RMAG
8 CALL VVT(R,TEMP1,4)
DO 81 I=1,4
DO 81 J=1,4
81 V(I,J)=V(I,J)-TEMP1(I,J)/P
82 IF(SGS.GT.0.)GO TO 83
IF(FS.LT.F)GO TO 14
ALPHA=ALPHA/10.0
IF(ALPHA.LT.ALPMIN)GO TO 84
GO TO 6
84 DO 840 I=1,4
DO 840 J=1,4
V(I,J)=0.
IF(I.EQ.J)V(I,J)=1.
840 V(I,J)=V(I,J)*EPSV/GMAG
WRITE(6,122)
GO TO 40
83 CONTINUE
CUBIC INTERPOLATION BETWEEN X AND XS
Z=3.*(F-FS)/ALPHA+SG+SGS
W2=Z*Z-SG*SGS
IF(W2.LE.0.)GO TO 13
W=DSQRT(W2)
ALPHAC=ALPHA*(1.-(SGS+W-Z)/(SGS-SG+2.*W))
DO 9 I=1,4
DXC(I)=ALPHAC*S(I)
9 XC(I)=X(I)+DXC(I)
DO 901 I=1,3
901 VEVOP(I)=XC(I)
WRITE(6,115)DXC,ALPHAC,XC
CALL COMF3(TSTART,XC(4),TEND,REVO,VEVO,VEVOP,REMO,VEMO,ERRMIN,
1ILINC,KNRSAV,ITERD,ITLMAX,REVMD,VEVMPD,REVSTAR,VEVTAR,SFM11D,
2SFM12D,REVMC,VEVMMC,VEVMPC,FC,UVIC,UVMC,UVFC,SMI11C,SMI12C,
3SMI121C,SMI122C,SFM11C,SFM12C,SFM21C,SFM22C)
CALL COMG(SMI11C,SMI12C,SMI21C,SMI22C,SFM11C,SFM12C,VEVMPC,
1VEVMMC,UVIC,UVMC,UVFC,DUVIC,DUVMMC,DUVMPC,GC)
GCMAG=DSQRT(DOT(GC,GC,4))
WRITE(6,116)FC,GC,GCMAG
DO 902 I=1,4
902 DGC(I)=GC(I)-G(I)
DO 91 I=1,3
REVMD(I)=REVMC(I)
VEVMPD(I)=VEVMPC(I)
DO 91 J=1,3
SFM11D(I,J)=SFM11C(I,J)
91 SFM12D(I,J)=SFM12C(I,J)

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CALL MXV(V,GC,RC,4,4)
DO 92 I=1,4
92 RC(I)=RC(I)-DXC(I)
RCMAG=DSQRT(DOT(RC,RC,4))
PC=DDT(DGC,RC,4)
CALL VVT(RC,TEMP1,4)
DO 93 I=1,4
DO 93 J=1,4
93 V(I,J)=V(I,J)-TEMP1(I,J)/PC
WRITE(6,117)DGC,PC,RC,RCMAG
IF(FS.GT.F)GO TO 11
IF(FC.GT.FS)GO TO 14
10 DO 20 I=1,4
X(I)=XC(I)
20 G(I)=GC(I)
DO 201 I=1,3
UVI(I)=UVIC(I)
UVM(I)=UVMC(I)
DUVIC(I)=DUVIC(I)
DUVMMC(I)=DUVMMC(I)
DUVMP(I)=DUVMP(I)
REVMD(I)=REVMC(I)
VEVMPD(I)=VEVMP(I)
DO 201 J=1,3
SFM11D(I,J)=SFM11C(I,J)
201 SFM12D(I,J)=SFM12C(I,J)
F=FC
GMAG=GCMAG
GO TO 16
11 IF(FC.LT.F)GO TO 10
FC GRTHN F. REPEAT INTERPOLATION IN REDUCED INTERVAL.
FS=FC
ALPHA=ALPHAC
DO 250 I=1,3
XS(I)=XC(I)
GS(I)=GC(I)
REVMS(I)=REVMC(I)
VEVMP(S(I))=VEVMP(I)
UVIS(I)=UVIC(I)
UVMS(I)=UVMC(I)
DUVIS(I)=DUVIC(I)
DUVMMMS(I)=DUVMMC(I)
DUVMP(S(I))=DUVMP(I)
DO 250 J=1,3
SFM11S(I,J)=SFM11C(I,J)
250 SFM12S(I,J)=SFM12C(I,J)
SGS=DOT(S,GS,4)
WRITE(6,121)SGS
GO TO 82
13 IF(FS.GT.F)GO TO 15
14 F=FS
GMAG=GSMAG
DO 140 I=1,4
X(I)=XS(I)
40 G(I)=GS(I)
DO 141 I=1,3
UVI(I)=UVIS(I)

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UVM(I)=UVMS(I)
DUVI(I)=DUVIS(I)
DUVMM(I)=DUVMS(I)
DUVMP(I)=DUVMP(S)
REVMD(I)=REVMS(I)
VEVMPD(I)=VEVMP(S)
DO 141 J=1,3
SFM11D(I,J)=SFM11S(I,J)
141 SFM12D(I,J)=SFM12S(I,J)
15 CONTINUE
16 DO 161 I=1,3
REV(M(I))=REVMD(I)
VEVMP(I)=VEVMPD(I)
DO 161 J=1,3
SFM11(I,J)=SFM11D(I,J)
161 SFM12(I,J)=SFM12D(I,J)
WRITE(6,118)X,F,G,GMAG,REVMD,VEVMPD
WRITE(6,107)((V(I,J),J=1,4),I=1,4)
IF(GMAG.LT.EPS)GO TO 18
IF(ITERD.LT.ITDMAX)GO TO 5
WRITE(6,119)
18 IPV=1
IPTRAJ=1
IFILE=IFILEX
WRITE(6,120)
C GENERATE OPTIMAL TRAJECTORY AND PRIMER VECTOR HISTORY
DO 30 I=1,3
PVO(I)=UVI(I)
PVO(I+3)=DUVI(I)
PVM(I)=UVM(I)
PVM(I+3)=DUVMP(I)
30 VEVOP(I)=X(I)
CALL THRBDY(TSTART,X(4),REVO,VEVOP,REMO,VEMO,PVO,REV(M),VEVMM,
1REMM,VEMM,SMI11,SMI12,SMI21,SMI22)
CALL THRBDY(X(4),TEND,REV(M),VEVMP,REMM,VEMM,PVM,REV(F),VEVF,REM(F),
1VEMF,SFM11,SFM12,SFM21,SFM22)
100 FORMAT(4D20.11)
101 FORMAT(6I5)
102 FORMAT(1H0,40X,'3-BODY 3-IMPULSE BOUNDARY VALUE PROBLEM'/
11H0,T8,'GAMMA',T28,'UDM',T48,'UTIME',T68,'UVELM',T88,'ERRMXM',
2T108,'ERRMAX'/1H ,1P6D20.11/1H ,T8,'ME',T28,'MM'/1H ,1P2D20.11)
103 FORMAT(1H ,T8,'TSTART',T28,'TM',T48,'TEND'/1H ,1P3D20.11/1H ,
1T8,'REVO',T68,'VEVO'/1H ,1P6D20.11/1H ,T8,'REMO',T68,'VEMO'/
21H ,1P6D20.11)
104 FORMAT(1H0,T8,'VEVOP',T68,'VEVMP'/1H ,1P6D20.11/1H ,T8,'REV TAR',
1T68,'VEVTAR'/1H ,1P6D20.11)
105 FORMAT(1H0,T8,'KNR',T28,'ERRMIN',T48,'FMINM',T68,'EPS',T88,
1'EPSV'/1H ,1P5D20.11)
106 FORMAT(1H0,T8,'ICOMV',T28,'ITLMAX',T48,'ILINC',T68,'ITDMAX',T88,
1'IFILEX'/1H ,I10,4I20)
107 FORMAT(1H0,T8,'V'/1H ,1P6D20.11/1H ,1P6D20.11/1H ,1P4D20.11)
108 FORMAT(1H ,T8,'F',T28,'G',T108,'GMAG'/1H ,1P6D20.11)
109 FORMAT(1H1,T8,'ITERD'/1H ,I10)
110 FORMAT(1H0,T8,'S',T88,'SG'/1H ,1P5D20.11)
111 FORMAT(1H0,T8,'SIGNS OF S AND SG REVERSED'/1H ,T8,'S',T88,'SG'/
11H ,1P5D20.11)
112 FORMAT(1H0,T8,'DX',T88,'ALPHA'/1H ,1P5D20.11/1H ,T8,'XS'/1H ,

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```
11H ,1P4D20.11)
113 FORMAT(1H ,T8,'FS',T28,'GS',T108,'GSMAG'/1H ,1P6D20.11)
114 FORMAT(1H ,T8,'DG',T88,'P',T108,'SGS'/1H ,1P6D20.11/1H ,T8,
   1'R',T88,'RMAG'/1H ,1P5D20.11)
115 FORMAT(1H0,T8,'CUBIC INTERPOLATION BETWEEN X AND XS'/1H0,T8,
   1'DXC',T88,'ALPHAC'/1H ,1P5D20.11/1H ,T8,'XC'/1H ,1P4D20.11)
116 FORMAT(1H ,T8,'FC',T28,'GC',T108,'GCMAG'/1H ,1P6D20.11)
117 FORMAT(1H ,T8,'DGC',T88,'PC'/1H ,1P5D20.11/1H ,T8,'RC',T88,
   1'RCMAG'/1H ,1P5D20.11)
118 FORMAT(1H0,T8,'OUTPUT OF THIS ITERATION'/1H0,T8,'X',T88,'F',
   1T108,'GMAG'/1H ,1P6D20.11/1H ,T8,'REVMD',T68,'VEVMPD'/1H ,
   21P6D20.11)
119 FORMAT(1H0,T8,'NO. OF DAVIDON ITERATIONS HAS REACHED MAXIMUM')
120 FORMAT(1H1)
121 FORMAT(1H0,T8,'SGS'/1H ,1P1D20.11)
122 FORMAT(1H0,T8,'RESTART WITH IDENTITY V MATRIX SCALED BY EPSV')
      RETURN
      END
```

```

SUBROUTINE FOURBY(XTO,XTF,RSVO,VSVO,RSE0,VSE0,RSMO,
1VSMO,PVO,RSVD,VSVD,RSED,VSED,RSMD,VSMD,S11,S12,S21,S22)
IMPLICIT REAL*8(A-H,L-M,O-Z)
DIMENSION RSV(3),VSV(3),RSE(3),VSE(3),RSM(3),VSM(3),PVO(6),
1S11(3,3),S12(3,3),S21(3,3),S22(3,3),REV(3),VEV(3),RMV(3),VMV(3),
2REM(3),VEM(3),DR4RSV(3),DR4RSE(3),DR4RSM(3),BIGJ(6,6),STM(6,6),
3STNTM(6,6),MTXSV(6,6),MTXEV(6,6),MTXMV(6,6),MTXSE(6,6),
4MTXSM(6,6),MTXEM(6,6),DRSV(3),DVSV(3),DRSE(3),DVSE(3)
DIMENSION RSV0(3),VSVO(3),RSE0(3),VSE0(3),RSM0(3),VSM0(3)
DIMENSION RTM(3),DRSM(3),DVSM(3),DREV(3),DVEV(3),DRMV(3),
1DVMV(3),DREM(3),DVEM(3),CRSV(3),CVSV(3),CRSE(3),CVSE(3),CRSM(3),
2CVSM(3),CREV(3),CVEV(3),CRMV(3),CVMV(3),CREM(3),CVEM(3),PRSV(3),
3,PVSV(3),PRSE(3),PVSE(3),PRSM(3),PVSM(3),RRSV(3),RVSV(3),
4RRSE(3),RVSE(3),RRSM(3),RVSM(3),STMH(6,6),TEMP(6,6)
DIMENSION VTM(3),PVTM(3),PVDTM(3),PV(6)
DIMENSION RDV(3),VDV(3),RDS(3),VDS(3),RDE(3),VDE(3),RDM(3),
1VDM(3),RDVD(3),VDVD(3),RDSD(3),VDS(3),RDMD(3),
2VDMD(3),RSVD(3),VSVD(3),RSED(3),VSED(3),RSMD(3),VSMD(3),RSL1(3),
3VSL1(3),RDL1(3),VDL1(3),RDL1D(3),VDL1D(3)
COMMON/TDATA/T0,T,H,RSV,VSV,REV,VEV,RMV,VMV,RSE,VSE,RSM,VSM,
1REM,VEM,RSL1,VSL1,RDVD,VDVD,RDSD,VDS(3),RDMD,VDMD,
2RDL1D,VDL1D,PV,LM,LDM,ANGV,ANGE,ANGS
COMMON/CONST/MS,ME,MM,GL1,AUM,UTIME,UVELM,ERRMAX,DTR
COMMON/FLAG/IMTX,IPV,IPTRAJ,IPVTM,IFILE,ITER,ITAR
COMMON/CTM/TTM,RTM,VTM,LTM,LDTM,PVTM,PVDTM,STNTM
DO 1 I=1,3
RSV(I)=RSVO(I)
VSV(I)=VSVO(I)
RSE(I)=RSE0(I)
VSE(I)=VSE0(I)
RSM(I)=RSMO(I)
1 VSM(I)=VSM0(I)
TO=XTO
MSME=MS+ME
MSMM=MS+MM
MEMM=ME+MM
ESE=ME/MSME
MSM=MM/MSMM
MEM=MM/MEMM
EEM=ME/MEMM
SSE=MS/MSME
SSM=MS/MSMM
PSISV=0.
PSISE=0.
PSISM=0.
PSIEV=0.
PSIMV=0.
PSIEM=0.
LM=0.
LDM=0.
CALL RVEMV(RSV,VSV,RSE,VSE,RSM,VSM,REV,VEV,RMV,VMV,REM,VEM)
IF (IMTX.EQ.0) GO TO 2
DO 2 I=1,6
PV(I)=0.
DO 2 J=1,6
STM(I,J)=0.
IF (I.EQ.J) STM(I,J)=1.0

```

```

2 CONTINUE
 1STEP=0
  T=XTO
  TGO=XTF-T
  CALL CSTEP(TGO,RSV,REV,RMV,RSE,RSM,REM,H,DR4RSV,DR4RSE,
 1DR4RSM,BIGJ)
  CALL DISP
  IF(IPV.EQ.0) GO TO 21
  LTM=1.
  TTM=XTO
  CALL PVEC(T,RSV,VSV,PVO,STM,PV,LM,LDM)
21 IF(IFILE.EQ.0) GO TO 22
  CALL FDATA
22 IF(IPTRAJ.EQ.0) GO TO 3
  WRITE(6,100)
  IF(IPV.EQ.0) GO TO 23
  WRITE(6,101)
23 CALL PTRAJ
3 1STEP=1STEP+1
  CALL TWOBDY(RSV,VSV,H,MS,PSISV,IMTX,CRSV,CVSV,MTXSV)
  CALL TWOBDY(RSE,VSE,H,MSME,PSISE,O,CRSE,CVSE,MTXSE)
  CALL TWOBDY(RSM,VSM,H,MSMM,PSISM,O,CRSM,CVSM,MTXSM)
  CALL TWOBDY(REV,VEV,H,ME,PSIEV,IMTX,CREV,CVEV,MTXEV)
  CALL TWOBDY(RMV,VMV,H,MM,PSIMV,IMTX,CRMV,CVMV,MTXMV)
  CALL TWOBDY(REM,VEM,H,MEMM,PSIEM,O,CREM,CVEM,MTXEM)
  DO 4 I=1,3
    DRSV(I)=CRSV(I)-RSV(I)-H*VSV(I)
    DVSV(I)=CVSV(I)-VSV(I)
    DRSE(I)=CRSE(I)-RSE(I)-H*VSE(I)
    DVSE(I)=CVSE(I)-VSE(I)
    DRSM(I)=CRSM(I)-RSM(I)-H*VSM(I)
    DVSM(I)=CVSM(I)-VSM(I)
    DREV(I)=CREV(I)-REV(I)-H*VEV(I)
    DVEV(I)=CVEV(I)-VEV(I)
    DRMV(I)=CRMV(I)-RMV(I)-H*VMV(I)
    DVMV(I)=CVMV(I)-VMV(I)
    DREM(I)=CREM(I)-REM(I)-H*VEM(I)
    DVEM(I)=CVEM(I)-VEM(I)
    PRSV(I)=ESE*DRSE(I)+DREV(I)+MSM*DRSM(I)+DRMV(I)
    PVSV(I)=ESE*DVS E(I)+DVEV(I)+MSM*DVS M(I)+DVMV(I)
    PRSE(I)=MSM*DRSM(I)-MEM*DREM(I)
    PVSE(I)=MSM*DVS M(I)-MEM*DDEM(I)
    PRSM(I)=ESE*DRSE(I)+EEM*DREM(I)
    PVSM(I)=ESE*DVS E(I)+EEM*DDEM(I)
    RSV(I)=CRSV(I)+PRSV(I)
    VSV(I)=CVSV(I)+PVSV(I)
    RSE(I)=CRSE(I)+PRSE(I)
    VSE(I)=CVSE(I)+PVSE(I)
    RSM(I)=CRSM(I)+PRSM(I)
4  VSM(I)=CVSM(I)+PVSM(I)
  CALL RVEMV(RSV,VSV,RSE,VSE,RSM,VSM,REV,VEV,RMV,VMV,REM,VEM)
  T=T+H
  CALL DELRV(H,RSV,REV,RMV,RSE,RSM,REM,CRSV,CREV,CRMV,CRSE,CRSM,
 1CREM,DR4RSV,DR4RSE,DR4RSM,RRSV,RVSV,RRSE,RVSE,RRSM,RVSM)
  DO 5 I=1,3
    RSV(I)=RSV(I)+RRSV(I)
    VSV(I)=VSV(I)+RVSV(I)

```

```

RSE(I)=RSE(I)+RRSE(I)
VSE(I)=VSE(I)+RVSE(I)
RSM(I)=RSM(I)+RRSM(I)
15 VSM(I)=VSM(I)+RVSM(I)
CALL RVEMV(RSV,VSV,RSE,VSE,RSM,VSM,REV,VEV,RMV,VMV,REM,VEM)
IF(1MTX.EQ.0) GO TO 70
DO 6 I=1,6
DO 6 J=1,6
6 STMH(I,J)=MTXSV(I,J)+MTXEV(I,J)+MTXMV(I,J)-2.0*BIGJ(I,J)
CALL MXM(STMH,STM,TEMP,6,6,6)
DO 7 J=1,6
DO 7 J=1,6
7 STM(I,J)=TEMP(I,J)
70 CALL DISP
IF(IPV.EQ.0) GO TO 71
CALL PVEC(T,RSV,VSV,PVO,STM,PV,LM,LDM)
71 IF(IFILE.EQ.0) GO TO 72
CALL FDATA
72 IF(IPTRAJ.EQ.0) GO TO 8
CALL PTRAJ
8 IF (T.GE.XTF) GO TO 9
TGO=XTF-T
CALL CSTEP(TGO,RSV,REV,RMV,RSE,RSM,REM,H,DR4RSV,DR4RSE,
1DR4RSM,BIGJ)
GO TO 3
9 DO 10 I=1,3
RSVD(I)=RSV(I)
VSVD(I)=VSV(I)
RSED(I)=RSE(I)
VSED(I)=VSE(I)
RSMD(I)=RSM(I)
VSMD(I)=VSM(I)
DO 10 J=1,3
S11(I,J)=STM(I,J)
S12(I,J)=STM(I,J+3)
S21(I,J)=STM(I+3,J)
10 S22(I,J)=STM(I+3,J+3)
IF(IPV.EQ.0) GO TO 11
IF(IPVTM.EQ.0) GO TO 11
WRITE(6,102)TTM,LTM,LDTM,RTM,VTM
11 IF(IPTRAJ.EQ.0) GO TO 12
WRITE(6,103)ISTEP
12 CONTINUE
100 FORMAT(1H1,40X,'FOUR-BODY TRAJECTORY'/1H0,T8,'T',T28,'TDAY',
1T48,'H',T68,'RSVMAG',T88,'REVMAG',T108,'RMVMAG'/1H ,T8,'RSV',
2T68,'VSV'/1H ,T8,'REV',T68,'VEV'/1H ,T8,'RMV',T68,'VMV'/1H0,T8,
3'RSE',T68,'VSE'/1H ,T8,'RSM',T68,'VSM'/1H ,T8,'REM',T68,'VEM'/
4H ,T8,'RSL1',T68,'VSL1'/1H0,T8,'RDVD',T68,'VDVD'/1H ,T8,'RDSD',
5T68,'VDSD'/1H ,T8,'RDMD',T68,'VDM'D/
61H ,T8,'RDL1D',T68,'VDL1D'/1H0,T8,'ANGV',T28,'ANGE',T48,'ANGS',
61H0,T8,'RDL1D',T68,'VDL1D'/1H ,T8,'ANGV',T28,'ANGE',T48,'ANGS',
7T68,'HDAY')
101 FORMAT(1H ,T8,'PV',T68,'PVD'/1H ,T8,'PVMAG',T28,'PVDMAG')
102 FORMAT(1H0,'TIME OF MAXIMUM PRIMER VECTOR MAGNITUDE'/1H0,T8,
1'TTM',T28,'LTM',T48,'LDTM'/1H ,1P3D20.11/1H ,T8,'RTM',T68,'VTM'
2/1H ,1P6D20.11)
103 FORMAT(1H0,T8,'ISTEP FOR THIS LEG = ',15)

```

**RETURN  
END**

```

SUBROUTINE THRBDY(XTO,XTF,REVO,VEVO,REMO,VEMO,PVO,REVD,VEVD,
1REM,VEMD,S11,S12,S21,S22)
IMPLICIT REAL*8(A-H,L-M,O-Z)
DIMENSION REVO(3),VEVO(3),REMO(3),VEMO(3),PVO(6),REVD(3),VEVD(3),
1,REM(3),VEMD(3),S11(3,3),S12(3,3),S21(3,3),S22(3,3),REV(3),
2VEV(3),REM(3),VEM(3),RMV(3),VMV(3),PV(6),STM(6,6),DR4REV(3),
3BIGJ(6,6),CREV(3),CVEV(3),MTXEV(6,6),CREM(3),CVEM(3),MTXEM(6,6),
4CRMV(3),CVMV(3),MTXMV(6,6),DRMV(3),DVMV(3),
5PREV(3),PVEV(3),RREV(3),RVEV(3),STMH(6,6),TEMP(6,6),REL(3),
6VEL(3),RDVD(3),VDVD(3),RDED(3),VDED(3),RDLD(3),VDLD(3)
DIMENSION RTM(3),VTM(3),PVTM(3),PVDTM(3),STNTM(6,6)
COMMON/TDATA3/T0,T,H,REV,VEV,RMV,VMV,REM,VEM,REL,VEL,RDVD,
1VDVD,RDED,VDED,RDLD,VDLD,PV,LM,LDM,ANGV,ANGE,ANGM
COMMON/CONST3/ME,MM,GAMMA,UDM,UTIME,UVELM,ERRMAX,DTR
COMMON/FLAG/IMTX,IPV,IPTRAJ,IPVTM,IFILE,ITER,ITAR
COMMON/CTM/TTM,RTM,VTM,LTM,LDTM,PVTM,PVDTM,STNTM
DO 1 I=1,3
REV(I)=REVO(I)
VEV(I)=VEVO(I)
REM(I)=REMO(I)
VEM(I)=VEMO(I)
RMV(I)=-REM(I)+REV(I)
1 VMV(I)=-VEM(I)+VEV(I)
T0=XTO
MEMM=ME+MM
MEM=MM/MEMM
PSIEV=0.
PSIEM=0.
PSIMV=0.
LM=0.
LDM=0.
IF(IMTX.EQ.0)GO TO 2
DO 2 I=1,6
PV(I)=0.
DO 2 J=1,6
STM(I,J)=0.
IF(I.EQ.J)STM(I,J)=1.0
2 CONTINUE
ISTEP=0
T=XTO
TGO=XTF-T
CALL CSTEP3(TGO,REV,RMV,REM,H,DR4REV,BIGJ)
CALL DISP3
IF(IPV.EQ.0) GO TO 21
LTM=1.0
TTM=XTO
CALL PVEC(T,REV,VEV,PVO,STM,PV,LM,LDM)
21 IF(IFILE.EQ.0) GO TO 22
CALL FDATA3
22 IF(IPTRAJ.EQ.0) GO TO 3
WRITE(6,100)
IF(IPV.EQ.0) GO TO 23
WRITE(6,101)
23 CALL PTRAJ3
3 ISTEP=ISTEP+1
CALL TWOBDY(REV,VEV,H,ME,PSIEV,IMTX,CREV,CVEV,MTXEV)
CALL TWOBDY(REM,VEM,H,MEMM,PSIEM,0,CREM,CVEM,MTXEM)

```

```

CALL TWOBODY(RMV,VMV,H,MM,PSIMV,IMTX,CRMV,CVMV,MTXMV)
DO 4 I=1,3
DRMV(I)=CRMV(I)-RMV(I)-H*VMV(I)
DVMV(I)=CVMV(I)-VMV(I)
PREV(I)=DRMV(I)
PVEV(I)=DVMV(I)
REV(I)=CREV(I)+PREV(I)
VEV(I)=CVEV(I)+PVEV(I)
REM(I)=CREM(I)
VEM(I)=CVEM(I)
RMV(I)=-REM(I)+REV(I)
4 VMV(I)=-VEM(I)+VEV(I)
T=T+H
CALL DELRV3(H,REV,RMV,CREV,CRMV,DR4REV,RREV,RVEV)
DO 5 I=1,3
REV(I)=REV(I)+RREV(I)
VEV(I)=VEV(I)+RVEV(I)
RMV(I)=-REM(I)+REV(I)
5 VMV(I)=-VEM(I)+VEV(I)
IF(1MTX.EQ.0) GO TO 70
DO 6 I=1,6
DO 6 J=1,6
6 STMH(I,J)=MTXEV(I,J)+MTXMV(I,J)-2.0*BIGJ(I,J)
CALL MXM(STMH,STM,TEMP,6,6,6)
DO 7 I=1,6
DO 7 J=1,6
7 STM(I,J)=TEMP(I,J)
70 CALL DISP3
IF(IPV.EQ.0) GO TO 71
CALL PVEC(T,REV,VEV,PVO,STM,PV,LM,LDM)
71 IF(IFILE.EQ.0) GO TO 72
CALL FDATA3
72 IF(IPTRAJ.EQ.0) GO TO 8
CALL PTRAJ3
8 IF(T.GE.XTF) GO TO 9
TGO=XTF-T
CALL CSTEP3(TGO,REV,RMV,REM,H,DR4REV,BIGJ)
GO TO 3
9 DO 10 I=1,3
REVD(I)=REV(I)
VEVD(I)=VEV(I)
REMD(I)=REM(I)
VEMD(I)=VEM(I)
DO 10 J=1,3
S11(I,J)=STM(I,J)
S12(I,J)=STM(I,J+3)
S21(I,J)=STM(I+3,J)
10 S22(I,J)=STM(I+3,J+3)
IF(IPV.EQ.0) GO TO 11
IF(IPVTM.EQ.0) GO TO 11
WRITE(6,102) TTM,LTM,LDTM,RTM,VTM
11 IF(IPTRAJ.EQ.0) GO TO 12
WRITE(6,103)ISTEP
12 CONTINUE
100 FORMAT(1H1,40X,'THREE-BODY TRAJECTORY'/1H0,T8,'T',T28,'TDAY',
1T48,'H',T68,'REVMAG',T88,'RMVMAG'/1H ,T8,'REV',T68,'VEV'/
21H ,T8,'RMV',T68,'VMV'/1H ,T8,'REM',T68,'VEM'/1H ,T8,'REL1',

```

3T68,'VEL1'/1H0,T8,'RDVD',T68,'VDVD'/1H ,T8,'RDED',T68,'VDED'/  
41H ,T8,'RDLD',T68,'VDLD'/1H ,T8,'ANGV',T28,'ANGE',T48,'ANGM')  
101 FORMAT(1H0,T8,'PV',T68,'PVD'/1H ,T8,'PVMAG',T28,'PVDMAG')  
12 FORMAT(1H0,T8,'TIME OF MAXIMUM PRIMER VECTOR MAGNITUDE'/1H0,  
1T8,'TTM',T28,'LTM',T48,'LDTM'/1H ,1P3D20.11/1H ,T8,'RTM',T68,  
2'VTM'/1H ,1P6D20.11)  
103 FORMAT(1H0,T8,'ISTEP FOR THIS LEG V ',15)  
RETURN  
END

```
SUBROUTINE TWOBODY(XR0,XV0,TAU,MU,PSI,IMTX,XRF,XVF,P)
```

```
C GENERAL SOLUTION OF TWO BODY PROBLEM WITH PARTIAL DERIVATIVES  
C RTRAN DOUBLE PRECISION SUBROUTINE
```

```
DOUBLE PRECISION SO(6),TAU,MU,PSI,S(6),P(6,6),PI(6,6),ACC(3),  
1ACCO(3),R,RO,SIG0,ALPHA,PSIN,PSIP,A,AP,C0,C1,C2,  
2C3,C4,C5X3,S1,S2,S3,DTAUN,DTAUP,U,FM1,G,FD,GDM1  
DOUBLE PRECISION XRO(3),XVO(3),XRF(3),XVF(3)
```

```
C           INPUTS
```

```
C SO(1),SO(2),SO(3)=X0,Y0,Z0=POSITION COMPONENTS AT REFERENCE TIME TO  
C SO(4),SO(5),SO(6)=X00,Y00,Z00=VELOCITY COMPONENTS AT REFERENCE TIME TO  
C TAU=TIME INTERVAL (T-T0) FROM REFERENCE TIME TO TO SOLUTION TIME T  
C MU=CONSTANT IN DIFF. EQS. (XDD,YDD,ZDD)=-MU*(X,Y,Z)/(R**3)  
C PSI=APPROXIMATION FOR FINAL SOLUTION PSI OF KEPLER'S EQUATION
```

```
C           OUTPUTS
```

```
C PSI=GENERALIZED ECCENTRIC ANOMALY=SOLUTION OF KEPLER'S EQUATION  
C S(1),S(2),S(3)=X,Y,Z=POSITION COMPONENTS AT SOLUTION TIME T=T0+TAU  
C S(4),S(5),S(6)=XD,YD,ZD=VELOCITY COMPONENTS AT SOLUTION TIME T=T0+TAU  
C P(I,J)=PARTIAL DERIVATIVE DS(I)/DS0(J) OF S(I) WITH RESPECT TO SO(J)  
C PI(I,J)=PARTIAL DS0(I)/DS(J) WITH ROLES OF T0 AND T REVERSED  
C ACC(1)=-MU*S(I)/(R**3)=ACCELERATION COMPONENT AT SOLUTION TIME T  
C ACC0(I)=-MU*SO(I)/(R0**3)=ACCELERATION COMPONENT AT REF TIME T0  
C R=RADIUS AT TIME T=SQUARE ROOT OF (X**2+Y**2+Z**2)  
C R0=RADIUS AT TIME T0
```

```
C START OF INITIAL COMPUTATIONS
```

```
DO 9 I=1,3
```

```
    SO(I)=XRO(I)
```

```
9   SO(I+3)=XVO(I)
```

```
C COMPUTE RADIUS R0
```

```
S1=DMAX1(DABS(SO(1)),DABS(SO(2)),DABS(SO(3)))
```

```
S2=(SO(1)/S1)**2+(SO(2)/S1)**2+(SO(3)/S1)**2
```

```
R0=2.
```

```
10  R=R0
```

```
R0=(R+S2/R)*.5
```

```
IF(R0.LT.R) GO TO 10
```

```
R0=R0*S1
```

```
C COMPUTE OTHER PARAMETERS
```

```
SIG0=SO(1)*SO(4)+SO(2)*SO(5)+SO(3)*SO(6)
```

```
ALPHA=SO(4)**2+SO(5)**2+SO(6)**2-2.*MU/R0
```

```
C INITIALIZE SERIES MOD COUNT M TO ZERO
```

```
M=0
```

```
C INITIALIZE BOUNDS PSIN AND PSIP FOR PSI OR SET PSI=0 IF TAU=0
```

```
IF(TAU).LT.20,30,40
```

```
20  PSIN=-1.D+38
```

```
PSIP=0.
```

```
DTAUN=PSIN
```

```
DTAUP=-TAU
```

```
GO TO 50
```

```
30  PSI=0.
```

```
GO TO 100
```

```
40  PSIN=0.
```

```
PSIP=+1.D+38
```

```
DTAUN=-TAU
```

```
DTAUP=PSIP
```

```
C USE APPROXIMATION FOR PSI IF IT IS BETWEEN BOUNDS PSIN AND PSIP
```

```

50 IF(PSI.GT.PSIN.AND.PSI.LT.PSIP) GO TO 100
C TRY NEWTON'S METHOD FOR INITIAL PSI SET EQUAL TO ZERO
  PSI=TAU/R0
C IF PSI=TAU IF NEWTON'S METHOD FAILS
  IF(PSI.LE.PSIN.OR.PSI.GE.PSIP) PSI=TAU
C END OF INITIAL COMPUTATIONS
C
C BEGINNING OF LOOP FOR SOLVING KEPLER'S EQUATION
C BEGINNING OF SERIES SUMMATION
C COMPUTE ARGUMENT A IN REDUCED SERIES OBTAINED BY FACTORING OUT PSI'S
100 A=ALPHA*PSI*PSI
    IF(DABS(A).LE.1.) GO TO 120
C SAVE A IN AP AND MOD A IF IT EXCEEDS UNITY IN MAGNITUDE
  AP=A
110 M=M+1
  A=A*.25
  IF(DABS(A).GT.1.) GO TO 110
C SUM SERIES C5X3=3*S5/PSI**5 AND C4=S4/PSI**4
120 C5X3=(1.+(1.+(1.+(1.+(1.+(1.+A/342.)*A/272.)*A/210.)*A/156.)*
           1.*A/110.)*A/72.)*A/42.)/40.
  C4=(1.+(1.+(1.+(1.+(1.+A/306.)*A/240.)*A/182.)*A/132.)*
           1.*A/90.)*A/56.)*A/30.)/24.
C COMPUTE SERIES C3=S3/PSI**3,C2=S2/PSI**2,C1=S1/PSI,C0=S0
  C3=(.5+A*C5X3)/3.
  C2=.5+A*C4
  C1=1.+A*C3
  C0=1.+A*C2
  IF(M.LE.0) GO TO 140
C DEMOD SERIES C0 AND C1 IF NECESSARY WITH DOUBLE ANGLE FORMULAS
  30 C1=C1*C0
  C0=2.*C0*C0-1.
  M=M-1
  IF(M.GT.0) GO TO 130
C DETERMINE C2,C3,C4,C5X3 FROM C0,C1,AP IF DEMOD REQUIRED
  C2=(C0-1.)/AP
  C3=(C1-1.)/AP
  C4=(C2-.5)/AP
  C5X3=(3.*C3-.5)/AP
C COMPUTE SERIES S1,S2,S3 FROM C1,C2,C3
  140 S1=C1*PSI
      S2=C2*PSI*PSI
      S3=C3*PSI*PSI*PSI
C END OF SERIES SUMMATION
C COMPUTE RESIDUAL DTAU AND SLOPE R FOR KEPLER'S EQUATION
  G=R0*S1+SIG0*S2
  DTAU=(G+MU*S3)-TAU
  R=DABS(R0*C0+(SIG0*S1+MU*S2))
  IF(DTAU) 200,300,210
C RESET BOUND
200 PSIN=PSI
  DTAUN=DTAU
  GO TO 220
210 PSIP=PSI
  DTAUP=DTAU
C TRY NEWTON'S METHOD AND INITIALIZE SELECTOR N
220 PSI=PSI-DTAU/R
  N=0

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C ACCEPT PSI IF IT IS BETWEEN BOUNDS PSIN AND PSIP
230 IF(PSI.GT.PSIN.AND.PSI.LT.PSIP) GO TO 100
C SELECT ALTERNATE METHOD OF COMPUTING PSI OR STOP ITERATIONS
N=N+1
GO TO (1,2,3,4,300),N
C TRY INCREMENTING BOUND WITH DTAU NEAREST ZERO BY THE RATIO 4*DTAU/TAU
1 IF(DABS(DTAUN).LT.DABS(DTAUP)) PSI=PSIN*(1.-(4.*DTAUN)/TAU)
IF(DABS(DTAUP).LT.DABS(DTAUN)) PSI=PSIP*(1.-(4.*DTAUP)/TAU)
GO TO 230
C TRY DOUBLING BOUND CLOSEST TO ZERO
2 IF(TAU.GT.0.) PSI=PSIN+PSIN
IF(TAU.LT.0.) PSI=PSIP+PSIP
GO TO 230
C TRY INTERPOLATION BETWEEN BOUNDS
3 PSI=PSIN+(PSIP-PSIN)*(-DTAUN/(DTAUP-DTAUN))
GO TO 230
C TRY HALVING BETWEEN BOUNDS
4 PSI=PSIN+(PSIP-PSIN)*.5
GO TO 230
C END OF LOOP FOR SOLVING KEPLER'S EQUATION
C
C COMPUTE REMAINING THREE OF FOUR FUNCTIONS FM1,G,FD,GDM1
300 FM1=-MU*S2/R0
FD=-MU*S1/R0/R
GDM1=-MU*S2/R
C COMPUTE COORDINATES AT SOLUTION TIME T=T0+TAU
DO 310 I=1,3
S(I)=SO(I)+(FM1*SO(I)+G*SO(I+3))
S(I+3)=(FD*SO(I)+GDM1*SO(I+3))+SO(I+3)
XRF(I)=S(I)
10 XVF(I)=S(I+3)
IF (IMTX.EQ. 0) GO TO 500
C COMPUTE ACCELERATIONS
DO 320 I=1,3
ACC(I)=-MU*S(I)/R/R/R
320 ACC0(I)=-MU*SO(I)/R0/R0/R0
C END OF COMPUTATION FOR COORDINATES AND ACCELERATIONS
C
C COMPUTATION OF PARTIAL DERIVATIVES
C COMPUTE COEFFICIENTS FOR STATE PARTIALS
U=S2*TAU+MU*(C4-C5*X3)*PSI*PSI*PSI*PSI*PSI
P(1,1)=-(FD*S1+FM1/R0)/R0
P(1,2)=-FD*S2
P(2,1)=FM1*S1/R0
P(2,2)=FM1*S2
P(1,3)=P(1,2)
P(1,4)=-GDM1*S2
P(2,3)=P(2,2)
P(2,4)=G*S2
P(3,1)=-FD*(C0/R0/R+1./R/R+1./R0/R0)
P(3,2)=-(FD*S1+GDM1/R)/R
P(4,1)=-P(1,1)
P(4,2)=-P(1,2)
P(3,3)=P(3,2)
P(3,4)=-GDM1*S1/R
P(4,3)=-P(1,2)
P(4,4)=-P(1,4)

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C COMPUTE COEFFICIENTS FOR MU PARTIALS

```
P(1,5)=-S1/R0/R  
P(2,5)=S2/R0  
P(3,5)=U/R0-S3  
P(1,6)=-P(1,5)  
P(2,6)=S2/R  
P(3,6)=-U/R+S3
```

```
DO 400 I=1,3
```

C MATRIX ACCUMULATIONS FOR STATE PARTIALS

```
DO 400 J=1,4  
PI(J,1)=P(J,1)*SO(I)+P(J,2)*SO(I+3)  
400 PI(J,I+3)=P(J,3)*SO(I)+P(J,4)*SO(I+3)  
DO 410 I=1,3  
DO 420 J=1,3  
P(I,J)=S(I)*PI(I,J)+S(I+3)*PI(2,J)+U*S(I+3)*ACCO(J)  
P(I,J+3)=S(I)*PI(I,J+3)+S(I+3)*PI(2,J+3)-U*S(I+3)*SO(J+3)  
P(I+3,J)=S(I)*PI(3,J)+S(I+3)*PI(4,J)+U*ACC(I)*ACCO(J)  
420 P(I+3,J+3)=S(I)*PI(3,J+3)+S(I+3)*PI(4,J+3)-U*ACC(I)*SO(J+3)
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```
P(I,1)=P(I,1)+FM1+1.
```

```
P(I,I+3)=P(I,I+3)+G
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```
P(I+3,1)=P(I+3,1)+FD
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```
410 P(I+3,I+3)=P(I+3,I+3)+GDM1+1.
```

C END OF COMPUTATION FOR PARTIAL DERIVATIVES

C

C END OF PROGRAM - ALL OUTPUTS HAVE BEEN COMPUTED

```
500 CONTINUE
```

```
RETURN
```

```
END
```

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SUBROUTINE CSTEP(TGO, RSV, REV, RMV, RSE, RSM, REM, H,
1DR4RSV, DR4RSE, DR4RSM, BIGJ)
IMPLICIT REAL*8(A-H,M,O-Z)
DIMENSION RSV(3), VSV(3), REV(3), VEV(3), RMV(3), VMV(3), RSE(3),
1VSE(3), RSM(3), VSM(3), REM(3), VEM(3), DR4RSV(3), DR4RSE(3),
2DR4RSM(3), URSV(3), UREV(3), URMV(3), URSE(3), URSM(3), UREM(3),
3UMTX(3,3), SVSV(3,3), EVEV(3,3), VMVM(3,3), SESE(3,3), SMSM(3,3),
4EMEM(3,3), BIGJ(6,6), TEMP1(3), TEMP2(3), TEMP3(3), TEMP4(3),
5TEMP5(3), TEMP6(3), TEMP7(3), TEMP8(3), TEMP9(3)
DIMENSION RSVRSV(3), REVREV(3), RMVRMV(3), RSERSE(3), RSMRSM(3),
1REMREM(3), DEVSE(3), DSVSE(3), DMVSM(3), DSVSM(3), DMVEM(3),
2DEMSM(3), DEVEM(3), DEMSE(3), DSMSE(3)
COMMON/CONST/MS,ME,MM,GL1,AUM,UTIME,UVELM,ERRMAX,DTR
RSV3=VMAG(RSV)**3
REV3=VMAG(REV)**3
RMV3=VMAG(RMV)**3
RSE3=VMAG(RSE)**3
RSM3=VMAG(RSM)**3
REM3=VMAG(REM)**3
CALL UNITV(RSV,URSV)
CALL UNITV(REV,UREV)
CALL UNITV(RMV,URMV)
CALL UNITV(RSE,URSE)
CALL UNITV(RSM,URSM)
CALL UNITV(REM,UREM)
DO 1 I=1,3
RSVRSV(I)=RSV(I)/RSV3
REVREV(I)=REV(I)/REV3
RMVRMV(I)=RMV(I)/RMV3
1RSERSE(I)=RSE(I)/RSE3
RSMRSM(I)=RSM(I)/RSM3
REMREM(I)=REM(I)/REM3
DEVSE(I)=REVREV(I)+RSERSE(I)
DSVSE(I)=RSVRSV(I)-RSERSE(I)
DMVSM(I)=RMVRMV(I)+RSMRSM(I)
DSVSM(I)=RSVRSV(I)-RSMRSM(I)
DMVEM(I)=RMVRMV(I)+REMREM(I)
DEMSM(I)=REMREM(I)-RSMRSM(I)
DEVEM(I)=REVREV(I)-REMREM(I)
DEMSE(I)=REMREM(I)+RSERSE(I)
DSMSE(I)=RSMRSM(I)-RSERSE(I)
DO 1 J=1,3
UMTX(I,J)=0.0
IF(I.EQ.J) UMTX(I,J)=1.0
1 CONTINUE
CALL VVT(URSV,SVSV,3)
CALL VVT(UREV,EVEV,3)
CALL VVT(URMV,VMVM,3)
CALL VVT(URSE,SESE,3)
CALL VVT(URSM,SMSM,3)
CALL VVT(UREM,EMEM,3)
DO 2 I=1,3
DO 2 J=1,3
SVSV(I,J)=(UMTX(I,J)-3.0*SVSV(I,J))/RSV3
EVEV(I,J)=(UMTX(I,J)-3.0*EVEV(I,J))/REV3
VMVM(I,J)=(UMTX(I,J)-3.0*VMVM(I,J))/RMV3
SESE(I,J)=(UMTX(I,J)-3.0*SESE(I,J))/RSE3

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SMSM(I,J)=(UMTX(I,J)-3.0*SMSM(I,J))/RSM3
EMEM(I,J)=(UMTX(I,J)-3.0*EMEM(I,J))/REM3
2 CONTINUE
    CALL MXV(SVSV,DEVSE,TEMP1,3,3)
    CALL MXV(EVEV,DSVSE,TEMP2,3,3)
    CALL MXV(SVSV,DMVSM,TEMP3,3,3)
    CALL MXV(VMVM,DSVSM,TEMP4,3,3)
    CALL MXV(EVEV,DMVEM,TEMP5,3,3)
    CALL MXV(SESE,DEMSM,TEMP6,3,3)
    CALL MXV(VMVM,DEVEM,TEMP7,3,3)
    CALL MXV(SMSM,DEMSE,TEMP8,3,3)
    CALL MXV(EMEM,DSMSE,TEMP9,3,3)
DO 3 I=1,3
DR4RSV(I)=MS*ME*(TEMP1(I)+TEMP2(I))+MS*MM*(TEMP3(I)+TEMP4(I))
1+ME*MM*(TEMP5(I)-TEMP6(I)+TEMP7(I)+TEMP8(I))
DR4RSE(I)=-(MS+ME)*MM*TEMP6(I)-MM*MS*TEMP9(I)+MM*ME*TEMP8(I)
DR4RSM(I)=(MS+MM)*ME*TEMP8(I)+ME*MS*TEMP9(I)-ME*MM*TEMP6(I)
3 CONTINUE
CPERR=VMAG(DR4RSV)/24.0
H=DSQRT(DSQRT(ERRMAX/CPERR))
IF(TGO.LT.H) H=TGO
DO 4 I=1,6
DO 4 J=1,6
BIGJ(I,J)=0.0
IF(I.EQ.J) BIGJ(I,J)=1.0
IF((J-I).EQ.3) BIGJ(I,J)=H
4 CONTINUE
RETURN
END

```

```

SUBROUTINE CSTEP3(TGO,REV,RMV,REM,H,DR4REV,BIGJ)
IMPLICIT REAL*8(A-H,M,O-Z)
DIMENSION REV(3),RMV(3),REM(3),DR4REV(3),BIGJ(6,6),UREV(3),
1URMV(3),RMVRMV(3),REMREM(3),REVREV(3),DMVEM(3),DEVEM(3),
2UMTX(3,3),EVEV(3,3),MVMV(3,3),TEMP1(3),TEMP2(3)
COMMON/CONST3/ME,MM,GAMMA,UDM,UTIME,UVELM,ERRMAX,DTR
REV3=VMAG(REV)**3
RMV3=VMAG(RMV)**3
REM3=VMAG(REM)**3
CALL UNITV(REV,UREV)
CALL UNITV(RMV,URMV)
DO 1 I=1,3
RMVRMV(I)=RMV(I)/RMV3
REMREM(I)=REM(I)/REM3
REVREV(I)=REV(I)/REV3
DMVEM(I)=RMVRMV(I)+REMREM(I)
DEVEM(I)=REVREV(I)-REMREM(I)
DO 1 J=1,3
UMTX(I,J)=0.
IF(I.EQ.J) UMTX(I,J)=1.0
1 CONTINUE
CALL VVT(UREV,EVEV,3)
CALL VVT(URMV,MVMV,3)
DO 2 I=1,3
DO 2 J=1,3
EVEV(I,J)=(UMTX(I,J)-3.0*EVEV(I,J))/REV3
2 MVMV(I,J)=(UMTX(I,J)-3.0*MVMV(I,J))/RMV3
CALL MXV(EVEV,DMVEM,TEMP1,3,3)
CALL MXV(MVMV,DEVEM,TEMP2,3,3)
DO 3 I=1,3
3 DR4REV(I)=ME*MM*(TEMP1(I)+TEMP2(I))
CPERR=VMAG(DR4REV)/24.0
H=DSQRT(DSQRT(ERRMAX/CPERR))
IF(TGO.LT.H) H=TGO
DO 4 I=1,6
DO 4 J=1,6
BIGJ(I,J)=0.
IF(I.EQ.J) BIGJ(I,J)=1.0
IF((J-I).EQ.3) BIGJ(I,J)=H
4 CONTINUE
RETURN
END

```

```

SUBROUTINE DELRV(H,RSV,REV,RMV,RSE,RSM,REM,CRSV,CREV,CRMV,
1CRSE,CRSM,CREM,DR4RSV,DR4RSE,DR4RSM,RRSV,RVSV,RRSE,RVSE,
2RRSM,RVSM)
IMPLICIT REAL*8(A-H,M,O-Z)
DIMENSION RSV(3),REV(3),RMV(3),RSE(3),RSM(3),REM(3),CRSV(3),
1CREV(3),CRMV(3),CRSE(3),CRSM(3),CREM(3),DR4RSV(3),DR4RSE(3),
2DR4RSM(3),RRSV(3),RVSV(3),RRSE(3),RVSE(3),RRSM(3),RVSM(3)
DIMENSION SSV(3),SEV(3),SMV(3),SSE(3),SSM(3),SEM(3),DDRSV(3),
1DDRSE(3),DDRSM(3)
COMMON/CONST/MS,ME,MM,GL1,AUM,UTIME,UVELM,ERRMAX,DTR
H2=H*H
H26=H2/6.0
H23=H2/3.0
RSV3=VMAG(RSV)**3
REV3=VMAG(REV)**3
RMV3=VMAG(RMV)**3
RSE3=VMAG(RSE)**3
RSM3=VMAG(RSM)**3
REM3=VMAG(REM)**3
CRSV3=VMAG(CRSV)**3
CREV3=VMAG(CREV)**3
CRMV3=VMAG(CRMV)**3
CRSE3=VMAG(CRSE)**3
CRSM3=VMAG(CRSM)**3
CREM3=VMAG(CREM)**3
DO 1 I=1,3
SSV(I)=CRSV(I)/CRSV3-RSV(I)/RSV3
SEV(I)=CREV(I)/CREV3-REV(I)/REV3
SMV(I)=CRMV(I)/CRMV3-RMV(I)/RMV3
SSE(I)=CRSE(I)/CRSE3-RSE(I)/RSE3
SSM(I)=CRSM(I)/CRSM3-RSM(I)/RSM3
SEM(I)=CREM(I)/CREM3-REM(I)/REM3
DDRSV(I)=MS*SSV(I)+ME*(SSE(I)+SEV(I))+MM*(SSM(I)+SMV(I))
DDRSE(I)=(MS+ME)*SSE(I)+MM*(SSM(I)-SEM(I))
DDRSM(I)=(MS+MM)*SSM(I)+ME*(SSE(I)+SEM(I))
RRSV(I)=H2*(DR4RSV(I)*H23+DDRSV(I))/20.0
RVSV(I)=H*(DR4RSV(I)*H26+DDRSV(I))/4.0
RRSE(I)=H2*(DR4RSE(I)*H23+DDRSE(I))/20.0
RVSE(I)=H*(DR4RSE(I)*H26+DDRSE(I))/4.0
RRSM(I)=H2*(DR4RSM(I)*H23+DDRSM(I))/20.0
RVSM(I)=H*(DR4RSM(I)*H26+DDRSM(I))/4.0
1 CONTINUE
RETURN
END

```

```
SUBROUTINE DELRV3(H,REV,RMV,CREV,CRMV,DR4REV,RREV,RREV)
IMPLICIT REAL*8(A-H,M,O-Z)
DIMENSION REV(3),RMV(3),CREV(3),CRMV(3),DR4REV(3),RREV(3),
1 RREV(3),SEV(3),SMV(3),DDREV(3)
COMMON/CONST3/ME,MM,GAMMA,UDM,UTIME,UVELM,ERRMAX,DTR
H2=H*H
H26=H2/6.0
H23=H2/3.0
REV3=VMAG(REV)**3
CREV3=VMAG(CREV)**3
RMV3=VMAG(RMV)**3
CRMV3=VMAG(CRMV)**3
DO 1 I=1,3
SEV(I)=CREV(I)/CREV3-REV(I)/REV3
SMV(I)=CRMV(I)/CRMV3-RMV(I)/RMV3
DDREV(I)=ME*SEV(I)+MM*SMV(I)
RREV(I)=H2*(DR4REV(I)*H23+DDREV(I))/20.0
1 RREV(I)=H*(DR4REV(I)*H26+DDREV(I))/4.0
RETURN
END
```

```

SUBROUTINE COMIC(REVMAG, VEMAG, LON, THE, OINC, OBL, RSEO, VSEO,
IREVO, VEO, RSVO, VSVO, VSVI)
IMPLICIT REAL*8(A-H,L-M,O-Z)
DIMENSION RSEO(3), VSEO(3), REVO(3), VEO(3), RSVO(3), VSVO(3),
VSVI(3), TEMP(3), VEVOP(3)
COMMON/CONST/MS,ME,MM,GL1,AUM,UTIME,UVELM,ERRMAX,DTR
COMMON/FLAG/IMTX,IPV,IPTRAJ,IPVTM,IFILE,ITER,ITAR
COMMON/TRIG/CLON,SLON,CHE,SHE,CINC,SINC,COBL,SOBL
IF(ITER.GT.0) GO TO 1
VCIR=DSQRT(ME/REVMAG)
CINC=DCOS(OINC)
SINC=DSIN(OINC)
COBL=DCOS(OBL)
SOBL=DSIN(OBL)
1 CLON=DCOS(LON)
SLON=DSIN(LON)
CHE=DCOS(THE)
SHE=DSIN(THE)
REVO(1)=REVMAG*(CLON*CHE-SLON*CINC*SHE)
REVO(2)=REVMAG*(COBL*(SLON*CHE+CLON*CINC*SHE)
1      +SOBL*SINC*SHE)
REVO(3)=REVMAG*(-SOBL*(SLON*CHE+CLON*CINC*SHE)
1      +COBL*SINC*SHE)
VEVOP(1)=VEVMAG*(-CLON*SHE-SLON*CINC*CHE)
VEVOP(2)=VEVMAG*(COBL*(-SLON*SHE+CLON*CINC*CHE)
1      +SOBL*SINC*CHE)
VEVOP(3)=VEVMAG*(-SOBL*(-SLON*SHE+CLON*CINC*CHE)
1      +COBL*SINC*CHE)
CALL UNITV(VEVOP,TEMP)
DO 2 I=1,3
VEVO(I)=VCIR*TEMP(I)
VSVO(I)=VSEO(I)+VEVO(I)
RSVO(I)=RSEO(I)+REVO(I)
2 VSVI(I)=VSEO(I)+VEVOP(I)
RETURN
END

```

```

SUBROUTINE COMIC3(REVMAG,VEVMAG,LON,THE,OINC,REVO,VEVO,VEVOP)
IMPLICIT REAL*8(A-H,L-M,O-Z)
DIMENSION REVO(3),VEVO(3),VEVOP(3),TEMP(3)
COMMON/FLAG/IMTX,IPV,IPTRAJ,IPVTM,IFILE,ITER,ITAR
COMMON/CONST3/ME,MM,GAMMA,UDM,UTIME,UVELM,ERRMAX,DTR
COMMON/TRIG3/CLON,SLON,CHE,SHE,CINC,SINC
IF(ITER.GT.0) GO TO 1
VCIR=DSQRT(IME/REVMAG)
CINC=DCOS(OINC)
SINC=DSIN(OINC)
1 CLON=DCOS(LON)
SLON=DSIN(LON)
CHE=DCOS(THE)
SHE=DSIN(THE)
REVO(1)=REVMAG*(CLON*CHE-SLON*CINC*SHE)
REVO(2)=REVMAG*(SLON*CHE+CLON*CINC*SHE)
REVO(3)=REVMAG*SINC*SHE
VEVOP(1)=VEVMAG*(-CLON*SHE-SLON*CINC*CHE)
VEVOP(2)=VEVMAG*(-SLON*SHE+CLON*CINC*CHE)
VEVOP(3)=VEVMAG*SINC*CHE
CALL UNITV(VEVOP,TEMP)
DO 2 I=1,3
2 VEO(I)=VCIR*TEMP(I)
WRITE(6,100)REVO,VEVO
WRITE(6,101)VEVOP
100 FORMAT(1H0,T8,'REVO',T68,'VEVO'/1H ,1P6D20.11)
101 FORMAT(1H ,T8,'VEVOP'/1H ,1P3D20.11)
RETURN
END

```

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SUBROUTINE COMFG(TSTART,TEND,REVMAG,XD,OINC,OBL,
1RSEO,VSEO,RSMO,VSMO,FD,TESTRD,TD,TSID,LTD,S11,S12,S21,S22,
2UVI,UVF)
IMPLICIT REAL*8(A-H,L-M,O-Z)
DIMENSION RSEO(3),VSEO(3),RSMO(3),VSMO(3),REVO(3),VEVO(3),
1RSVO(3),VSVO(3),VSVI(3),RSVTAR(3),VSVTAR(3),REM(3),VEMF(3),
2PVO(6),RSVF(3),VSVF(3),RSEF(3),VSEF(3),RSMF(3),VSMF(3),
3S11(3,3),S12(3,3),S21(3,3),S22(3,3),TSID(3),DVI(3),UVI(3),
4DVF(3),UVF(3),DRODX(3,3),DVODX(3,3),TEMP1(3,3),TEMP2(3,3),
5GD(3),LTD(3,3),XD(3),REV(3),VEVF(3),RMVF(3),VMVF(3)
DIMENSION DUVI(3),DUM(3),S12I(3,3)
COMMON/CONST/MS,ME,MM,GL1,AUM,UTIME,UVELM,ERRMAX,DTR
COMMON/TRIG/CLON,SLON,CTHE,STHE,CINC,SINC,COBL,SOBL
COMMON/FLAG/IMTX,IPV,IPTRAJ,IPVTM,IFILE,ITER,ITAR
COMMON/TARG/AY,AZ,ATAR,RSVTAR,VSVTAR
REVMAG=XD(1)
LON=XD(2)
THE=XD(3)
VEVMPS=REVMAG/UVELM
LOND=LON/DTR
THED=THE/DTR
WRITE(6,108)
WRITE(6,101)XD,VEVMPS,LOND,THED
CALL COMIC(REVMAG,REVMAG,LON,THE,OINC,OBL,RSEO,VSEO,
1REVO,VEVO,RSVO,VSVO,VSVI)
CALL FOURBY(TSTART,TEND,RSVO,VSVI,RSEO,VSEO,RSMO,VSMO,
1PVO,RSVF,VSVF,RSEF,VSEF,RSMF,VSMF,S11,S12,S21,S22)
CALL RVERMV(RSVF,VSVF,RSEF,VSEF,RSMF,VSMF,REV,VEVF,RMF,VMVF,
1REM,REM)
WRITE(6,102)RSVF,VSVF
IF(ITER.GT.0) GO TO 11
IF(ITAR.GT.0) GO TO 11
CALL CTAR(RSEF,VSEF,RSMF,VSMF,REM,REM,AY,AZ,ATAR,RSVTAR,
1VSVTAR)
11 DO 2 I=1,3
TSID(I)=RSVF(I)-RSVTAR(I)
DVI(I)=VSVI(I)-VSVO(I)
2 DVF(I)=VSVTAR(I)-VSVF(I)
TESTRD=VMAG(TSID)
DVIMAG=VMAG(DVI)
DVFMAG=VMAG(DVF)
DVIMPS=DVIMAG/UVELM
DVFMPS=DVFMAG/UVELM
CALL UNITV(DVI,UVI)
CALL UNITV(DVF,UVF)
FD=DVFMAG
CALL MXV(S11,UVI,DUM,3,3)
DO 21 I=1,3
21 DUM(I)=UVF(I)-DUM(I)
CALL INVERT(S12,S12I)
CALL MXV(S12I,DUM,DUVI,3,3)
WRITE(6,103)DVI,UVI
WRITE(6,104)DVF,UVF
WRITE(6,105)DUVI,TSID
WRITE(6,106)DVIMAG,DVFMAG,DVIMPS,DVFMPS,FD,TESTRD
DRODX(1,1)=0.
DRODX(1,2)=REVMAG*(-SLON*CTHE-CLON*CINC*STHE)

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DRODX(1,3)=REVMAG*(-CLON*STHE-SLON*CINC*CTHE)
DRODX(2,1)=0.
DRODX(2,2)=REVMAG*COBL*(CLON*CTHE-SLON*CINC*STHE)
DRODX(2,3)=REVMAG*(COBL*(-SLON*STHE+CLON*CINC*CTHE)
1      +SOBL*SINC*CTHE)
DRODX(3,1)=0.
DRODX(3,2)=-REVMAG*SOBL*(CLON*CTHE-SLON*CINC*STHE)
DRODX(3,3)=REVMAG*(-SOBL*(-SLON*STHE+CLON*CINC*CTHE)
1      +COBL*SINC*CTHE)
DVODX(1,1)=-CLON*STHE-SLON*CINC*CTHE
DVODX(1,2)=VEVMAG*(SLON*STHE-CLON*CINC*CTHE)
DVODX(1,3)=VEVMAG*(-CLON*CTHE+SLON*CINC*STHE)
DVODX(2,1)=COBL*(-SLON*STHE+CLON*CINC*CTHE)
1      +SOBL*SINC*CTHE
DVODX(2,2)=VEVMAG*COBL*(-CLON*STHE-SLON*CINC*CTHE)
DVODX(2,3)=VEVMAG*(COBL*(-SLON*CTHE-CLON*CINC*STHE)
1      -SOBL*SINC*STHE)
DVODX(3,1)=-SOBL*(-SLON*STHE+CLON*CINC*CTHE)
1      +COBL*SINC*CTHE
DVODX(3,2)=-VEVMAG*SOBL*(-CLON*STHE-SLON*CINC*CTHE)
DVODX(3,3)=VEVMAG*(-SOBL*(-SLON*CTHE-CLON*CINC*STHE)
1      -COBL*SINC*STHE)
CALL MXM(S21,DRODX,TEMP1,3,3,3)
CALL MXM(S22,DVODX,TEMP2,3,3,3)
DO 3 I=1,3
DO 3 J=1,3
3 TEMP1(I,J)=TEMP1(I,J)+TEMP2(I,J)
CALL MTRANS(TEMP1,TEMP2,3,3)
CALL MXV(TEMP2,UVF,GD,3,3)
DO 4 I=1,3
4 GD(1)=-GD(1)
WRITE(6,107)GD
CALL MXM(S11,DRODX,TEMP1,3,3,3)
CALL MXM(S12,DVODX,TEMP2,3,3,3)
DO 5 I=1,3
DO 5 J=1,3
LTD(I,J)=TEMP1(I,J)+TEMP2(I,J)
5 CONTINUE
101 FORMAT(1H0,T8,'XD',T68,'VEVMPS',T88,'LOND',T108,'THED'/1H,
11P6D20.11)
102 FORMAT(1H ,T8,'RSVF',T68,'VSVF'/1H ,1P6D20.11)
103 FORMAT(1H ,T8,'DVI',T68,'UVI'/1H ,1P6D20.11)
104 FORMAT(1H ,T8,'DVF',T68,'UVF'/1H ,1P6D20.11)
105 FORMAT(1H ,T8,'DUV',T68,'TSID'/1H ,1P6D20.11)
106 FORMAT(1H ,T8,'DVIMAG',T28,'DVFMAG',T48,'DVIMPS',T68,'DVFMPS',
1T88,'FD',T108,'TESTRD'/1H ,1P6D20.11)
107 FORMAT(1H ,T8,'GD'/1H ,1P3D20.11)
108 FORMAT(1H0,T8,'-----')
      RETURN
      END

```

```

SUBROUTINE COMFG3(TSTART,TEND,REVMAG,XD,OINC,REMO,
1 VEMO,FD,TESTRD,GD,TSID,LTD,S11,S12,S21,S22,UVI,UVF)
IMPLICIT REAL*8(A-H,L-M,O-Z)
DIMENSION REMO(3),VEMO(3),REVO(3),VEVO(3),VEVOP(3),REVTAR(3),
1 VEV TAR(3),PVO(6),REV F(3),VEVF(3),REM F(3),VEM F(3),S11(3,3),XD(3),
2 S12(3,3),S21(3,3),S22(3,3),TSID(3),DVI(2),UVI(3),DVF(3),UVF(3),
3 DRODX(3,3),DVODX(3,3),TEMP1(3,3),TEMP2(3,3),GD(3),LTD(3,3)
DIMENSION DUVI(3),DUM(3),S121(3,3)
COMMON/CONST3/ME,MM,GAMMA,UDM,UTIME,UVELM,ERRMAX,DTR
COMMON/TRIG3/CLON,SLON,CTHE,STHE,CINC,SINC
COMMON/FLAG/IMTX,IPV,IPTRAJ,IPVTM,IFILE,ITER,ITAR
COMMON/TARG/AY,AZ,ATAR,REVTAR,VEVTAR
VEVMAG=XD(1)
LON=XD(2)
THE=XD(3)
VEVMPS=VEVMAG/UVELM
LOND=LON/DTR
THED=THE/DTR
WRITE(6,108)
WRITE(6,101)XD,VEVMPS,LOND,THED
CALL COMIC3(REVMAG,VEVMAG,LON,THE,OINC,REVO,VEVO,VEVOP)
CALL THRBDY(TSTART,TEND,REVO,VEVOP,REMO,VEMO,PVO,REV F,VEVF,
1 REM F,VEM F,S11,S12,S21,S22)
WRITE(6,102)REV F,VEVF
IF(ITER.GT.0) GO TO 11
IF(ITAR.GT.0) GO TO 11
CALL CTAR3(REMF,VEM F,AY,AZ,ATAR,REVTAR,VEVTAR)
11 DO 2 I=1,3
  TSID(I)=REV F(I)-REVTAR(I)
  DVI(I)=VEVOP(I)-VEVO(I)
2  DVF(I)=VEVTAR(I)-VEVF(I)
  TESTRD=VMAG(TSID)
  DVIMAG=VMAG(DVI)
  DVFMAG=VMAG(DVF)
  DVIMPS=DVIMAG/UVELM
  DVFMPS=DVFMAG/UVELM
  CALL UNITV(DVI,UVI)
  CALL UNITV(DVF,UVF)
  FD=DVFMAG
  CALL MXV(S11,UVI,DUM,3,3)
  DO 21 I=1,3
21  DUM(I)=UVF(I)-DUM(I)
  CALL INVERT(S12,S121)
  CALL MXV(S121,DUM,DUVI,3,3)
  WRITE(6,103)DVI,UVI
  WRITE(6,104)DVF,UVF
  WRITE(6,105)DUVI,TSID
  WRITE(6,106)DVIMAG,DVFMAG,DVIMPS,DVFMPS,FD,TESTRD
  DRODX(1,1)=0.
  DRODX(1,2)=REVMAG*(-SLON*CTHE-CLON*CINC*STHE)
  DRODX(1,3)=REVMAG*(-CLON*STHE-SLON*CINC*CTHE)
  DRODX(2,1)=0.
  DRODX(2,2)=REVMAG*(CLON*CTHE-SLON*CINC*STHE)
  DRODX(2,3)=REVMAG*(-SLON*STHE+CLON*CINC*CTHE)
  DRODX(3,1)=0.
  DRODX(3,2)=0.
  DRODX(3,3)=REVMAG*SINC*CTHE

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DVODX(1,1)=-CLON*STHE-SLON*CINC*CTHE
DVODX(1,2)=VEVMAG*(SLON*STHE-CLON*CINC*CTHE)
DVODX(1,3)=VEVMAG*(-CLON*CTHE+SLON*CINC*STHE)
DVODX(2,1)=-SLON*STHE+CLON*CINC*CTHE
DVODX(2,2)=VEVMAG*(-CLON*STHE-SLON*CINC*CTHE)
DVODX(2,3)=VEVMAG*(-SLON*CTHE-CLON*CINC*STHE)
DVODX(3,1)=SINC*CTHE
DVODX(3,2)=0.
DVODX(3,3)=-VEVMAG*SINC*STHE
CALL MXM(S21,DRODX,TEMP1,3,3,3)
CALL MXM(S22,DVODX,TEMP2,3,3,3)
DO 3 I=1,3
DO 3 J=1,3
3 TEMP1(I,J)=TEMP1(I,J)+TEMP2(I,J)
CALL MTRANS(TEMP1,TEMP2,3,3)
CALL MXV(TEMP2,UVF,GD,3,3)
DO 4 I=1,3
4 GD(I)=-GD(I)
WRITE(6,107)GD
CALL MXM(S11,DRODX,TEMP1,3,3,3)
CALL MXM(S12,DVODX,TEMP2,3,3,3)
DO 5 I=1,3
DO 5 J=1,3
LTD(I,J)=TEMP1(I,J)+TEMP2(I,J)
5 CONTINUE
100 FORMAT(1H0,T8,'COMPUTED TARGET'/1H0,T8,'REVTAR',T68,'VEVTAR'/
1H ,1P6D20.11)
101 FORMAT(1H0,T8,'XD',T68,'VEVMPS',T88,'LOND',T108,'THED'/1H ,
1P6D20.11)
102 FORMAT(1H ,T8,'REVF',T68,'VEVF'/1H ,1P6D20.11)
103 FORMAT(1H ,T8,'DVI',T68,'UVI'/1H ,1P6D20.11)
104 FORMAT(1H ,T8,'DVF',T68,'UVF'/1H ,1P6D20.11)
105 FORMAT(1H ,T8,'DUVI',T68,'TSID'/1H ,1P6D20.11)
106 FORMAT(1H ,T8,'DVIMAG',T28,'DVFMAG',T48,'DVIMPS',T68,'DVFMPS',
1T88,'FD',T108,'TESTRD'/1H ,1P6D20.11)
107 FORMAT(1H ,T8,'GD'/1H ,1P3D20.11)
108 FORMAT(1H0,T8,'-----')
      RETURN
      END

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SUBROUTINE COMF(TSTART,TM,TEND,RSVO,VSVO,VSVI,RSEO,VSEO,RSMO,
1VSMO,ERRMIN,ILINC,KNRSAV,ITERD,ITLMAX,RSVMD,VSVPD,RSVTAR,
2VSVTAR,S11D,S12D,RSVM,VSVM,VSVPD,DV,UVI,UVM,UVF,SMI11,SMI12,
3SMI121,SMI122,SMF11,SMF12,SMF21,SMF22)
IMPLICIT REAL*8(A-H,K-M,O-Z)
EXTRAPOLATE STATES TO TM AND SOLVE LAMBERT PROBLEM FROM TM TO
TEND
DIMENSION RSVO(3),VSVO(3),VSVI(3),RSEO(3),VSEO(3),RSMO(3),
1VSMO(3),PVO(6),RSVM(3),VSVM(3),RSEM(3),VSEM(3),RSMM(3),
2VSMM(3),SMI11(3,3),SMI12(3,3),SMI21(3,3),SMI22(3,3),SMF11(3,3),
3SMF12(3,3),SMF21(3,3),SMF22(3,3),S11D(3,3),S12D(3,3),
4RSVMX(3),VSVPDX(3),DRM(3),TEMP1(3,3),DUM(3),
5RSVF(3),VSVF(3),RSEF(3),VSEF(3),RSMF(3),VSMF(3),VSVPD(3),
6DV(3),DVM(3),DVF(3),UVI(3),UVM(3),UVF(3),DVMPX(3)
DIMENSION RSVTAR(3),VSVTAR(3),RSVMD(3),VSVPD(3)
COMMON/CONST/MS,ME,MM,GL1,AUM,UTIME,UVELM,ERRMAX,DTR
KNR=KNRSAV
WRITE(6,100)
WRITE(6,101)VSVI,TM
ADVANCE STATES FROM TSTART TO TM
CALL FOURBY(TSTART,TM,RSVO,VSVO,RSEO,VSEO,RSMO,VSMO,
1PVO,RSVM,VSVM,RSEM,VSEM,RSMM,VSMM,SMI11,SMI12,SMI21,SMI22)
IF(ITERD.GT.0) GO TO 3
DO 2 I=1,3
VSVPDX(I)=VSVPD(I)
2 RSVMX(I)=RSVMD(I)
KNR=KNRSAV
CALL LAMB(TM,TEND,RSVMX,VSVPDX,RSEM,VSEM,RSMM,VSMM,KNR,ITLMAX,
1ERRMIN,RSVTAR,RSVF,VSVF,RSEF,VSEF,RSMF,VSMF,SMF11,SMF12,SMF21,
2SMF22)
GO TO 71
INCREMENTAL SOLUTION OF SECOND LEG LAMBERT PROBLEM
3 DO 4 I=1,3
VSVPDX(I)=VSVPD(I)
RSVMX(I)=RSVMD(I)
DRM(I)=(RSVMD(I)-RSVMD(I))/ILINC
DO 4 J=1,3
SMF11(I,J)=S11D(I,J)
4 SMF12(I,J)=S12D(I,J)
WRITE(6,102)RSVMD,RSVM,DRM,ILINC
WRITE(6,106)VSVPD
DO 7 ITERL=1,ILINC
CALL INVERT(SMF12,TEMP1)
CALL MXV(SMF11,DRM,DUM,3,3)
CALL MXV(TEMP1,DUM,DVMPX,3,3)
DO 5 I=1,3
DVMPX(I)=-DVMPX(I)
RSVMX(I)=RSVMX(I)+DRM(I)
5 VSVPDX(I)=VSVPDX(I)+DVMPX(I)
WRITE(6,103)ITERL,DVMPX,RSVMX,VSVPDX
KNR=KNRSAV
6 CALL LAMB(TM,TEND,RSVMX,VSVPDX,RSEM,VSEM,RSMM,VSMM,
1KNR,ITLMAX,ERRMIN,RSVTAR,RSVF,VSVF,RSEF,VSEF,RSMF,VSMF,SMF11,
2SMF12,SMF21,SMF22)
7 CONTINUE
SAVE VSVPD AND COMPUTE DV
71 DO 8 I=1,3

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VSVMP(I)=VSVMPX(I)
DVI(I)=VSVI(I)-VSVO(I)
DVM(I)=VSVMP(I)-VSMM(I)
8 DVF(I)=VSVTAR(I)-VSVF(I)
DVIMAG=VMAG(DVI)
DVMMAG=VMAG(DVM)
DVFMAG=VMAG(DVF)
DV=DVIMAG+DVMMAG+DVFMAG
DVIMPS=DVIMAG/UVELM
DVMMPS=DVMMAG/UVELM
DVFMPS=DVFMAG/UVELM
DVMP(S)=DV/UVELM
CALL UNITV(DVI,UVI)
CALL UNITV(DVM,UVM)
CALL UNITV(DVF,UVF)
WRITE(6,104)DVI,UVI,DVM,UVM,DVF,UVF,DVIMAG,DVMMAG,DVFMAG,
1DV,DVIMPS,DVMMPS,DVFMPS,DVMP(S)
100 FORMAT(1H0,40X,'FIRST LEG TRAJECTORY')
101 FORMAT(1H0,T8,'VS VI',T68,'TM'/1H ,1P4D20.11)
102 FORMAT(1H0,T8,'SOLVE SECOND LEG LAMBERT PROBLEM IN INCREMENTS'
1/1H0,T8,'RSVMD',T68,'RSVM'/1H ,1P6D20.11/1H ,T8,'DRM',T68,
2'ILINC'/1H ,1P3D20.11,I10)
103 FORMAT(1H1,T8,'ITERL',T28,'DVMPX'/1H ,I10,10X,1P3D20.11/1H ,T8,
1'RSVMX',T68,'VS VMPX'/1H ,1P6D20.11)
104 FORMAT(1H0,T8,'DVI',T68,'UVI'/1H ,1P6D20.11/1H ,T8,'DVM',T68,
1'UVM'/1H ,1P6D20.11/1H ,T8,'DVF',T68,'UVF'/1H ,1P6D20.11/1H ,
2T8,'DVIMAG',T28,'DVMMAG',T48,'DVFMAG',T68,'DV'/1H ,1P4D20.11/
31H ,T8,'DVIMPS',T28,'DVMMPS',T48,'DVFMPS',T68,'DVMP(S')/1H ,
41P4D20.11)
106 FORMAT(1H ,T8,'VS VMPD'/1H ,1P3D20.11)
RETURN
END

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SUBROUTINE COMF3(TSTART,TM,TEND,REVO,VEVO,VEVOP,REMO,VEMO,
1ERRMIN,ILINC,KNRSAV,ITERD,ITLMAX,REVMD,VEVMPD,REVTAR,VEVTAR,
2S11D,S12D,REVM,VEVMM,VEVMP,DV,UVI,UVM,UVF,SMI11,SMI12,SMI21,
3SMI22,SFM11,SFM12,SFM21,SFM22)
IMPLICIT REAL*8(A-H,K-M,O-Z)
C EXTRAPOLATE STATES TO TM AND SOLVE LAMBERT PROBLEM FROM TM TO
C TEND
C DIMENSION REVO(3),VEVO(3),VEVOP(3),REMO(3),VEMO(3),PVO(6),
1REVM(3),VEVMM(3),VEVMP(3),REMM(3),VEMM(3),SMI11(3,3),SMI12(3,3),
2SMI21(3,3),SMI22(3,3),SFM11(3,3),SFM12(3,3),SFM21(3,3),
3SFM22(3,3),S11D(3,3),S12D(3,3),REVMX(3),VEVMPX(3),DRM(3),
4REVF(3),VEVF(3),REM(3),VEMF(3),DVI(3),DVM(3),DVF(3),
5UVI(3),UVM(3),UVF(3),DVMPX(3),REVTAR(3),VEVTAR(3),REVMD(3),
6VEVMPD(3),TEMP1(3,3),DUM(3)
COMMON/CONST3/ME,MM,GAMMA,UDM,UTIME,UVELM,ERRMAX,DTR
WRITE(6,100)
WRITE(6,101)VEVOP,TM
C ADVANCE STATES FROM TSTART TO TM
CALL THRBDY(TSTART,TM,REVO,VEVOP,REMO,VEMO,PVO,REVM,VEVMM,
1REMM,VEMM,SMI11,SMI12,SMI21,SMI22)
IF(ITERD.GT.0)GO TO 3
DO 2 I=1,3
VEVMPX(I)=VEVMP(I)
2 REVMX(I)=REVM(I)
KNR=KNRSAV
CALL LAMB3(TM,TEND,REVMX,VEVMPX,REMM,VEMM,KNR,ITLMAX,ERRMIN,
1REVTAR,REVF,VEVF,REM(3),VEMF,SFM11,SFM12,SFM21,SFM22)
GO TO 71
INCREMENTAL SOLUTION OF SECOND LEG LAMBERT PROBLEM
3 DO 4 I=1,3
VEVMPX(I)=VEVMPD(I)
REVMX(I)=REVMD(I)
DRM(I)=(REVM(I)-REVMD(I))/ILINC
DO 4 J=1,3
SFM11(I,J)=S11D(I,J)
4 SFM12(I,J)=S12D(I,J)
WRITE(6,102)REVMD,REVM,DRM,ILINC
WRITE(6,106)VEVMPD
DO 7 ITERL=1,ILINC
CALL INVERT(SFM12,TEMP1)
CALL MXV(SFM11,DRM,DUM,3,3)
CALL MXV(TEMP1,DUM,DVMPX,3,3)
DO 5 I=1,3
DVMPX(I)=-DVMPX(I)
REVMX(I)=REVMX(I)+DRM(I)
5 VEVMPX(I)=VEVMPX(I)+DVMPX(I)
WRITE(6,103)ITERL,DVMPX,REVMX,VEVMPX
KNR=KNRSAV
6 CALL LAMB3(TM,TEND,REVMX,VEVMPX,REMM,VEMM,KNR,ITLMAX,ERRMIN,
1REVTAR,REVF,VEVF,REM(3),VEMF,SFM11,SFM12,SFM21,SFM22)
7 CONTINUE
SAVE VEVMP AND COMPUTE DV
71 DO 8 I=1,3
VEVMP(I)=VEVMPX(I)
DVI(I)=VEVOP(I)-VEVO(I)
DVM(I)=VEVMP(I)-VEVMM(I)
8 DVF(I)=REVTAR(I)-VEVF(I)

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DVIMAG=VMAG(DVI)
DVMMAG=VMAG(DVM)
DVF MAG=VMAG(DVF)
DV=DVIMAG+DVMMAG+DVF MAG
DVIMPS=DVIMAG/UVELM
DVMMPS=DVMMAG/UVELM
DVF MPS=DVF MAG/UVELM
DVMP S=DVMAG/UVELM
CALL UNITV(DVI,UVI)
CALL UNITV(DVM,UVM)
CALL UNITV(DVF,UVF)
WRITE(6,104)DVI,UVI,DVM,UVM,DVF,UVF,DVIMAG,DVMMAG,DVF MAG,
1DV,DVIMPS,DVMMPS,DVF MPS,DVMP S
100 FORMAT(1HO,40X,'FIRST LEG TRAJECTORY')
101 FORMAT(1HO,T8,'VEVOP',T68,'TM'/1H ,1P4D20.11)
102 FORMAT(1HO,T8,'SOLVE SECOND LEG LAMBERT PROBLEM IN INCREMENTS'
1/1HO,T8,'REVMD',T68,'REVM'/1H ,IP6D20.11/1H ,T8,'DRM',T68,
2'ILINC'/1H ,1P3D20.11,I10)
103 FORMAT(1H1,T8,'ITERL',T28,'DVMPX'/1H ,110,10X,1P3D20.11/1H ,T8,
1'REVMX',T68,'VEVMPX'/1H ,1P6D20.11)
104 FORMAT(1HO,T8,'DVI',T68,'UVI'/1H ,1P6D20.11/1H ,T8,'DVM',T68,
1'UVM'/1H ,1P6D20.11/1H ,T8,'DVF',T68,'UVF'/1H ,1P6D20.11/1H ,
2T8,'DVIMAG',T28,'DVMMAG',T48,'DVF MAG',T68,'DV'/1H ,1P4D20.11/
31H ,T8,'DVIMPS',T28,'DVMMPS',T48,'DVF MPS',T68,'DVMP S'/1H ,
41P4D20.11)
106 FORMAT(1H ,T8,'VEVMPD'/1H ,1P3D20.11)
      RETURN
      END

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SUBROUTINE COMG(SMI11,SMI12,SMI21,SMI22,SFM11,SFM12,VTMP,
1VTMM,UVI,UVM,UVF,DUVI,DUVMM,DUVMP,G)
IMPLICIT REAL*8(A-H,O-Z)
DIMENSION SMI11(3,3),SMI12(3,3),SMI21(3,3),SMI22(3,3),
1SFM11(3,3),SFM12(3,3),VTMP(3),VTMM(3),UVI(3),UVM(3),UVF(3),
2G(4),SMI12I(3,3),TEMP1(3,3),DUM1(3),DUM2(3),DUM3(3),
3SFM12I(3,3),DUVI(3),DUVMM(3),DUVMP(3),SMI12T(3,3),GVI(3),DVM(3)
CALL INVERT(SMI12,SMI12I)
CALL MXV(SMI11,UVI,DUM3,3,3)
DO 1 I=1,3
1 DUM3(I)=UVM(I)-DUM3(I)
CALL MXV(SMI12I,DUM3,DUVI,3,3)
CALL MXV(SMI22,DUVI,DUM2,3,3)
CALL MXV(SMI21,UVI,DUM1,3,3)
DO 2 I=1,3
2 DUVMM(I)=DUM1(I)+DUM2(I)
CALL INVERT(SFM12,SFM12I)
CALL MXV(SFM11,UVM,DUM1,3,3)
DO 3 I=1,3
3 DUM1(I)=UVF(I)-DUM1(I)
CALL MXV(SFM12I,DUM1,DUVMP,3,3)
PVMAG=DOT(DUVMM,UVM,3)
PVPAG=DOT(DUVMP,UVM,3)
CALL MTRANS(SMI12,SMI12T,3,3)
DO 4 I=1,3
4 DUM3(I)=DUVMP(I)-DUVMM(I)
CALL MXV(SMI12T,DUM3,GVI,3,3)
DO 5 I=1,3
5 G(I)=GVI(I)
5 DVM(I)=VTMP(I)-VTMM(I)
G(4)=-DOT(DUVMP,DVM,3)
WRITE(6,100)DUVI,PVMAG,PVPAG
WRITE(6,101)DUVMM,DUVMP
WRITE(6,102)G
100 FORMAT(1H ,T8,'DUVI',T68,'PVMAG',T88,'PVPAG'/1H ,1P5D20.11)
101 FORMAT(1H ,T8,'DUVMM',T68,'DUVMP'/1H ,1P6D20.11)
102 FORMAT(1H ,T8,'G'/1H ,1P4D20.11)
RETURN
END

```

```

SUBROUTINE CTAR(RSEF,VSEF,RSMF,VSMF,REMF,VEMF,AY,AZ,ATAR,RSVTAR,
1 VSVTAR)
IMPLICIT REAL*8(A-H,K-M,O-Z)
DIMENSION RSEF(3),VSEF(3),REMF(3),VEMF(3),RSVTAR(3),VSVTAR(3),
1 RSL1(3),VSL1(3),UXLS(3),TEMP(3),UZLS(3),UYLS(3),CLS(3,3),
2 CSL(3,3),RLTARL(3),VLTARL(3),RLTAR(3),TEMP1(3),OMGSL(3)
DIMENSION RSMF(3),VSMF(3)
COMMON/FLAG/IMTX,IPV,IPTRAJ,IPVTM,IFILE,ITER,ITAR
COMMON/CONST/MS,ME,MM,GL1,AUM,UTIME,UVELM,ERRMAX,DTR
MEM=MM/(ME+MM)
WRITE(6,100)
DO 1 I=1,3
RSL1(I)=(1.-GL1)*(RSEF(I)+MEM*REMF(I))
1 VSL1(I)=(1.-GL1)*(VSEF(I)+MEM*VEMF(I))
IF(AY.NE.0.) GO TO 11
IF(AZ.NE.0.) GO TO 11
DO 12 I=1,3
RSVTAR(I)=RSL1(I)
12 VSVTAR(I)=VSL1(I)
GO TO 5
11 CALL UNITVIRSL1,UXLS)
CALL VXV(RSEF,VSEF,TEMP)
CALL VXV(RSMF,VSMF,TEMP1)
DO 13 I=1,3
13 TEMP(I)=ME*TEMP(I)+MM*TEMP1(I)
CALL UNITV(TEMP,UZLS)
CALL VXV(UZLS,UXLS,UYLS)
DO 2 J=1,3
CLS(1,J)=UXLS(J)
CLS(2,J)=UYLS(J)
2 CSL(3,J)=UZLS(J)
CALL MTRANS(CLS,CSL,3,3)
MU=(ME+MM)/(MS+ME+MM)
BL=(1.-MU)/(1.-GL1)**3+MU/GL1**3
OMEGAN=DSQRT(1.-BL/2.+DSQRT((3.*BL/2.)**2-2.*BL))
KTAR=2.*OMEGAN/(OMEGAN**2+2.*BL+1.)
CATAR=DCOS(ATAR)
SATAR=DSIN(ATAR)
RLTARL(1)=KTAR*AY*SATAR
RLTARL(2)=AY*CATAR
RLTARL(3)=AZ*SATAR
VLTARL(1)=KTAR*OMEGAN*AY*CATAR
VLTARL(2)=-OMEGAN*AY*SATAR
VLTARL(3)=OMEGAN*AZ*CATAR
WRITE(6,101)RLTARL,VLTARL
CALL MXV(CSL,RLTARL,RLTAR,3,3)
RMAG=VMAG(RSL1)
VY=DOT(UYLS,VSL1,3)
DO 3 I=1,3
3 OMGSL(I)=VY*UZLS(I)/RMAG
CALL VXV(OMGSL,RLTAR,TEMP)
CALL MXV(CSL,VLTARL,TEMP1,3,3)
DO 4 I=1,3
RSVTAR(I)=RSL1(I)+RLTARL(I)
4 VSVTAR(I)=VSL1(I)+TEMP1(I)+TEMP(I)
5 CONTINUE
WRITE(6,102)RSVTAR,VSVTAR

```

```
      WRITE(6,103)
100 FORMAT(1HO,T8,'COMPUTED TARGET')
101 FORMAT(1HO,T8,'RLTARL',T68,'VLTARL'/1H ,1P6D20.11)
102 FORMAT(1H ,T8,'RSVTAR',T68,'VSVTAR'/1H ,1P6D20.11)
103 FORMAT(1HO)
      RETURN
      END
```

```

SUBROUTINE CTAR3(REMF, VEMF, AY, AZ, ATAR, REVSTAR, VEVTAR)
IMPLICIT REAL*8(A-H,K-M,O-Z)
DIMENSION REMF(3), VEMF(3), REVSTAR(3), VEVTAR(3), REL(3), VEL(3),
1UXLE(3), TEMP(3), UZLE(3), UYLE(3), CLE(3,3), CEL(3,3), RLTARL(3),
2VLTARL(3), RLTAR(3), TEMP1(3), OMGEL(3)
COMMON/FLAG/1MTX, IPV, JPTRAJ, JPVTM, IFILE, ITER, ITAR
COMMON/CONST3/ME, MM, GAMMA, UDM, UTIME, UVELM, ERRMAX, DTR
WRITE(6,100)
DO 1 I=1,3
  REL(I)=(1.-GAMMA)*REMF(I)
1  VEL(I)=(1.-GAMMA)*VEMF(I)
  IF(AY.NE.0.) GO TO 11
  IF(AZ.NE.0.) GO TO 11
  DO 12 I=1,3
    REVSTAR(I)=REL(I)
12  VEVTAR(I)=VEL(I)
  GO TO 5
11 CALL UNITV(REGM,UXLE)
  CALL VXV(REMF,VEMF,TEMP)
  CALL UNITV(TEMP,UZLE)
  CALL VXV(UZLE,UXLE,LYLE)
  DO 2 J=1,3
    CLE(1,J)=UXLE(J)
    CLE(2,J)=UYLE(J)
2  CLE(3,J)=UZLE(J)
  CALL MTRANS(CLE,CEL,3,3)
  MU=MM/(ME+MM)
  BL=(1.-MU)/(1.-GAMMA)**3+MU/GAMMA**3
  OMEGAN=DSQRT(1.-BL/2.+DSQRT((3.*BL/2.)**2-2.*BL))
  KTAR=2.*OMEGAN/(OMEGAN**2+2.*BL+1.)
  CATAR=DCOS(ATAR)
  SATAR=DSIN(ATAR)
  RLTARL(1)=KTAR*AY*SATAR
  RLTARL(2)=AY*CATAR
  RLTARL(3)=AZ*SATAR
  VLSTARL(1)=KTAR*OMEGAN*AY*CATAR
  VLSTARL(2)=-OMEGAN*AY*SATAR
  VLSTARL(3)=OMEGAN*AZ*CATAR
  WRITE(6,101)RLTARL,VLTARL
  CALL MXV(CSL,RLTARL,RLTAR,3,3)
  RMAG=VMAG(REL)
  VY=DOT(UYLE,VEL,3)
  DO 3 I=1,3
3  OMGEL(I)=VY*UZLE(I)/RMAG
  CALL VXV(OMGEL,RLTAR,TEMP)
  CALL MXV(CEL,VLSTARL,TEMP1,3,3)
  DO 4 I=1,3
    REVSTAR(I)=REL(I)+RLTARL(I)
4  VEVTAR(I)=VEL(I)+TEMP1(I)+TEMP(I)
5  CONTINUE
  WRITE(6,102)REVSTAR,VEVTAR
  WRITE(6,103)
100 FORMAT(1H0,T8,'COMPUTED TARGET')
101 FORMAT(1H ,T8,'RLTARL',T68,'VLSTARL'/1H ,1P6D20.11)
102 FORMAT(1H ,T8,'REVSTAR',T68,'VEVTAR'/1H ,1P6D20.11)
103 FORMAT(1H0)
  RETURN

```

**END**

SUBROUTINE LAMB(TO,TF,RSV,VSV,RSE,VSE,RSM,VSM,KNR,ITLMAX,  
 1ERRMIN,RSVTAR,RSVX,VSVX,RSEX,VSEX,RSMX,VSMX,S11,S12,S21,S22)  
 SOLVE LAMBERT PROBLEM BY NEWTON-RAPHSON METHOD ITERATING ON  
 INITIAL VELOCITY  
 IMPLICIT REAL\*8(A-H,K-M,O-Z)  
 DIMENSION RSV(3),VSV(3),RSE(3),VSE(3),RSM(3),VSM(3),RSVTAR(3),  
 1S11(3,3),S12(3,3),S21(3,3),S22(3,3),RSVX(3),VSVX(3),RSEX(3),  
 2VSEX(3),RSMX(3),VSMX(3),REVX(3),VEVX(3),RMVX(3),VMVX(3),  
 3REMX(3),VEMX(3),ERR(3),G2(2,2),G(3,3),GI(3,3),G2I(2,2),VIT(3),  
 4DELV(3),UDELV(3),KDELV(3),PVO(6)  
 COMMON/CONST/MS,ME,MM,GL1,AUM,UTIME,UVELM,ERRMAX,DTR  
 ITER=1  
 TESTRP=100.0  
 WRITE(6,108)  
 WRITE(6,100)TO,TF,RSV,VSV  
 DO 1 I=1,3  
 PVO(I)=0.  
 PVO(I+3)=0.  
 1 VIT(I)=VSV(I)  
 2 WRITE(6,101)ITER,VIT  
 CALL FOURBY(TO,TF,RSV,VIT,RSE,VSE,RSM,VSM,PVO,RSVX,  
 1VSVX,RSEX,VSEX,RSMX,VSMX,S11,S12,S21,S22)  
 CALL RVEMV(RSVX,VSVX,RSEX,VSEX,RSMX,VSMX,REVX,VEVX,RMVX,VMVX,  
 1REMX,VEMX)  
 DO 3 I=1,3  
 3 ERR(I)=RSVTAR(I)-RSVX(I)  
 TESTR=VMAG(ERR)  
 DO 4 I=1,3  
 DO 4 J=1,3  
 4 G(I,J)=-S12(I,J)  
 WRITE(6,102)RSVX,VSVX  
 WRITE(6,107)ERR,TESTR  
 IF(ERR(3).NE.0.0) GO TO 5  
 DO 6 I=1,3  
 DO 6 J=1,3  
 6 G2(I,J)=G(I,J)  
 D2=G2(1,1)\*G2(2,2)-G2(1,2)\*G2(2,1)  
 G2I(1,1)=G2(2,2)/D2  
 G2I(1,2)=-G2(1,2)/D2  
 G2I(2,1)=-G2(2,1)/D2  
 G2I(2,2)=G2(1,1)/D2  
 DO 7 I=1,2  
 DO 7 J=1,2  
 GI(I,J)=G2I(I,J)  
 GI(I,3)=0.0  
 7 GI(3,J)=0.0  
 GI(3,3)=0.0  
 GO TO 8  
 5 CALL INVERT(G,GI)  
 8 IF (TESTR.GE.TESTRP) GO TO 9  
 DO 10 I=1,3  
 10 VSV(I)=VIT(I)  
 IF (TESTR.LT.ERRMIN) GO TO 14  
 CALL MXV(GI,ERR,DELV,3,3)  
 DO 11 I=1,3  
 11 DELV(I)=-DELV(I)  
 TESTRP=TESTR

```

DV=VMAG(DELV)
CALL UNITV(DELV,UDELV)
KNR=2.0*KNR
IF(KNR.GT.DV) KNR=DV
GO TO 12
9 KNR=KNR/10.0
12 DO 13 I=1,3
  KDELV(I)=KNR*UDELV(I)
13 VIT(I)=VSV(I)+KDELV(I)
  ITER=ITER+1
  KLV=VMAG(KDELV)
  KLVMIN=10.D-24
  IF(KLV.LT.KLVMIN) GO TO 14
  IF(ITER.LT.ITLMAX) GO TO 2
  WRITE(6,112)
  STOP
14 CONTINUE
  WRITE(6,109)
  WRITE(6,110)VSV
  WRITE(6,111)RSVX,VSVX
  WRITE(6,103)REVX,VEVX
  WRITE(6,104)RMVX,VMVX
  WRITE(6,105)RSEX,VSEX
  WRITE(6,106)RSMX,VSMX
100 FORMAT(1H0,T8,'TO',T28,'TF'/1H ,1P20.20.11/1H ,T8,'RSV',T68,
1'VSV'/1H ,1P6D20.11)
101 FORMAT(1H0,T8,'ITER',T28,'VIT'/1H ,I10,10X,1P3D20.11)
102 FORMAT(1H ,T8,'RSVX',T68,'VSVX'/1H ,1P6D20.11)
103 FORMAT(1H ,T8,'REVX',T68,'VEVX'/1H ,1P6D20.11)
104 FORMAT(1H ,T8,'RMVX',T68,'VMVX'/1H ,1P6D20.11)
105 FORMAT(1H ,T8,'RSEX',T68,'VSEX'/1H ,1P6D20.11)
106 FORMAT(1H ,T8,'RSMX',T68,'VSMX'/1H ,1P6D20.11)
107 FORMAT(1H ,T8,'ERR',T68,'TESTR'/1H ,1P4D20.11)
108 FORMAT(1H1)
109 FORMAT(1H0,T8,'LAMBERT PROBLEM HAS CONVERGED')
110 FORMAT(1H0,T8,'CONVERGED VSV'/1H ,1P3D20.11)
111 FORMAT(1H0,T8,'RSVX',T68,'VSVX'/1H ,1P6D20.11)
112 FORMAT(1H0,T8,'NO. OF LAMBERT ITERATIONS HAS REACHED MAXIMUM')
  RETURN
END

```

SUBROUTINE LAMB3(T0,TF,REV,VEV,REM,VEM,KNR,ITLMAX,ERRMIN,REVTAR,  
 1REVF,VEVF,REMF,VEMF,S11,S12,S21,S22)  
 IMPLICIT REAL\*8(A-H,K-M,O-Z)  
 THIS ROUTINE  
 SOLVES 3-BODY LAMBERT PROBLEM BY NEWTON-RAPHSON METHOD ITERATING  
 ON INITIAL VELOCITY.  
 DIMENSION REV(3),VEV(3),REM(3),VEM(3),REVTAR(3),REVF(3),VEVF(3),  
 1REM(3),VEMF(3),S11(3,3),S12(3,3),S21(3,3),S22(3,3),VIT(3),  
 2PVO(6),RMVF(3),VMVF(3),ERR(3),G(3,3),G2(2,2),G2I(2,2),GI(3,3),  
 3DELV(3),UDELV(3),KDELV(3)  
 COMMON/CONST3/ME,MM,GAMMA,UDM,UTIME,UVELM,ERRMAX,DTR  
 ITER=1  
 TESTRP=100.0  
 WRITE(6,100)T0,TF,REV,VEV  
 DO 1 I=1,3  
 PVO(I)=0.  
 PVO(I+3)=0.  
 1 VIT(I)=VEV(I)  
 2 WRITE(6,101)ITER,VIT  
 CALL THRBDY(T0,TF,REV,VEV,REM,VEM,PVO,REVF,VEVF,REMF,VEMF,S11,  
 1S12,S21,S22)  
 DO 21 I=1,3  
 RMVF(I)=-REM(1)+REVF(1)  
 21 VMVF(I)=-VEMF(I)+VEVF(I)  
 DO 3 I=1,3  
 3 ERR(I)=REVTAR(I)-REVF(I)  
 TESTR=VMAG(ERR)  
 DO 4 I=1,3  
 DO 4 J=1,3  
 4 G(I,J)=-S12(I,J)  
 WRITE(6,102)REVF,VEVF  
 WRITE(6,105)ERR,TESTR  
 IF(ERR(3).NE.0.0) GO TO 5  
 DO 6 I=1,2  
 DO 6 J=1,2  
 6 G2(I,J)=G(I,J)  
 D2=G2(1,1)\*G2(2,2)-G2(1,2)\*G2(2,1)  
 G2I(1,1)=G2(2,2)/D2  
 G2I(1,2)=-G2(1,2)/D2  
 G2I(2,1)=-G2(2,1)/D2  
 G2I(2,2)=G2(1,1)/D2  
 DO 7 I=1,2  
 DO 7 J=1,2  
 GI(I,4)=G2I(I,J)  
 GI(I,3)=0.  
 7 GI(3,J)=0.  
 GI(3,3)=0.  
 GO TO 8  
 5 CALL INVERT(G,GI)  
 8 IF(TESTR.GE.TESTRP) GO TO 9  
 DO 10 I=1,3  
 10 VEV(I)=VIT(I)  
 IF(TESTR.LT.ERRMIN) GO TO 14  
 CALL MXV(GI,ERR,DELV,3,3)  
 DO 11 I=1,3  
 11 DELV(I)=-DELV(I)  
 TESTRP=TESTR

```

DV=VMAG(DELV)
CALL UNITV(DELV,UDELV)
KNR=2.0*KNR
IF(KNR.GT.DV) KNR=DV
GO TO 12
9 KNR=KNR/10.0
12 DO 13 I=1,3
  KDELV(I)=KNR*UDELV(I)
13 VIT(I)=VEV(I)+KDELV(I)
  ITER=ITER+1
  KLV=VMAG(KDELV)
  KLVMIN=10.D-24
  IF(KLV.LT.JLVMIN) GO TO 14
  IF(ITER.LT.ITLMAX) GO TO 2
  WRITE(6,110)
  STOP
14 CONTINUE
  WRITE(6,107)
  WRITE(6,108)VEV
  WRITE(6,109)REVF,VEVF
  WRITE(6,103)RMVF,VMVF
  WRITE(6,104)REMF,VEMF
100 FORMAT(1H0,T8,'TO',T28,'TF'/1H ,1P2D20.11/1H ,T8,'REV',T68,
     1'VEV'/1H ,1P6D20.11)
101 FORMAT(1H0,T8,'ITER',T28,'VIT'/1H ,I10,10X,1P3D20.11)
102 FORMAT(1H ,T8,'REVF',T68,'VEVF'/1H ,1P6D20.11)
103 FORMAT(1H ,T8,'RMVF',T68,'VMVF'/1H ,1P6D20.11)
104 FORMAT(1H ,T8,'REMF',T68,'VEMF'/1H ,1P6D20.11)
105 FORMAT(1H ,T8,'ERR',T68,'TESTR'/1H ,1P4D20.11)
107 FORMAT(1H0,T8,'LAMBERT PROBLEM HAS CONVERGED')
108 FORMAT(1H0,T8,'CONVERGED VEV'/1H ,1P3D20.11)
109 FORMAT(1H0,T8,'REVF',T68,'VEVF'/1H ,1P6D20.11)
110 FORMAT(1H0,T8,'NO. OF LAMBERT ITERATIONS HAS REACHED MAXIMUM')
    RETURN
END

```

## SUBROUTINE DISP

```
IMPLICIT REAL*8(A-H,L-M,O-Z)
DIMENSION RSV(3),VSV(3),RSE(3),VSE(3),RSM(3),VSM(3),UXDS(3),
10(3),TEMP1(3),TEMP2(3),UZDS(3),UYDS(3),OMGSD(3),RDVD(3),VDVD(3),
2RDMD(3),VDMD(3),CDS(3,3),RDV(3),VDV(3),RDS(3),
3VDS(3),RDM(3),VDM(3),RDSD(3),VDSD(3)
DIMENSION RSB(3),VSB(3),RSD(3),VSD(3),REV(3),VEV(3),RMV(3),
1VMV(3),PV(6),RSL1(3),VSL1(3),RDL1(3),VDL1(3),RDL1D(3),VDL1D(3),
2URSV(3),URSE(3),UREV(3),REM(3),VEM(3)
COMMON/CONST/MS,ME,MM,GL1,AUM,UTIME,UVELM,ERRMAX,DTR
COMMON/TDATA/TO,T,H,RSV,VSV,REV,VEV,RMV,VMV,RSE,VSE,RSM,VSM,
IREM,VEM,RSL1,VSL1,RDVD,VDVD,RDSD,VDSD,RDMD,VDMD,
2RDL1D,VDL1D,PV,LM,LDM,ANGV,ANGE,ANGS
ESE=ME/(MS+ME)
MEM=MM/(ME+MM)
DO 1 I=1,3
RSB(I)=RSE(I)+MEM*REM(I)
VSB(I)=VSE(I)+MEM*VEM(I)
RSD(I)=RSE(I)
VSD(I)=VSE(I)
RSL1(I)=(1.-GL1)*RSB(I)
1 VSL1(I)=(1.-GL1)*VSB(I)
CALL UNITV(RSE,UXDS)
CALL VXV(RSE,VSE,Q)
CALL UNITV(Q,UZDS)
CALL VXV(UZDS,UXDS,UYDS)
DO 3 J=1,3
CDS(1,J)=UXDS(J)
CDS(2,J)=UYDS(J)
3 CDS(3,J)=UZDS(J)
RSEMAG=VMAG(RSE)
VY=DOT(UYDS,VSE,3)
DO 4 I=1,3
4 OMGSD(I)=UZDS(I)*VY/RSEMAG
DO 5 I=1,3
RDV(I)=RSV(I)-RSD(I)
VDV(I)=VSV(I)-VSD(I)
RDS(I)=-RSD(I)
VDS(I)=-VSD(I)
RDM(I)=RSM(I)-RSD(I)
VDM(I)=VSM(I)-VSD(I)
RDL1(I)=RSL1(I)-RSD(I)
5 VDL1(I)=VSL1(I)-VSD(I)
C COMPUTE STATE VECTOR IN ROTATING FRAME
CALL MXV(CDS,RDV,VDVD,3,3)
CALL VXV(OMGSD,RDV,TEMP1)
DO 6 I=1,3
6 TEMP2(I)=VDV(I)-TEMP1(I)
CALL MXV(CDS,TEMP2,VDVD,3,3)
CALL MXV(CDS,RDS,RDSD,3,3)
CALL VXV(OMGSD,RDS,TEMP1)
DO 7 I=1,3
7 TEMP2(I)=VDS(I)-TEMP1(I)
CALL MXV(CDS,TEMP2,VDSD,3,3)
CALL MXV(CDS,RDM,RDMD,3,3)
CALL VXV(OMGSD,RDM,TEMP1)
DO 9 I=1,3
```

```
9 TEMP2(I)=VDM(I)-TEMP1(I)
CALL MXV(CDS,TEMP2,VOMD,3,3)
CALL MXV(CDS,RDL1,RDL1D,3,3)
CALL VXV(OMGSD,RDL1,TEMP1)
DO 10 I=1,3
10 TEMP2(I)=VDL1(I)-TEMP1(I)
CALL MXV(CDS,TEMP2,VDL1D,3,3)
C COMPUTE ANGLES AT SUN,EARTH AND VEHICLE
CALL UNITV(RSE,URSE)
CALL UNITV(REV,UREV)
CALL UNITV(RSV,URSV)
ANGV=DARCOS(DOT(UREV,URSV,3))/DTR
ANGE=DARCOS(-DOT(URSE,UREV,3))/DTR
ANGS=180.0-(ANGV+ANGE)
RETURN
END
```

### SUBROUTINE DISP3

```
IMPLICIT REAL*8(A-H,L-M,O-Z)
DIMENSION REV(3),VEV(3),RMV(3),VMV(3),REM(3),VEM(3),REL(3),
1VEL(3),RDVD(3),VDVD(3),RDED(3),VDED(3),
2RDL(3),VDLD(3),PV(6),UXDE(3),UYDE(3),UZDE(3),Q(3),CDE(3,3),
3OMGED(3),RDV(3),VDV(3),RDE(3),VDE(3),RDL(3),
4VDL(3),TEMP1(3),TEMP2(3),UREM(3),URMV(3),UREV(3),RED(3),VED(3)
COMMON/CONST3/ME,MM,GAMMA,UDM,UTIME,UVELM,ERRMAX,DTR
COMMON/TDATA3/T0,T,H,REV,VEV,RMV,VMV,REM,VEM,REL,VEL,RDVD,
1VDVD,RDED,VDED,RDLD,VDLD,PV,LM,LDM,ANGV,ANGE,ANGM
EEM=ME/(ME+MM)
DO 1 I=1,3
  RED(I)=REM(I)
  VED(I)=VEM(I)
  REL(I)=(1.-GAMMA)*REM(I)
1  VEL(I)=(1.-GAMMA)*VEM(I)
  CALL UNITV(REM,UXDE)
  CALL VXV(REM,VEM,Q)
  CALL UNITV(Q,UZDE)
  CALL VXV(UZDE,UXDE,UYDE)
  DO 2 J=1,3
    CDE(1,J)=UXDE(J)
    CDE(2,J)=UYDE(J)
2  CDE(3,J)=UZDE(J)
  REMMAG=VMAG(REM)
  VY=DOT(UYDE,VEM,3)
  DO 3 I=1,3
3  OMGED(I)=UZDE(I)*VY/REMMAG
  DO 4 I=1,3
    RDV(I)=REV(I)-RED(I)
    VDV(I)=VEV(I)-VED(I)
    RDE(I)=-RED(I)
    VDE(I)=-VED(I)
    RDL(I)=REL(I)-RED(I)
4  VDL(I)=VEL(I)-VED(I)
  COMPUTE STATES IN ROTATING FRAME
  CALL MXV(CDE,RDV,RDVD,3,3)
  CALL VXV(OMGED,RDV,TEMP1)
  DO 5 I=1,3
5  TEMP2(I)=VDV(I)-TEMP1(I)
  CALL MXV(CDE,TEMP2,VDVD,3,3)
  CALL MXV(CDE,RDE,RDED,3,3)
  CALL VXV(OMGED,RDE,TEMP1)
  DO 6 I=1,3
6  TEMP2(I)=VDE(I)-TEMP1(I)
  CALL MXV(CDE,TEMP2,VDED,3,3)
  CALL MXV(CDE,RDL,RDLD,3,3)
  CALL VXV(OMGED,RDL,TEMP1)
  DO 8 I=1,3
8  TEMP2(I)=VDL(I)-TEMP1(I)
  CALL MXV(CDE,TEMP2,VDLD,3,3)
  COMPUTE ANGLES AT VEHICLE, EARTH AND MOON
  CALL UNITV(REM,UREM)
  CALL UNITV(RMV,URMV)
  CALL UNITV(REV,UREV)
  ANGV=DARCCOS(DOT(URMV,UREV,3))/DTR
  ANGM=DARCCOS(-DOT(UREM,URMV,3))/DTR
```

ANGE=180.0-(ANGV+ANGM)

RETURN

END

```

SUBROUTINE PTRAJ
IMPLICIT REAL*8(A-H,L-M,O-Z)
DIMENSION RSV(3),VSV(3),REV(3),VEV(3),RMV(3),VMV(3),RSE(3),
1VSE(3),RSM(3),VSM(3),RDVD(3),VDVD(3),RDSD(3),VDSD(3),
2RDMD(3),VDMD(3),PV(6),RSL1(3),VSL1(3),RDL1D(3),VDL1D(3)
DIMENSION REM(3),VEM(3)
COMMON/TDATA/T0,T,H,RSV,VSV,REV,VEV,RMV,VMV,RSE,VSE,RSM,VSM,
1REM,VEM,RSL1,VSL1,RDVD,VDVD,RDSD,VDSD,RDMD,VDMD,
2RDL1D,VDL1D,PV,LM,LDM,ANGV,ANGE,ANGS
COMMON/CONST/MS,ME,MM,GL1,AUM,UTIME,UVELM,ERRMAX,DTR
COMMON/FLAG/IMTX,IPV,IPTRAJ,IPVTM,IFILE,ITER,ITAR
TDAY=(T-T0)*UTIME
HDAY=H*UTIME
RSVMAG=VMAG(RSV)
REVMAG=VMAG(REV)
RMVMAG=VMAG(RMV)
WRITE(6,101)
WRITE(6,100)T,TDAY,H,RSVMAG,REVMAG,RMVMAG
C PRINT STATES IN INERTIAL S-FRAME
WRITE(6,100)RSV,VSV
WRITE(6,100)REV,VEV
WRITE(6,100)RMV,VMV
WRITE(6,101)
WRITE(6,100)RSE,VSE
WRITE(6,100)RSM,VSM
WRITE(6,100)REM,VEM
WRITE(6,100)RSL1,VSL1
WRITE(6,101)
C PRINT STATES IN ROTATING D-FRAME
WRITE(6,100)RDVD,VDVD
WRITE(6,100)RDSD,VDSD
WRITE(6,100)RDMD,VDMD
WRITE(6,100)RDL1D,VDL1D
WRITE(6,101)
WRITE(6,102)ANGV,ANGE,ANGS,HDAY
IF(IPV.EQ.0) GO TO 1
C PRINT PRIMER VECTOR
WRITE(6,100)PV
WRITE(6,103)LM,LDM
1 CONTINUE
WRITE(6,104)
100 FORMAT(1H ,1P6D20.11)
101 FORMAT(1H )
102 FORMAT(1H ,1P4D20.11)
103 FORMAT(1H ,1P2D20.11)
104 FORMAT(1H0,'-----')
RETURN
END

```

SUBROUTINE PTRAJ3

```
IMPLICIT REAL*8(A-H,L-M,O-Z)
DIMENSION REV(3),VEV(3),RMV(3),VMV(3),REM(3),VEM(3),REL(3),
1VEL(3),RDVD(3),VDVD(3),RDED(3),VDED(3),RDLD(3),VDLD(3),PV(6)
COMMON/FLAG/IMTX,IPV,IPTRAJ,IPVTM,IFILE,ITER,ITAR
COMMON/TDATA3/T0,T,H,REV,VEV,RMV,VMV,REM,VEM,REL,VEL,RDVD,
1VDVD,RDED,VDED,RDLD,VDLD,PV,LM,LDM,ANGV,ANGE,ANGM
TDAY=(T-T0)*UTIME
HDAY=H*UTIME
REVMAG=VMAG(REV)
RMVMAG=VMAG(RMV)
WRITE(6,101)
WRITE(6,100)T,TDAY,H,HDAY,REVMAG,RMVMAG
C PRINT STATES IN INERTIAL E-FRAME
WRITE(6,100)REV,VEV
WRITE(6,100)RMV,VMV
WRITE(6,100)REM,VEM
WRITE(6,100)REL,VEL
WRITE(6,101)
C PRINT STATES IN ROTATING D-FRAME
WRITE(6,100)RDVD,VDVD
WRITE(6,100)RDED,VDED
WRITE(6,100)RDLD,VDLD
WRITE(6,102)ANGV,ANGE,ANGM
IF(IPV.EQ.0) GO TO 1
WRITE(6,101)
WRITE(6,100)PV
WRITE(6,103)LM,LDM
100 FORMAT(1H ,1P6D20.11)
101 FORMAT(1H )
102 FORMAT(1H ,1P3D20.11)
103 FORMAT(1H ,1P2D20.11)
1 CONTINUE
RETURN
END
```

SUBROUTINE FDATA

```
IMPLICIT REAL*8(A-H,K-M,O-Z)
DIMENSION RSV(3),VSV(3),REV(3),VEV(3),RMV(3),VMV(3),RSE(3),
1VSE(3),RSM(3),VSM(3),RSL1(3),VSL1(3),RDVD(3),VDVD(3),RDSD(3),
2VDSD(3),RDMD(3),VDMD(3),RDL1D(3),VDL1D(3),PV(6),
3DUM(9),REM(3),VEM(3)
COMMON/TDATA/TO,T,H,RSV,VSV,REV,VEV,RMV,VMV,RSE,VSE,RSM,VSM,
1REM,VEM,RSL1,VSL1,RDVD,VDVD,RDSD,VDSD,RDMD,VDMD,
2RDL1D,VDL1D,PV,LM,LDM,ANGV,ANGE,ANGS
C EACH RECORD CONSISTS OF 100 DOUBLE PRECISION UNFORMATED NUMBERS.
C FILED SEQUENTIALLY. THE LAST 15 NUMBERS ARE BLANKS FILLED WITH
C ZEROS AND MAY BE USED FOR FUTURE EXPANSION.
DO 1 I=1,15
1 DUM(I)=0.
RSVMAG=VMAG(RSV)
VSVMAG=VMAG(VSV)
REVMAG=VMAG(REV)
VEVMAG=VMAG(VEV)
RMVMAG=VMAG(RMV)
VMVMAG=VMAG(VMV)
WRITE(8)T,H,RSV,VSV,REV,VEV,RMV,VMV,RSE,VSE,RSM,VSM,REM,VEM,
1RSL1,VSL1,RDVD,VDVD,RDSD,VDSD,RDMD,VDMD,RDL1D,VDL1D,
2PV,LM,LDM,ANGV,ANGE,ANGS,RSVMAG,VSVMAG,REVMAG,VEVMAG,RMVMAG,
3VMVMAG,DUM
RETURN
END
```

```
SUBROUTINE FDATA3
IMPLICIT REAL*8(A-H,K-M,O-Z)
DIMENSION REV(3),VEV(3),RMV(3),VMV(3),REM(3),VEM(3),REL(3),
1VEL(3),RDVD(3),VDVD(3),RDED(3),VDED(3),RDLD(3),VDLD(3),PV(6),
2DUM(14)
COMMON/TDATA3/T0,T,H,REV,VEV,RMV,VMV,REM,VEM,REL,VEL,RDVD,
1VDVD,RDED,VDED,RDLD,VDLD,PV,LM,LDM,ANGV,ANGE,ANGM
DIT 1 I=1,14
1 DUM(I)=0.
REVMAG=VMAG(REV)
VEVMAG=VMAG(VEV)
RMVMAG=VMAG(RMV)
REMMAG=VMAG(REM)
VEMMAG=VMAG(VEM)
WRITE(8)T,H,REV,VEV,RMV,VMV,REM,VEM,REL,VEL,RDVD,VDVD,RDED,
1VDED,RDLD,VDLD,PV,LM,LDM,ANGV,ANGE,ANGM,DUM
RETURN
END
```

```

SUBROUTINE COMAUG(F,G,TSI,LT,V,L,FG,GG)
IMPLICIT REAL*8(A-H,L-N,O-Z)
DIMENSION TSI(3),G(3),LTLI(3,3),LT(3,3),L(3,3),NU(3),GG(3),
1TEMP1(3,3),TEMP2(3,3),DUM(3),V(3,3)
CALL MTRANS(LT,L,3,3)
CALL MXM(LT,V,TEMP1,3,3,3)
CALL MXM(TEMP1,L,TEMP2,3,3,3)
CALL INVERT(TEMP2,LTLI)
CALL MXM(LTLI,LT,TEMP1,3,3,3)
CALL MXM(TEMP1,V,TEMP2,3,3,3)
CALL MXV(TEMP2,G,NU,3,3)
DO 1 I=1,3
1 NU(I)=-NU(I)
FG=F+DOT(NU,TSI,3)
CALL MXV(L,NU,DUM,3,3)
DO 2 I=1,3
2 GG(I)=G(I)+DUM(I)
WRITE(6,100)FG,GG
WRITE(6,101)
100 FORMAT(1H ,T8,'FG',T28,'GG'/1H ',1P4D20.11)
101 FORMAT(1H0,T8,'-----')
RETURN
END

```

```
SUBROUTINE COMDX(LTS,LS,TSIS,DX)
IMPLICIT REAL*8(A-H,L,O-Z)
DIMENSION LTS(3,3),LS(3,3),TSIS(3),DX(3),TEMP1(3,3),TEMP2(3,3)
CALL MXM(LTS,LS,TEMP1,3,3,3)
CALL INVERT(TEMP1,TEMP2)
CALL MXM(LS,TEMP2,TEMP1,3,3,3)
CALL MXV(TEMP1,TSIS,DX,3,3)
DO 1 I=1,3
1 DX(I)=-DX(I)
RETURN
END
```

```
SUBROUTINE UPX(XD,FD,TESTRD,GD,TSID,LTD,LD,FGD,GGD,S11D,S12D,  
1S21D,S22D,UVID,UVFD,X,F,TESTR,G,TSI,LT,L,FG,GG,S11,S12,S21,S22,  
2UVI,UVF)  
IMPLICIT REAL*8(A-H,L,N,O-Z)  
DIMENSION XD(3),GD(3),TSID(3),LTD(3,3),LD(3,3),X(3),G(3),  
1TSI(3),LT(3,3),L(3,3),S11D(3,3),S12D(3,3),S21D(3,3),S22D(3,3),  
2S11(3,3),S12(3,3),S21(3,3),S22(3,3),GG(3),UVID(3),UVFD(3),  
3UVI(3),UVF(3),GGD(3)  
F=FD  
TESTR=TESTRD  
FG=FGD  
DO 1 I=1,3  
X(I)=XD(I)  
G(I)=GD(I)  
TSI(I)=TSID(I)  
GG(I)=GGD(I)  
UVI(I)=UVID(I)  
UVF(I)=UVFD(I)  
DO 1 J=1,3  
LT(I,J)=LTD(I,J)  
L(I,J)=LD(I,J)  
S11(I,J)=S11D(I,J)  
S12(I,J)=S12D(I,J)  
S21(I,J)=S21D(I,J)  
S22(I,J)=S22D(I,J)  
1 CONTINUE  
RETURN  
END
```

```

SUBROUTINE PVEC(T,R,V,PVO,STM,PV,LM,LDM)
IMPLICIT REAL*8(A-H,L,O-Z)
DIMENSION R(3),V(3),PVO(6),PV(6),STM(6,6),DL(3),DLD(3),
1RTM(3),VTM(3),PVTM(3),PVDTM(3),STNTM(6,6)
COMMON/FLAG/IMTX,IPV,IPTRAJ,IPVTM,IFILE,ITER,ITAR
COMMON/CTM/TTM,RTM,VTM,LTM,LDTM,PVTM,PVDTM,STNTM
CALL MXV(STM,PVO,PV,6,6)
DO 3 I=1,3
  DL(I)=PV(I)
3 DLD(I)=PV(I+3)
  LM=VMAG(DL)
  LDM=DOT(DL,DLD,3)/LM
  IF(IPVTM.LE.0) GO TO 2
  IF(LM.LE.LTM) GO TO 2
  LTM=LM
  LDTM=LDM
  TTM=T
  DO 1 I=1,3
    RTM(I)=R(I)
    VTM(I)=V(I)
    PVTM(I)=DL(I)
    PVDTM(I)=DLD(I)
    DO 1 J=1,3
      STNTM(I,J)=STM(I,J)
      STNTM(I,J+3)=STM(I,J+3)
      STNTM(I+3,J)=STM(I+3,J)
1 STNTM(I+3,J+3)=STM(I+3,J+3)
2 CONTINUE
  RETURN
END

```

```
SUBROUTINE RVEMV(RSV,VSV,RSE,VSE,RSM,VSM,REV,VEV,RMV,VMV,  
1REM, VEM)  
IMPLICIT REAL*8(A-H,O-Z)  
DIMENSION RSV(3),VSV(3),RSE(3),VSE(3),RSM(3),VSM(3),REV(3),  
1VEV(3),RMV(3),VMV(3),REM(3),VEM(3)  
DO 1 I=1,3  
REV(I)=-RSE(I)+RSV(I)  
VEV(I)=-VSE(I)+VSV(I)  
RMV(I)=-RSM(I)+RSV(I)  
VMV(I)=-VSM(I)+VSV(I)  
REM(I)=-RSE(I)+RSM(I)  
1 VEM(I)=-VSE(I)+VSM(I)  
RETURN  
END
```

```
SUBROUTINE MXV(A,V,VN,M,N)
IMPLICIT REAL*8(A-H,O-Z)
MATRIX VECTOR MULTIPLICATION A(M,N) V(N)=VN(M)
DIMENSION A(M,N),V(N),VN(M)
DO 4 I=1,M
S=0.
DO 3 J=1,N
3 S=S+A(I,J)*V(J)
4 VN(I)=S
RETURN
END
```

C

```
SUBROUTINE VVT(V, VV, IDIM)
IMPLICIT REAL*8(A-H,O-Z)
OUTER PRODUCT OF 2 VECTORS OF DIMENSION IDIM
DIMENSION V(IDIM),VV(IDIM, IDIM)
DO 1 I=1, IDIM
DO 1 J=1, IDIM
1 VV(I,J)=V(I)*V(J)
RETURN
END
```

DOUBLE PRECISION FUNCTION DOT(V1,V2, IDIM)

IMPLICIT REAL\*8(A-H,O-Z)

DOT PRODUCT OF 2 VECTORS

DIMENSION V1(IDIM),V2(IDIM)

S=0.

DO 1 I=1, IDIM

S=S+V1(I)\*V2(I)

DOT=S

RETURN

END

C DOUBLE PRECISION FUNCTION VMAG(V)  
C IMPLICIT REAL\*8(A-H,O-Z)  
C MAGNITUDE OF VECTORS OF DIMENSION IDIM  
C DIMENSION V(3)  
C S=0.  
C DO 1 I=1,3  
C S=S+V(I)\*\*2  
C VMAG=DSQRT(S)  
C RETURN  
C END

C

```
SUBROUTINE INVERT(B,BI)
IMPLICIT REAL*8(A-H,O-Z)
INVERSION OF A 3X3 MATRIX
DIMENSION B(3,3),BI(3,3)
D=B(1,1)*(B(2,2)*B(3,3)-B(2,3)*B(3,2))+B(2,1)*(B(1,3)*B(3,2)-
1B(1,2)*B(3,3))+B(3,1)*(B(1,2)*B(2,3)-B(1,3)*B(2,2))
BI(1,1)=(B(2,2)*B(3,3)-B(2,3)*B(3,2))/D
BI(2,1)=(B(2,3)*B(3,1)-B(2,1)*B(3,3))/D
BI(3,1)=(B(2,1)*B(3,2)-B(2,2)*B(3,1))/D
BI(1,2)=(B(1,3)*B(3,2)-B(1,2)*B(3,3))/D
BI(2,2)=(B(1,1)*B(3,3)-B(1,3)*B(3,1))/D
BI(3,2)=(B(1,2)*B(3,1)-B(1,1)*B(3,2))/D
BI(1,3)=(B(1,2)*B(2,3)-B(1,3)*B(2,2))/D
BI(2,3)=(B(1,3)*B(2,1)-B(1,1)*B(2,3))/D
BI(3,3)=(B(1,1)*B(2,2)-B(1,2)*B(2,1))/D
RETURN
END
```

```
SUBROUTINE UNITV(A,UA)
IMPLICIT REAL*8(A-H,D-Z)
DIMENSION A(3),UA(3)
S=0.
DO 1 I=1,3
1 S=S+A(I)**2
AMAG=DSQRT(S)
DO 2 I=1,3
2 UA(I)=A(I)/AMAG
RETURN
END
```

SUBROUTINE VXV(V1,V2,V3)  
IMPLICIT REAL\*8(A-H,O-Z)  
C CROSS PRODUCT OF 2 3-DIMENSIONAL VECTORS  
DIMENSION V1(3),V2(3),V3(3)  
V3(1)=V1(2)\*V2(3)-V1(3)\*V2(2)  
V3(2)=V1(3)\*V2(1)-V1(1)\*V2(3)  
V3(3)=V1(1)\*V2(2)-V1(2)\*V2(1)  
RETURN  
END

C

```
SUBROUTINE MTRANS(A,B,IROW,ICOL)
IMPLICIT REAL*8(A-H,O-Z)
TRANPOSE A MATRIX OF IROW X ICOL
DIMENSION A(IROW,ICOL),B(ICOL,IROW)
DO 1 I=1,IROW
DO 1 J=1,ICOL
1 B(J,I)=A(I,J)
RETURN
END
```

C

```
SUBROUTINE MXM(A,B,C,K,L,M)
IMPLICIT REAL*8(A-H,O-Z)
  MATRIX MULTIPLICATION A(K,L) B(L,M)=C(K,M)
DIMENSION A(K,L),B(L,M),C(K,M)
DO 4 I=1,K
DO 4 J=1,M
S=0.
DO 3 N=1,L
3 S=S+A(I,N)*B(N,J)
4 C(I,J)=S
RETURN
END
```

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